Information Storage and Processing for Web Search

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Outline

• Some info about ISTI-CNR

- Introduction to Information Retrieval and Web Search
- Classical query processing

Learning to Rank and query processing

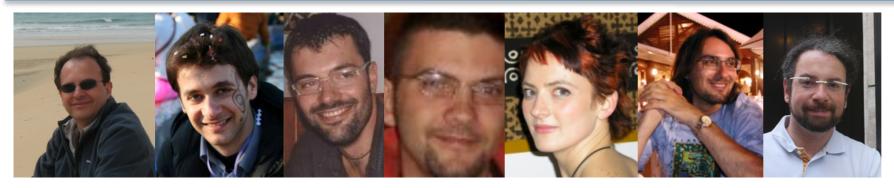


CNR -> ISTI -> HPC









7 researchers



2 post-doc fellows



3 research associates



6 PhD students



Main Research Topics

***** Web Search & data mining

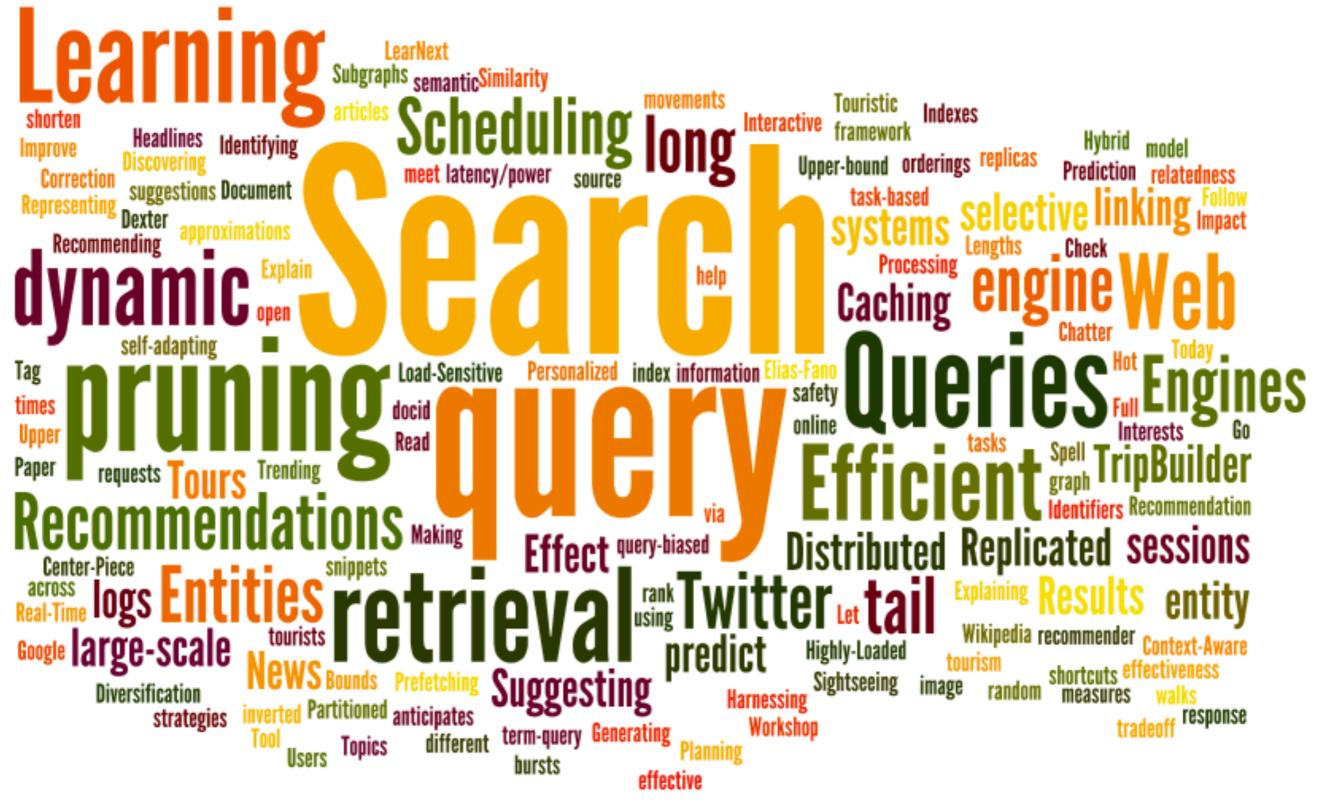
- Responsiveness of large-scale search systems
- (Machine learned) ranking, prediction, recommendation, diversification
- Social media analysis
- Semantic Enrichment and Entity Linking
- Storage and Indexing of large amounts of data

***** Cloud and Distributed computing

- Cloud federations, Resource Management
- Network overlays for P2P and Big Data
- Scalable data analysis with Hadoop Map-Reduce, Giraph, Spark, etc



From paper titles 2011-2013





Our Strengths

- Highly-motivated group of (mostly u) young researchers
- Papers accepted at all the main top conferences on Web IR & DM
- Attractive to HQ students, former PhDs now at Twitter 3, Facebook 3, Yahoo! and Tiscali 5
- Good portfolio of EC projects, good international and national connections with academia and industry



Products / Achievements

Production Systems

istella

Learning to Rank for Tiscali istella, feature tuning, near-duplicate detection, massive Hadoop MapReduce computations

Learning to Rank Metadata Records for Europeana, Entity suggestion





Framework for implementing and evaluating entity linking algorithms.

http://dexter.isti.cnr.it

Fast and Scalable Learning to Rank with QuickRank

http://quickrank.isti.cnr.it

Budgeted Sightseeing Tours Planning exloiting Social Media

http://tripbuilder.isti.cnr.it

Università La Sapienza – 18 October 2016

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Collaboration with istella





Information Retrieval

- Information Retrieval (IR) is finding material (usually documents) of an unstructured nature (usually text) that satisfies an information need from within large collections (usually stored on computers).
- These days we frequently think first of Web Search, but there are many other cases:
 - E-mail search
 - Searching your laptop
 - Corporate knowledge bases
 - Legal information retrieval
 - Patent Retrieval
 - Medical Retrieval



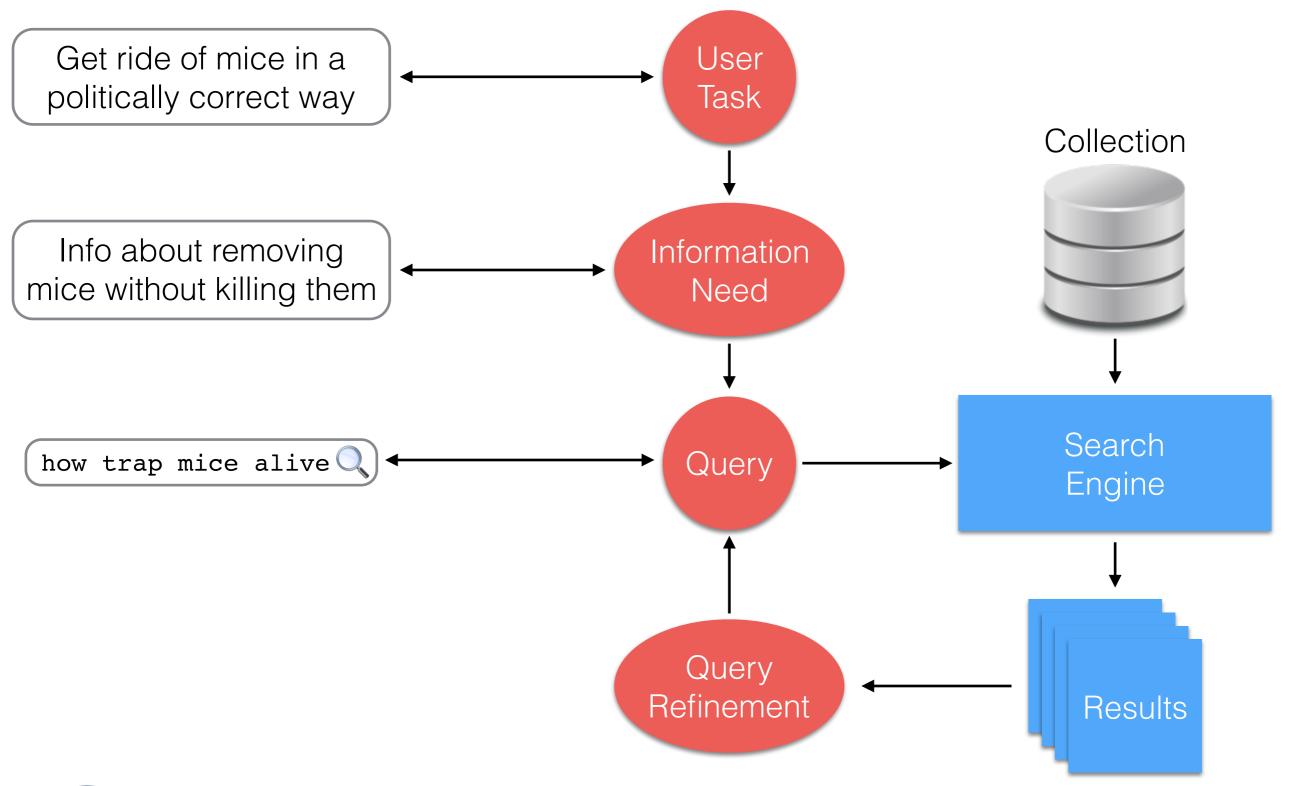
Basic Assumptions

• Collection: A set of textual documents

 Goal: Retrieve documents with information that is relevant to the user's information need and helps the user complete a task



Classical IR Model





Search in 1620

- Which plays of Shakespeare contain the words
 Brutus AND Caesar but NOT Calpurnia?
- One could grep all of Shakespeare's plays for Brutus and Caesar, then strip out lines containing Calpurnia?
- Why is that not the answer?
 - Slow (for large corpora)
 - NOT Calpurnia is non-trivial
 - Other operations (e.g., find the word Romans near countrymen) not feasible
 - Ranked retrieval (only best documents to return)



Term-Document Incidence Matrix

	Antony and Cleopatra	Julius Caesar	The Tempest	Hamlet	Othello	Macbeth	
Antony	1	1	0	0	0	1	
Brutus	1	1	0	1	0	0	
Caesar	1	1	0	1	1	1	
Calpurnia	0	1	0	0	0	0	
Cleopatra	1	0	0	0	0	0	
mercy	1	0	1	1	1	1	
worser	1	0	1	1	1	0	
Brutus	AND Caesar BUT NC)T Calnurnia	1 if pl	ay cont	tains w	ord	
Brutus AND Caesar BUT NOT Calpurnia				0 otherwise			



Incidence Vectors

- So we have a 0/1 vector for each term.
- To answer query: take the vectors for Brutus, Caesar and Calpurnia (complemented) and perform bitwise AND. 110100 AND

110111 AND 101111 = 100100

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worser	1	0	1	1	1	0



Bigger Collections

- Consider N = 1 million documents, each with about 1000 words.
- Average 6 bytes/word including spaces/punctuation
- 6GB of data in the documents.
- Say there are M = **500K distinct terms** among these.
- 500K x 1M matrix has **0.5T** 0's and 1's.
- But it has no more than one **1G** 1's.
- Matrix is **extremely sparse**.
- What's a better representation?



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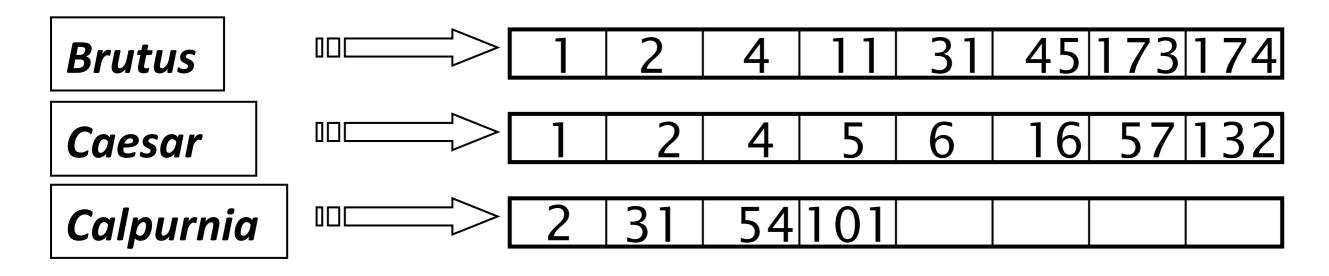
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***** We only record the 1's positions.



Inverted Index

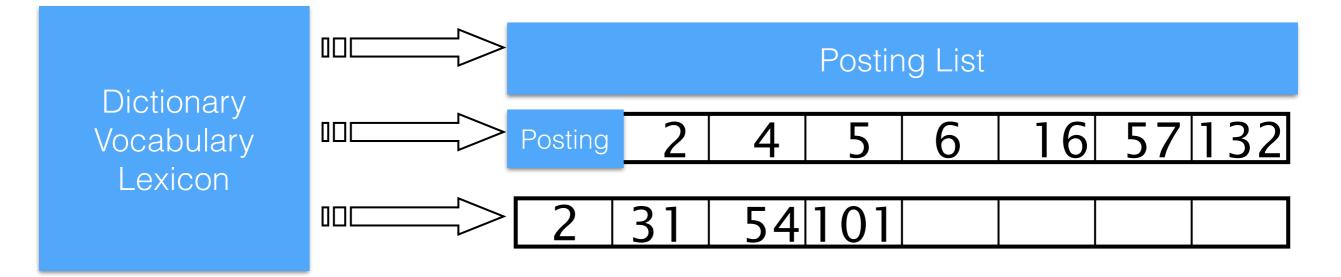
- For each term t, we must store a list of all documents that contain t.
- Identify each doc by a docid, a document serial number.



- Can we used fixed-size arrays for this?
- We need variable-size **posting lists**.

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Boolean queries: exact match

- The Boolean retrieval model is being able to ask a query that is a Boolean expression:
 - Boolean queries are queries using AND, OR and NOT to join query terms
 - Views each document as a set of words
 - Is precise: document matches condition or not.
- Perhaps the **simplest model** to build an IR system on
- Primary commercial retrieval tool for **3 decades**.
- Many search systems you still use are boolean:
 - Email, library catalog, Mac OS X Spotlight



Ranked Retrieval

 Ranking is (one of) the most important challenges in Web Search

please, find the document i need

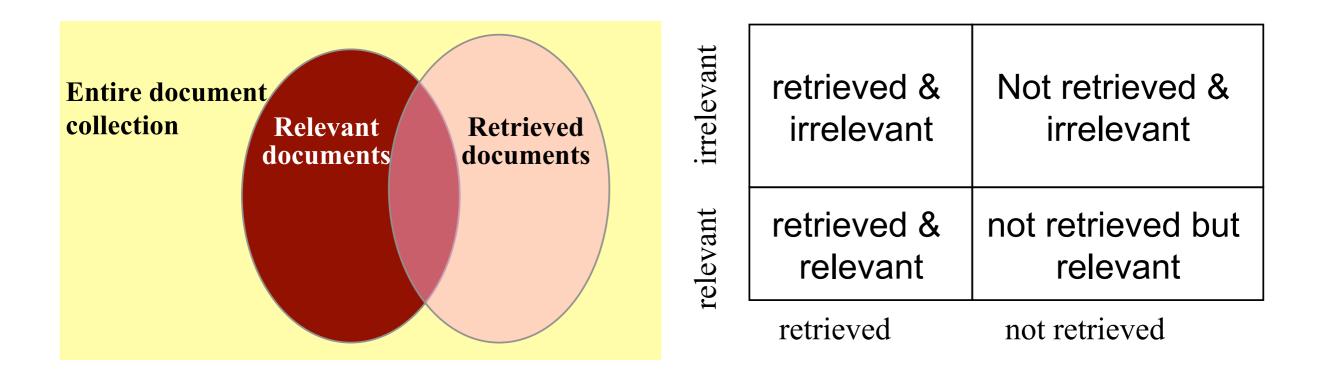
I'm Feeling Lucky

• We define Ranking as the problem of sorting a set of documents according to their **relevance** to the user query.



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Precision and Recall



 $recall = \frac{Number of relevant documents retrieved}{Total number of relevant documents}$

 $precision = \frac{Number of relevant documents retrieved}{Total number of documents retrieved}$



Precision and Recall

 Rather than evaluating the full list of documents, look only at the top k:

P@k R@k

There are more advanced measures:
 MAP@k
 Mean Average Precision

NDCG@k

Normalized Discounted Cumulative Gain



BM25

 BM25 is a probabilistic model: using term independence assumption to approximate the document probability of being relevant

$$BM25(d,q) = \sum_{t} IDF_t \tau(F_t)$$

- IDF_t=log(N/n_t) is the inverse document frequency
 - N is the number of docs in the collection
 - n_t is the number of docs containing t
- Frequent terms are not very specific, and their contribution is reduced



BM25

$$BM25(d,q) = \sum_{t} IDF_t \tau(F_t)$$

$$F_t = \frac{f_{t,d}}{1 - b + b \cdot l_d/L} \qquad \qquad \tau(F_t) = \frac{F_t}{k + F_t}$$

- f_{t,d} is the frequency of term t in document d
- Id is the length of document d
 - longer documents are less important
- L is the average document length in the collection
- b determines the importance of I_d
- τ () is a **smoothing function**, modelling non-linearity of terms contribution



Query Processing Breakdown

Pre-process the query (e.g., tokenisation, stemming)

- Lookup the statistics for each term in the lexicon
- Process the postings for each query term, computing
 - scores for documents to identify the final retrieved set
- Output the retrieved set with metadata (e.g., URLs)



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Document-at-a-Time (DAAT)

 Input: The index I of the collection The query q
 Output: A set D containing the top K ranked documents

```
Allocate an empty list L
For each term t in q
      Scan index I and grab posting list I_t
      Calculate w_q(t)
While all posting lists I_t have postings
      Set d \leftarrow \infty
      For each posting list I_t
            If current document id in I_t < d
                 d \leftarrow \text{current document id in } I_t
      Set A \leftarrow 0
      For each posting list I_t
           If current document id in I_t = d
                 A \leftarrow A + w_q(t) \cdot w_q(d, t)
                 Move I_t one step ahead to the next document id
      If A \neq 0
            Insert A in L
Select the K highest scores in L and put the corresponding docids in D
```



Dynamic Pruning

- •What takes time?
 - Number of query terms
 - Longer queries have more terms with posting lists to process
 - Length of posting lists
 - More postings takes longer times

Aim: avoid (unnecessary) scoring of posting



Safeness

• Safe pruning: the output ordering of the strategy is identical to the output ordering of the full processing

• Safe up to rank K: the first K documents are identical to the first K documents of the full processing

• Approximate: no guarantees on final ordering of document w.r.t. full processing



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DAAT Pruning

- MaxScore (Turtle & Flood, IPM 31(6), 1995)
 - Early termination: does not compute scores for documents that won't be retrieved
 - By comparing upper bounds with threshold
 - Suitable for TAAT as well
- WAND (Broder et al., CIKM 2003)
 - Approximate evaluation: does not consider documents with approximate scores (sum of upper bounds) lower than threshold
 - Exploit skipping
- BlockMaxWAND (Ding & Suel, SIGIR 2011)
 - Two levels: initially on blocks (128 postings), then on postings
 - Approximate evaluation: does not consider documents with approximate scores (sum of upper bounds) lower than threshold
 - Exploit skipping
- All three use docids sorted posting lists



Some (Unpublished) Results (50 M docs)

Ranking	Num Terms						
Algorithm	1	2	3	4	5	6	7
Ranked And	43.59	38.08	32.68	25.23	29.26	17.57	15.78
Ranked Or	43.05	261.59	536.06	807.05	1,107.93	1,402.26	1,756.52
MaxScore	45.01	48.21	51.06	57.28	75.66	95.06	117.61
Wand	62.62	44.98	48.24	55.27	69.39	98.47	120.70
BlockMaxWand	0.71	13.11	40.69	64.62	99.95	149.94	192.65

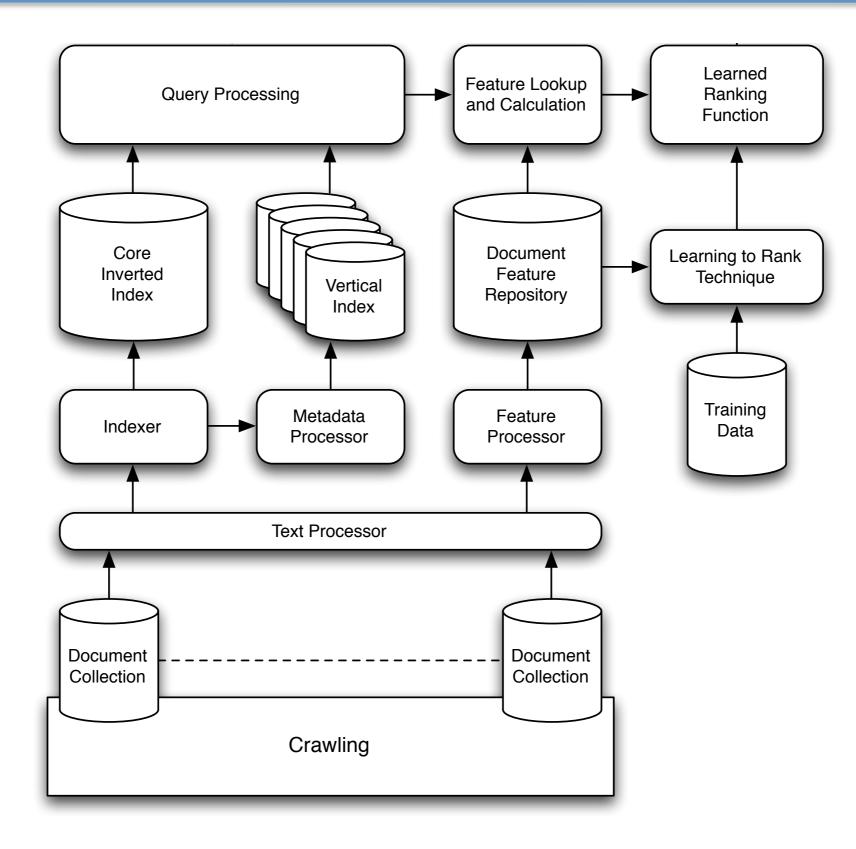
Average Response Times (msec)

Ranking		Num Terms						
Algorithm	1	2	3	4	5	6	7	
Ranked And	265.25	182.84	136.33	101.75	94.99	66.70	61.26	
Ranked Or	260.74	838.04	1,296.98	1,759.49	2,209.58	2,663.02	3,130.37	
MaxScore	245.03	189.39	174.92	175.44	215.57	253.29	313.25	
Wand	387.55	210.37	184.10	182.05	210.05	289.27	337.07	
BlockMaxWand	1.64	43.05	140.12	201.39	280.05	394.48	500.16	



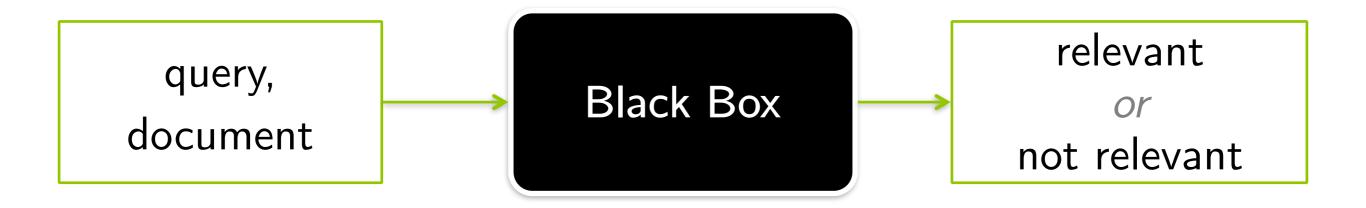
95% Response Time (msec)

Web Search Engine



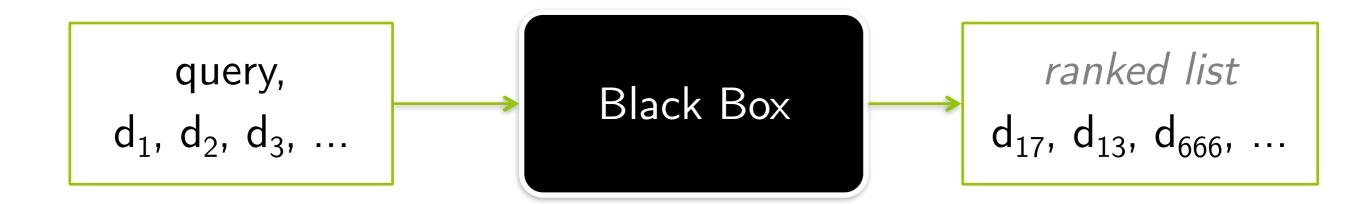


Learning to Rank is not classification





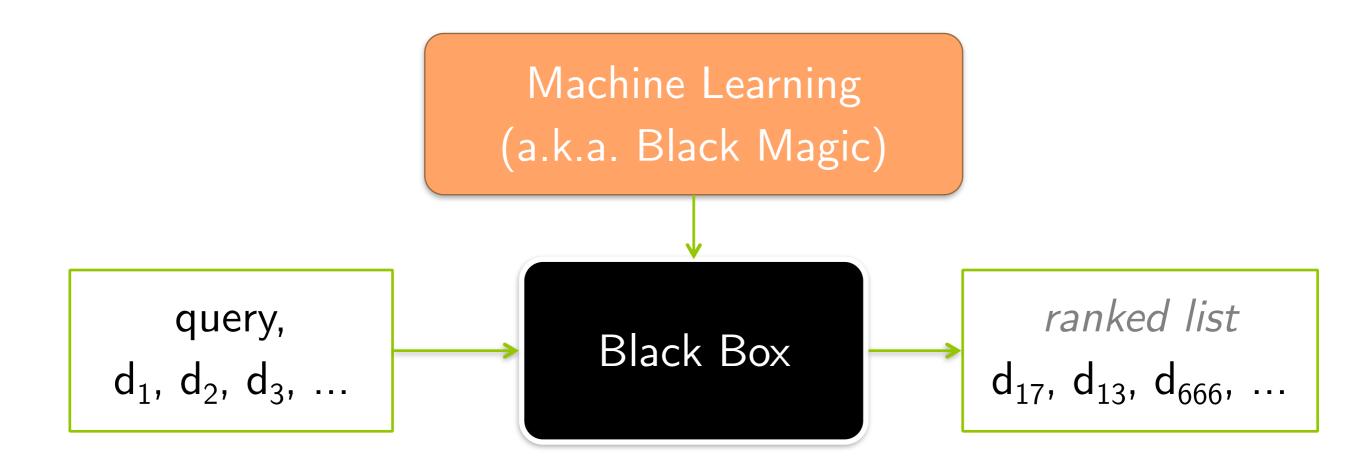
Learning to Rank is:



The goal is to learn the ranking, not the label !

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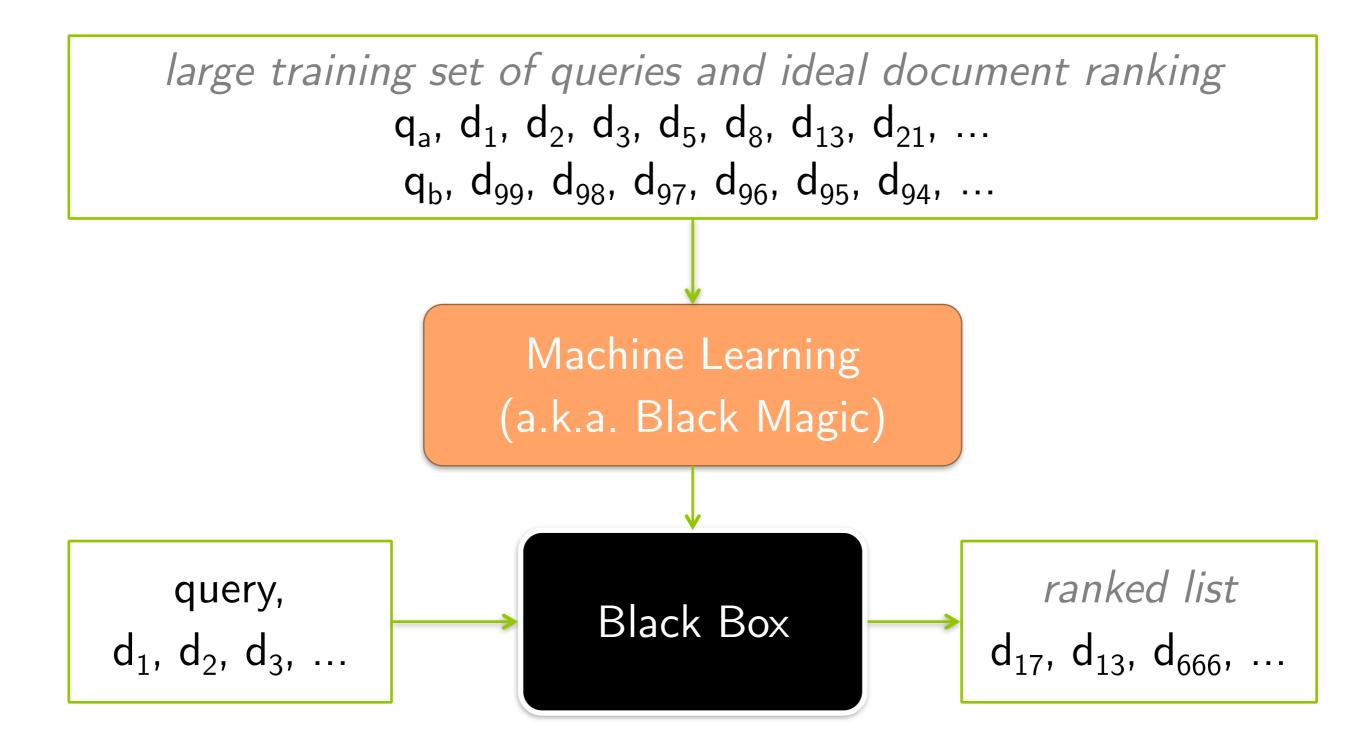
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Normalized Discounted Cumulative Gain NDCG@K

- Consider only the top-K ranked documents, and sum up (cumulate) their contribution
- The contribution (gain) of a result depends on its relevance label
- Contribution is diminished (discounted) if the result is in the "bottom" positions
- Normalize between 0 and 1

$$DCG@k = \sum_{i=1}^{k} \frac{2^{rel_i} - 1}{\log(i+1)} \quad NDCG@k = \frac{DCG@k}{IDCG@k}$$

rel; is the relevance label of the *i-th* result (e.g., 1..5)
 IDCG@k is the score of the ideal ranking

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Learning to Rank Approaches

• Pointwise

- Each query-document pair is associated with a score
- The objective is to predict such score
 - Can be considered a regression problem
- Does not consider the position of a document into the result list

• Pairwise

- We are given pairwise preferences, d1 is better than d2 for query
 q
- The objective is to predict a score that preserves such preferences
 - Can be considered a classification problem
- It partially considers the position of a document into the result list
- Listwise
 - We are given the ideal ranking of results for each query
 - NB: It might not be trivial to produce such training set
 - Objective maximize the quality of the resulting ranked list
 - We need some improved approach...

Decision Tree

- Tree-like structure similar to a flow chart.
- Every internal node denotes a test over an attribute/feature
 - Outgoing edges correspond to the test possible outcomes
- Every leaf node is associated to a class label (if it is a classification task) or class distribution or predicted value (if it is a regression task)
- It is used to label a new data instance on the basis of its attributes
- Runs tests on the data instance attributes and traverses the tree according to the tests results
 - Starting form the root, the data instances follows a path to a leaf
 - The label associated to the leaf is the prediction of the decision tree.





• We want to learn a predictor incrementally:

$$F^*(x) = \sum_{m=0}^{M} f_m(x)$$

• Input: a learning sample { (x_i, y_i) : i = 1, ..., N }



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- For t = 1 to M:
 - Regression tree predicts the residual error
 - For i = 1 to N, compute the residuals

$$\mathsf{r}_\mathsf{i} \leftarrow \mathsf{r}_\mathsf{i-1} - \hat{y}_\mathsf{t-1}(\mathsf{x}_\mathsf{i})$$

- Build a regression tree from the learning sample { (x_i,y_i): i = 1, ..., N }
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- Return the model $\hat{y}(x) = \hat{y}_0(x) + \hat{y}_1(x) + ... + \hat{y}_M(x)$



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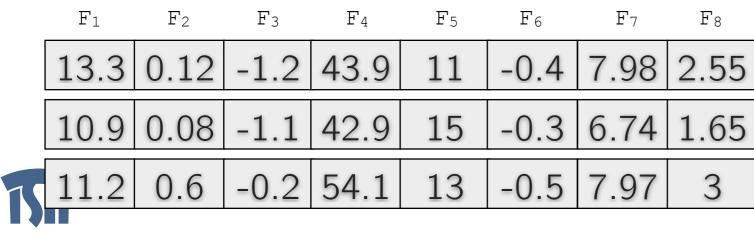
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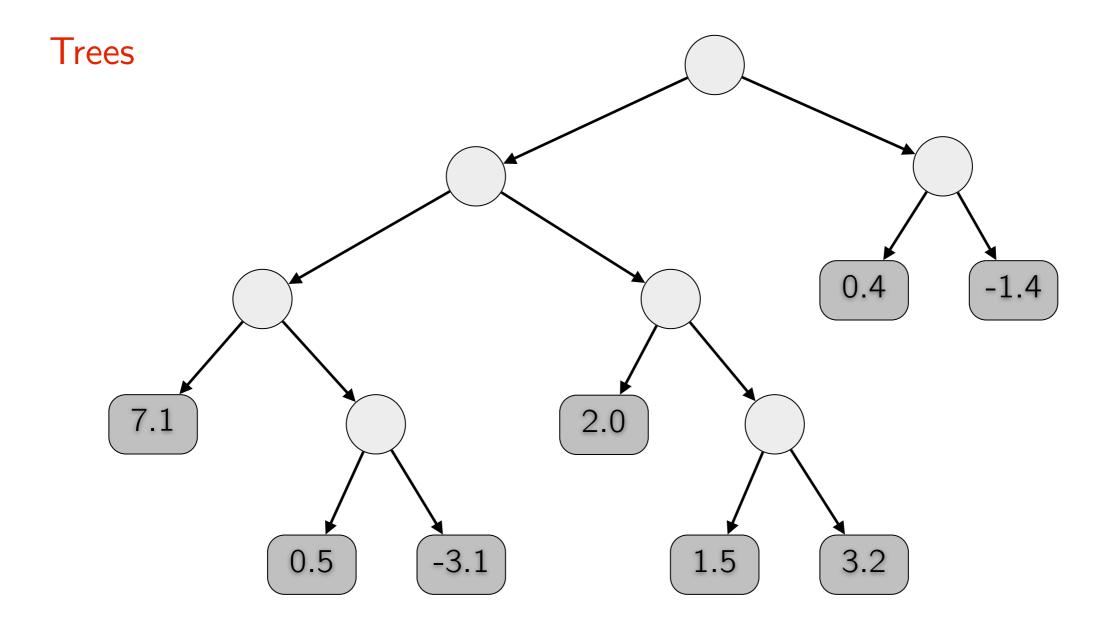
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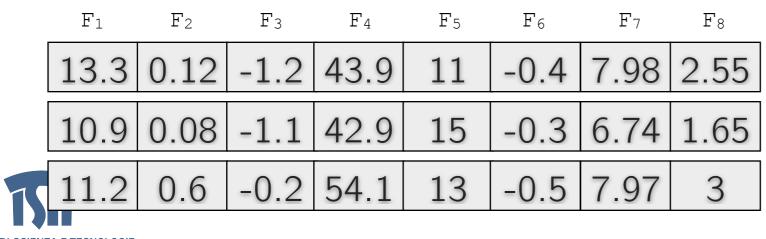
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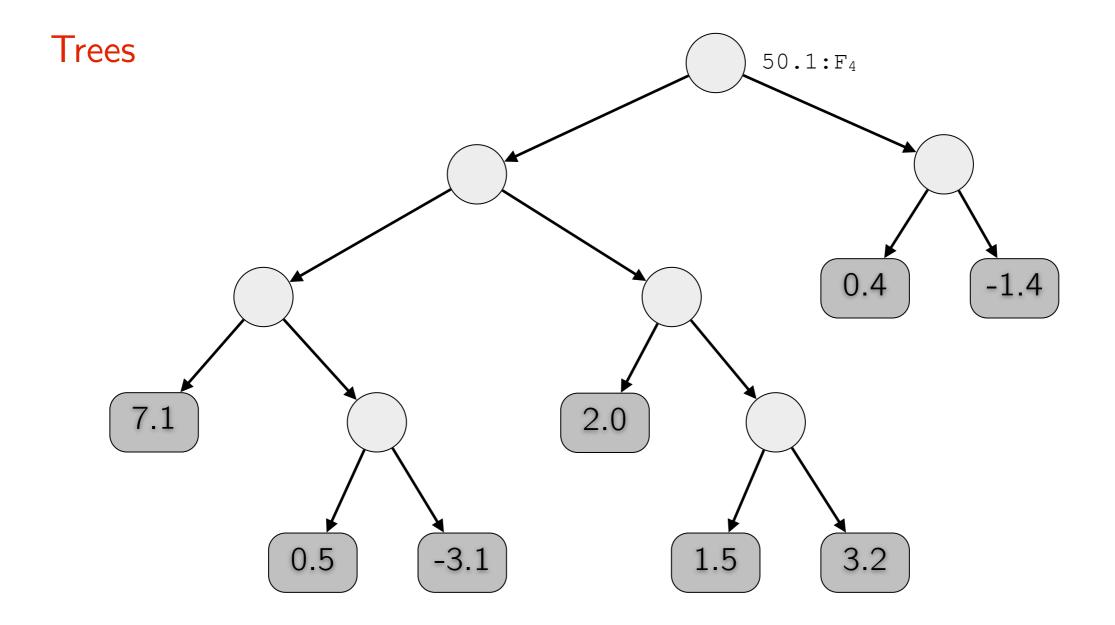
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- Return the model $\hat{y}(x) = \hat{y}_0(x) + \hat{y}_1(x) + ... + \hat{y}_M(x)$
- Function f_m should be easy to be learnt:
 - Decision stump: trees with one node and two leaves

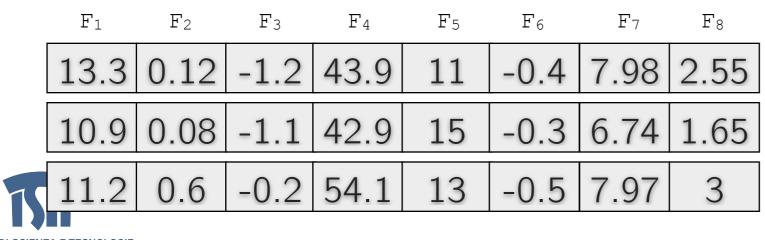


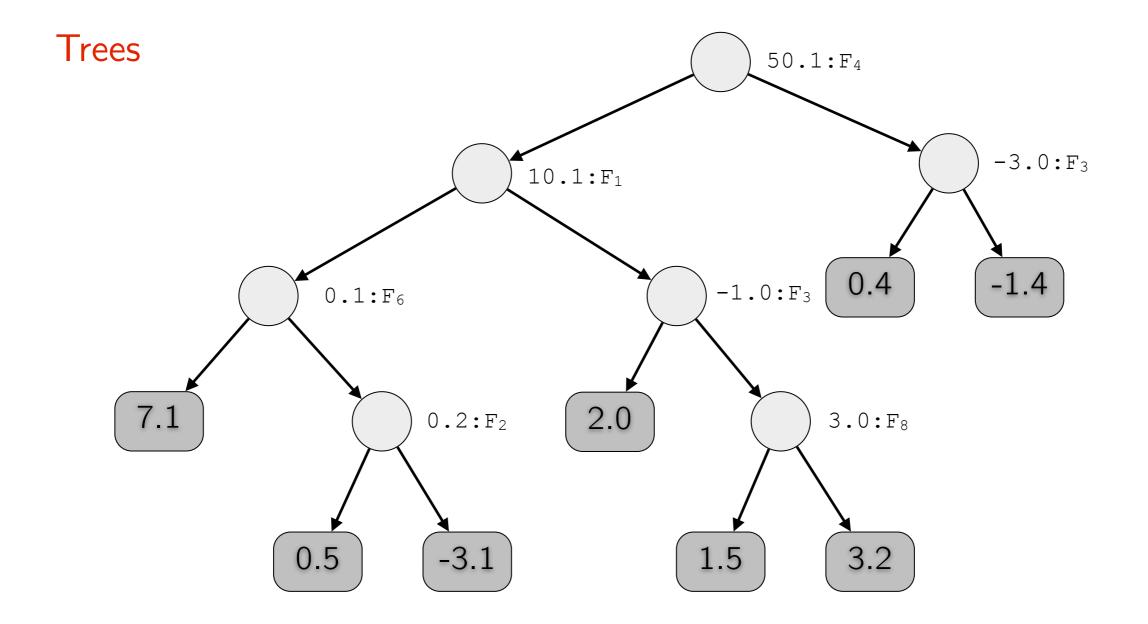


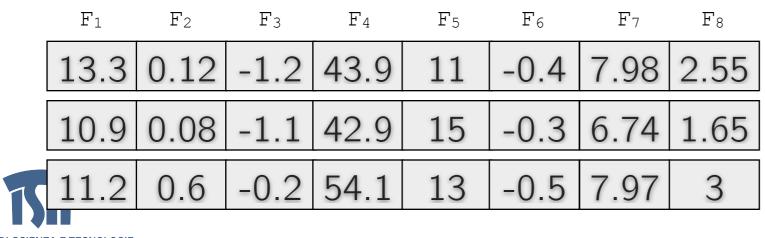


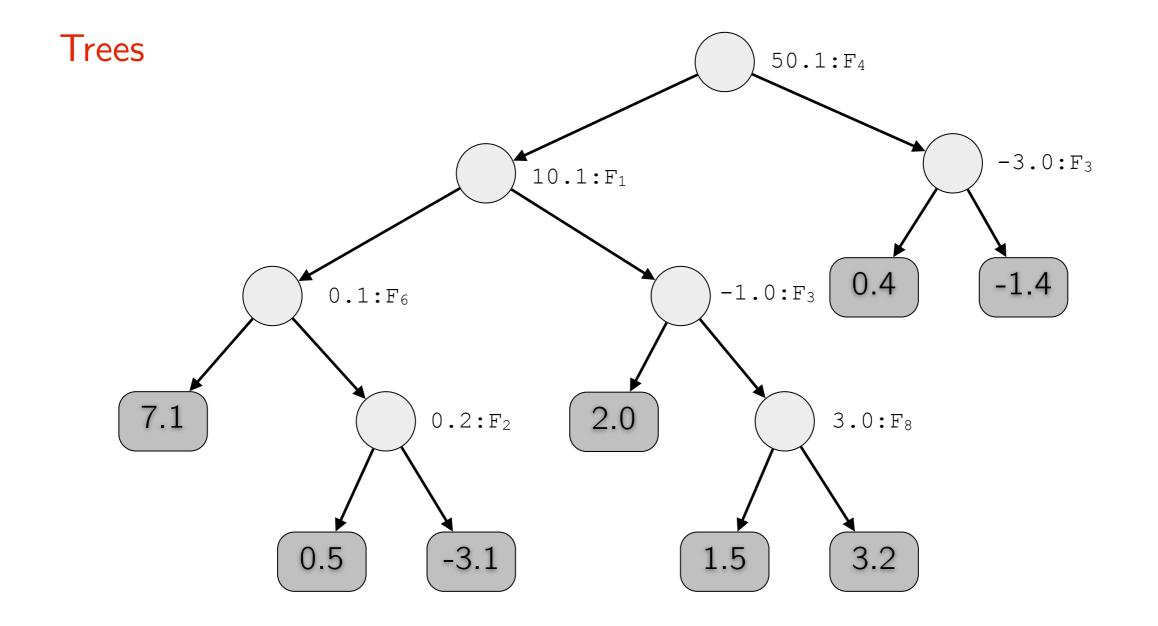


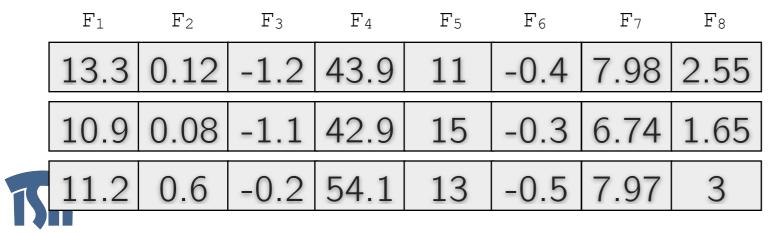


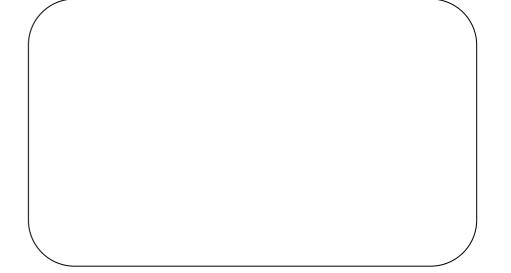


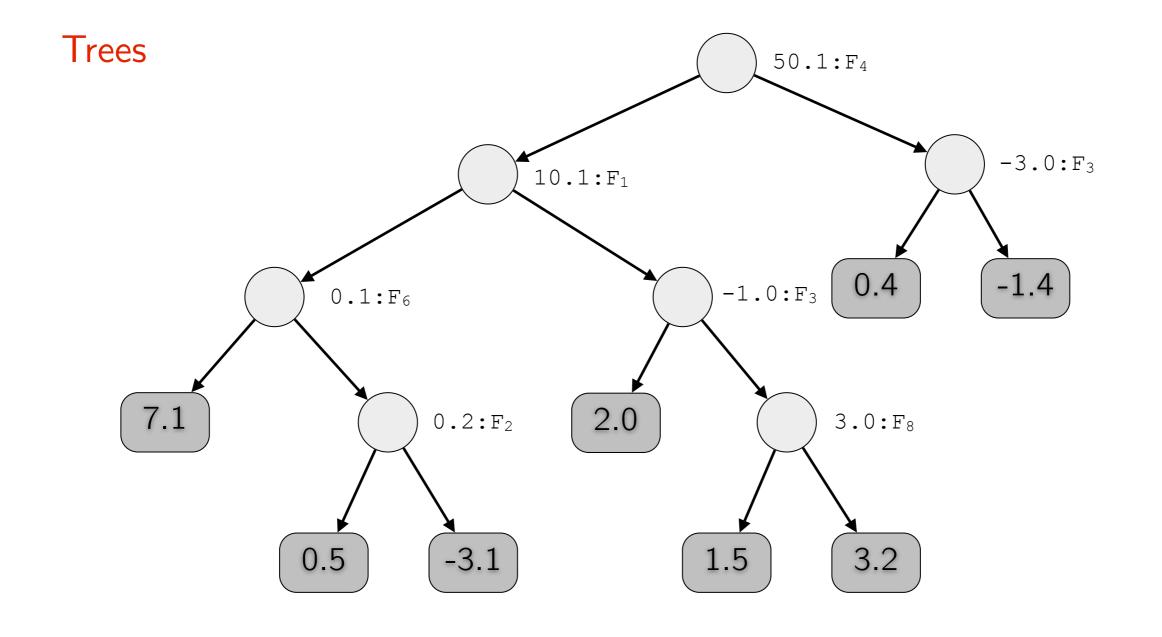


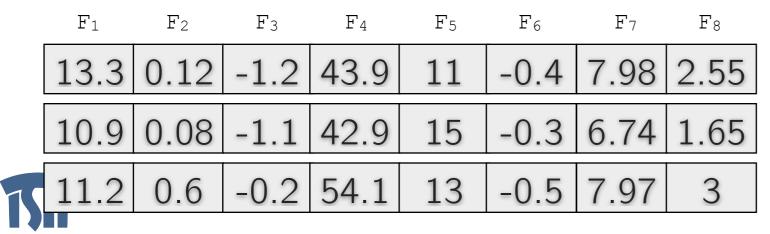




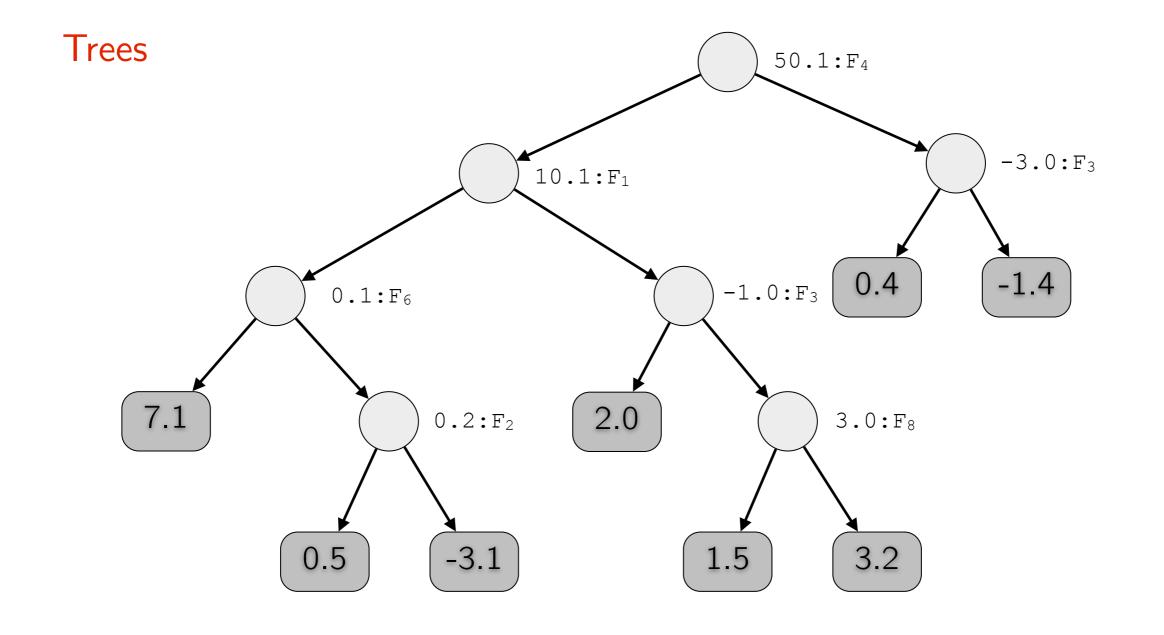


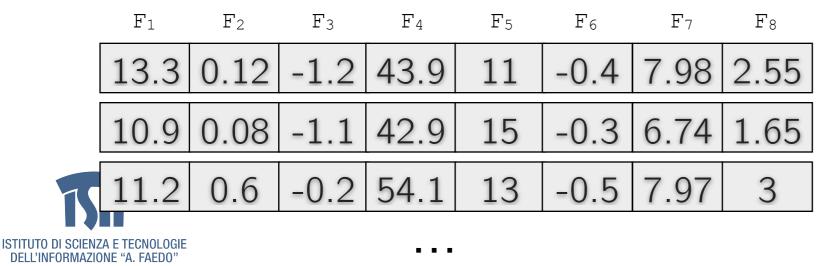


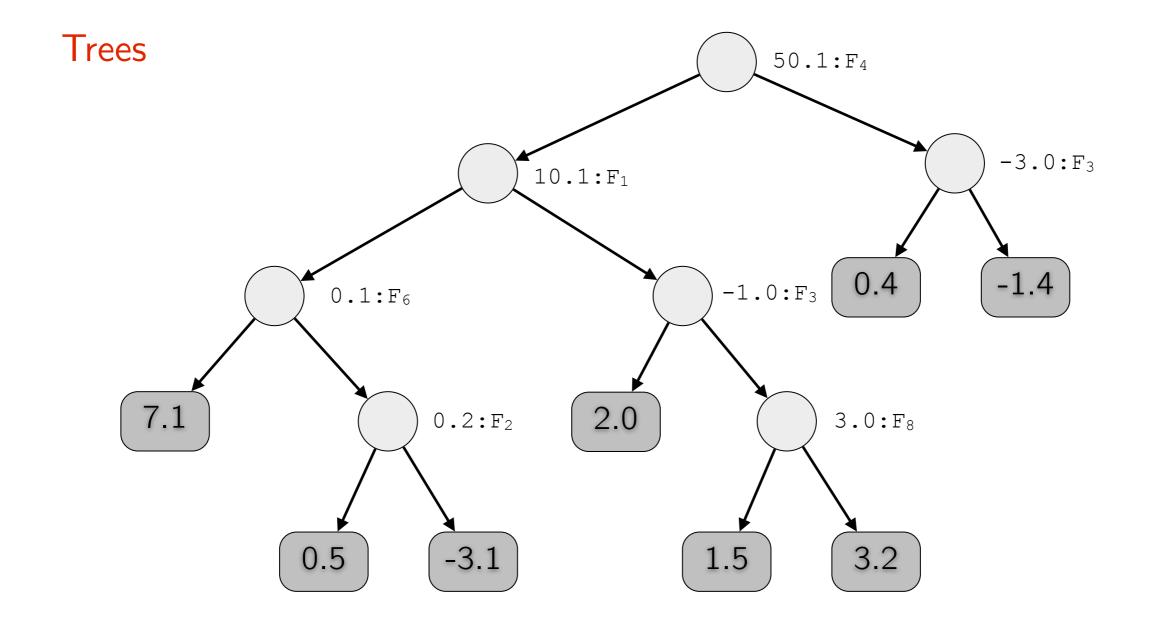


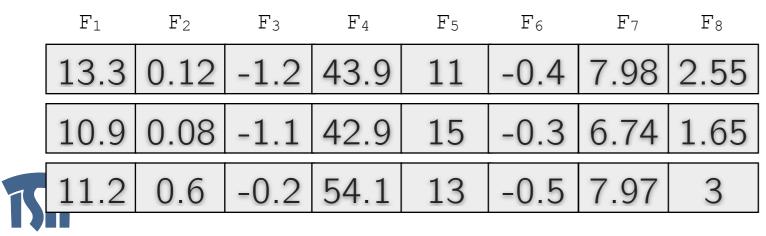


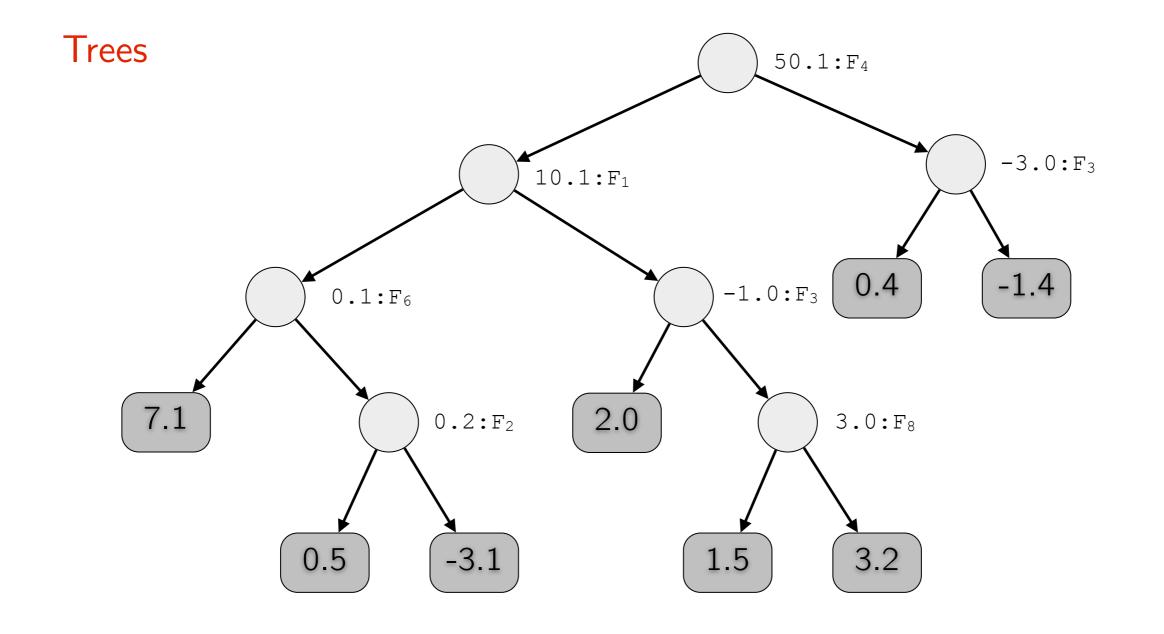
$$\# \text{ docs} = >100 \text{K}$$

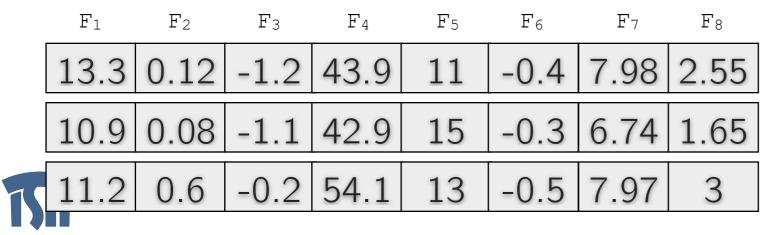


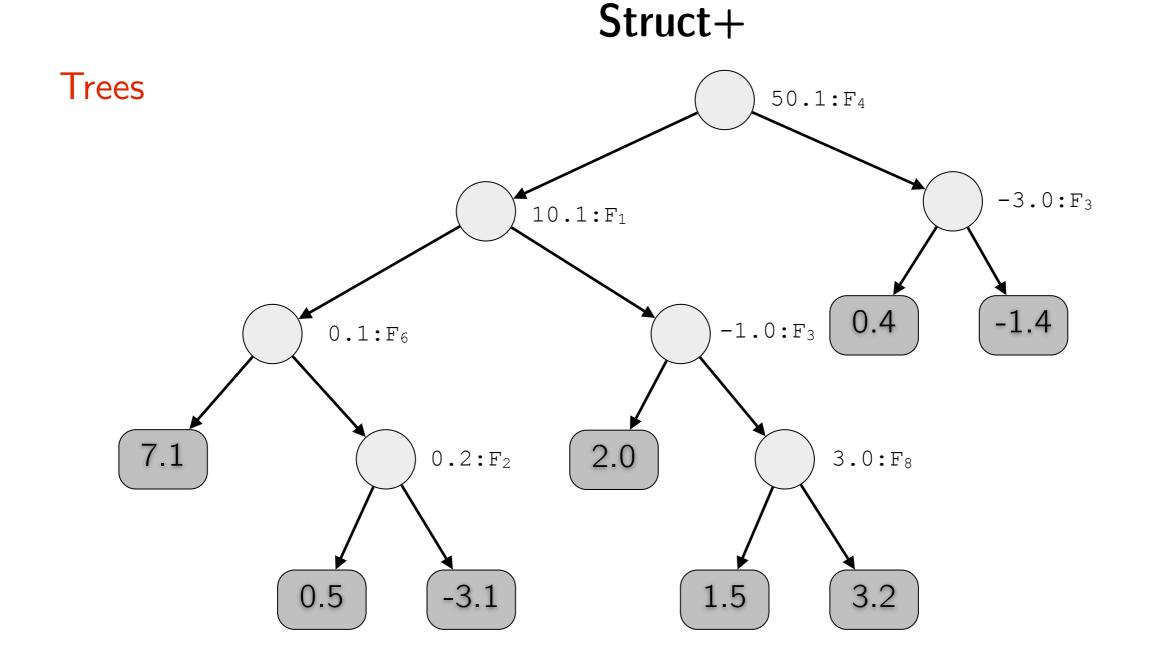


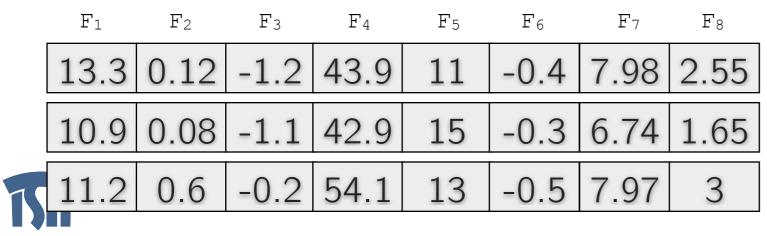


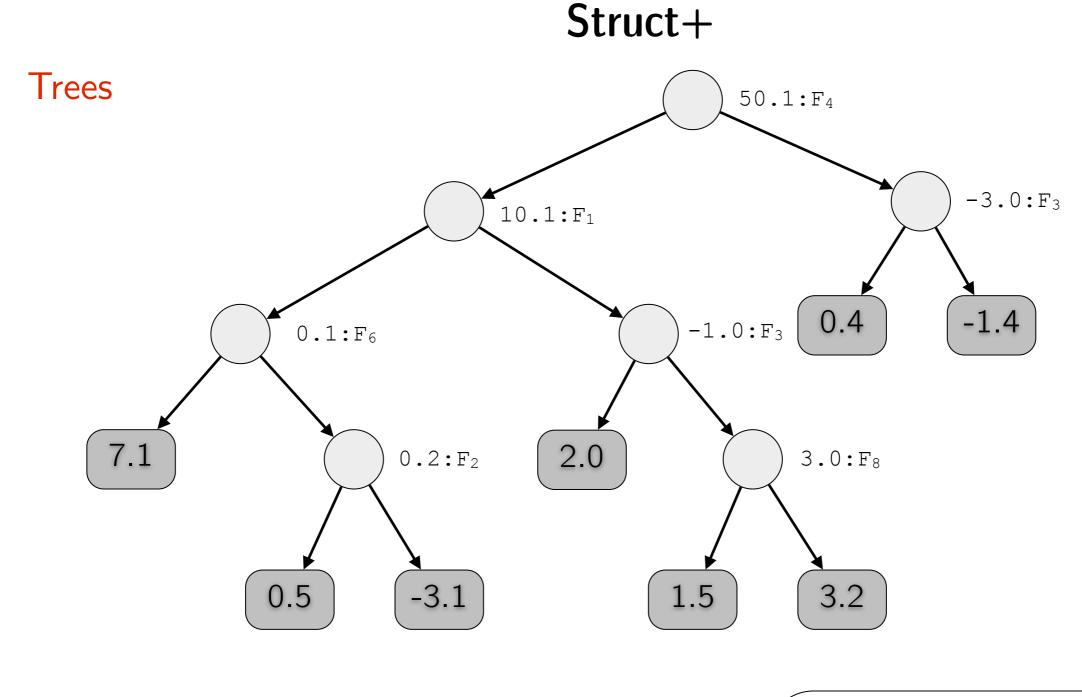


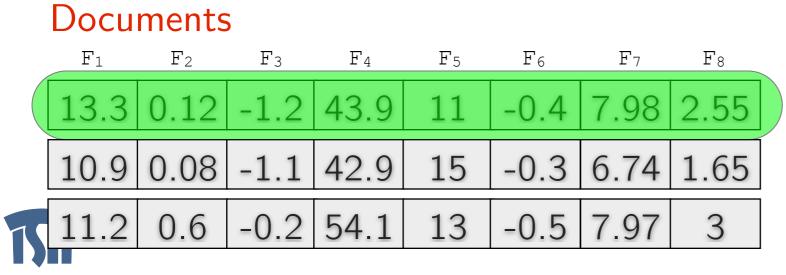


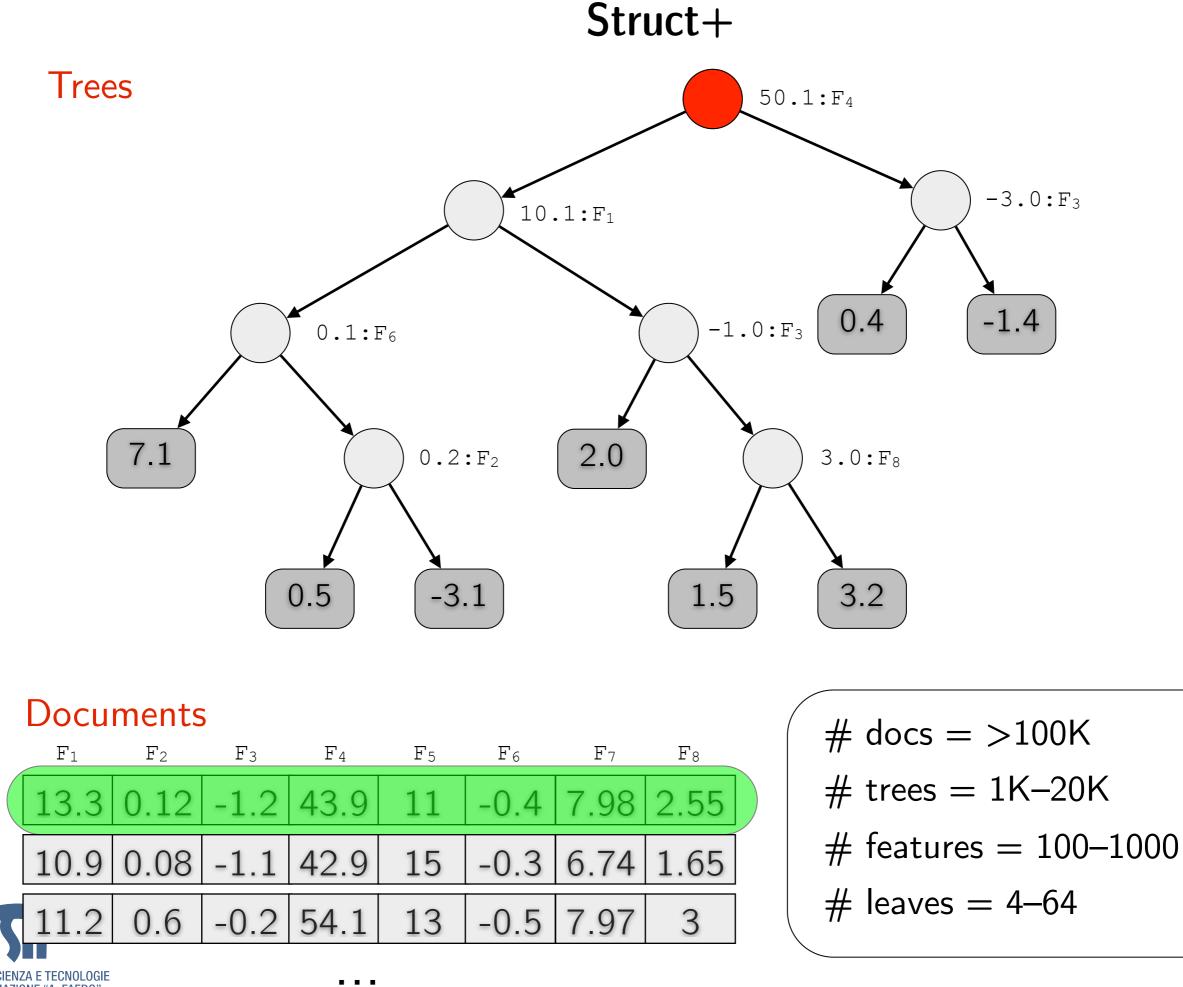


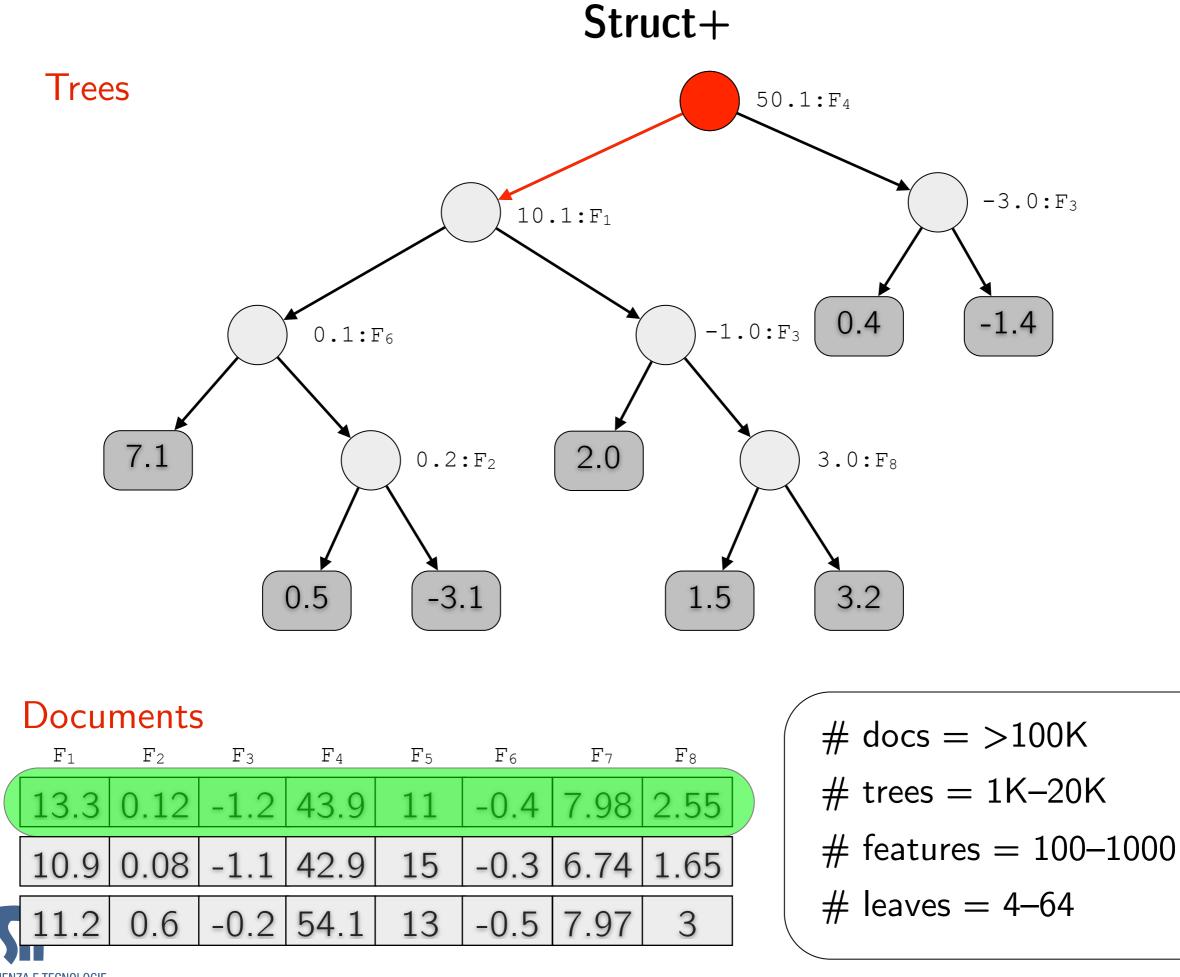


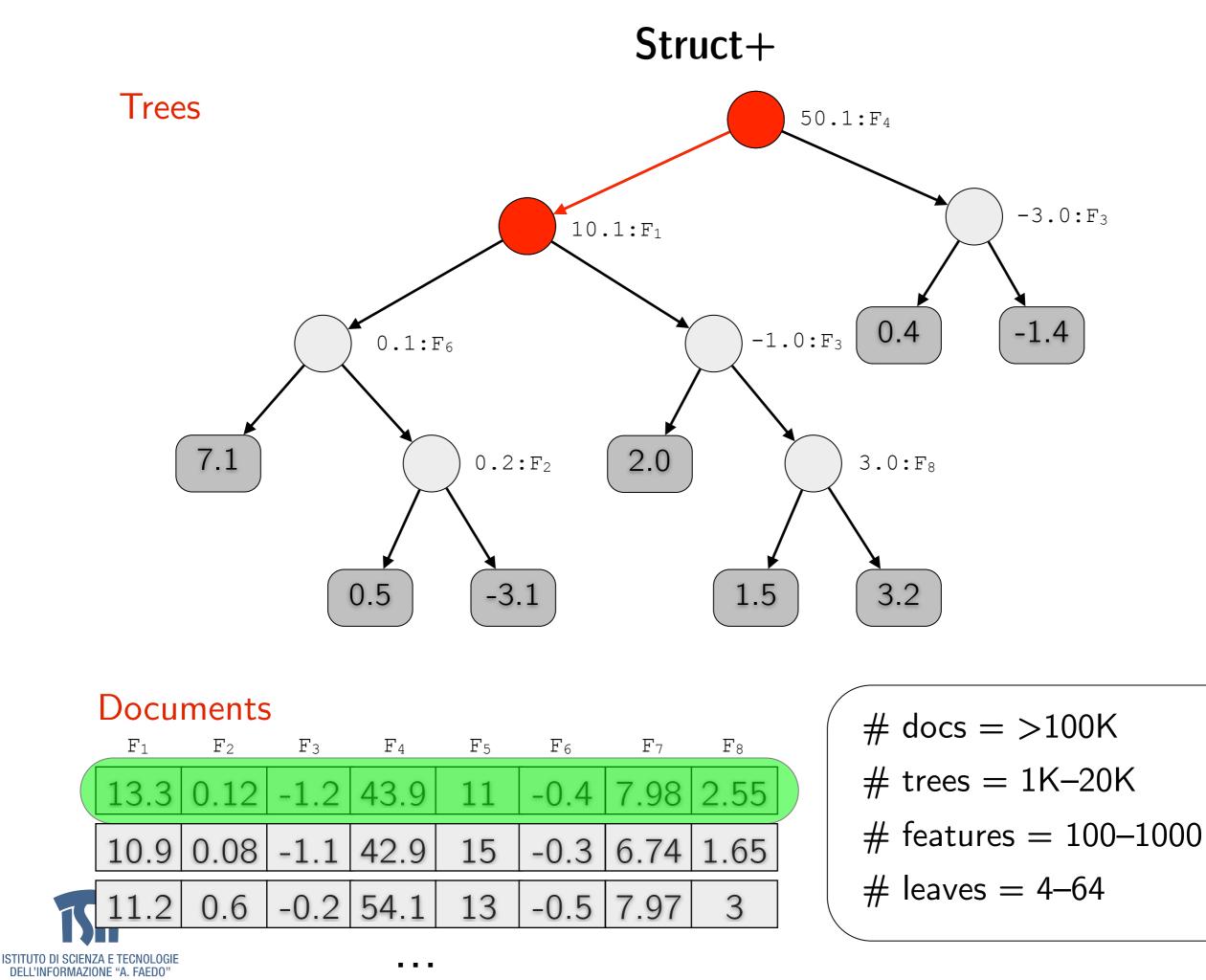


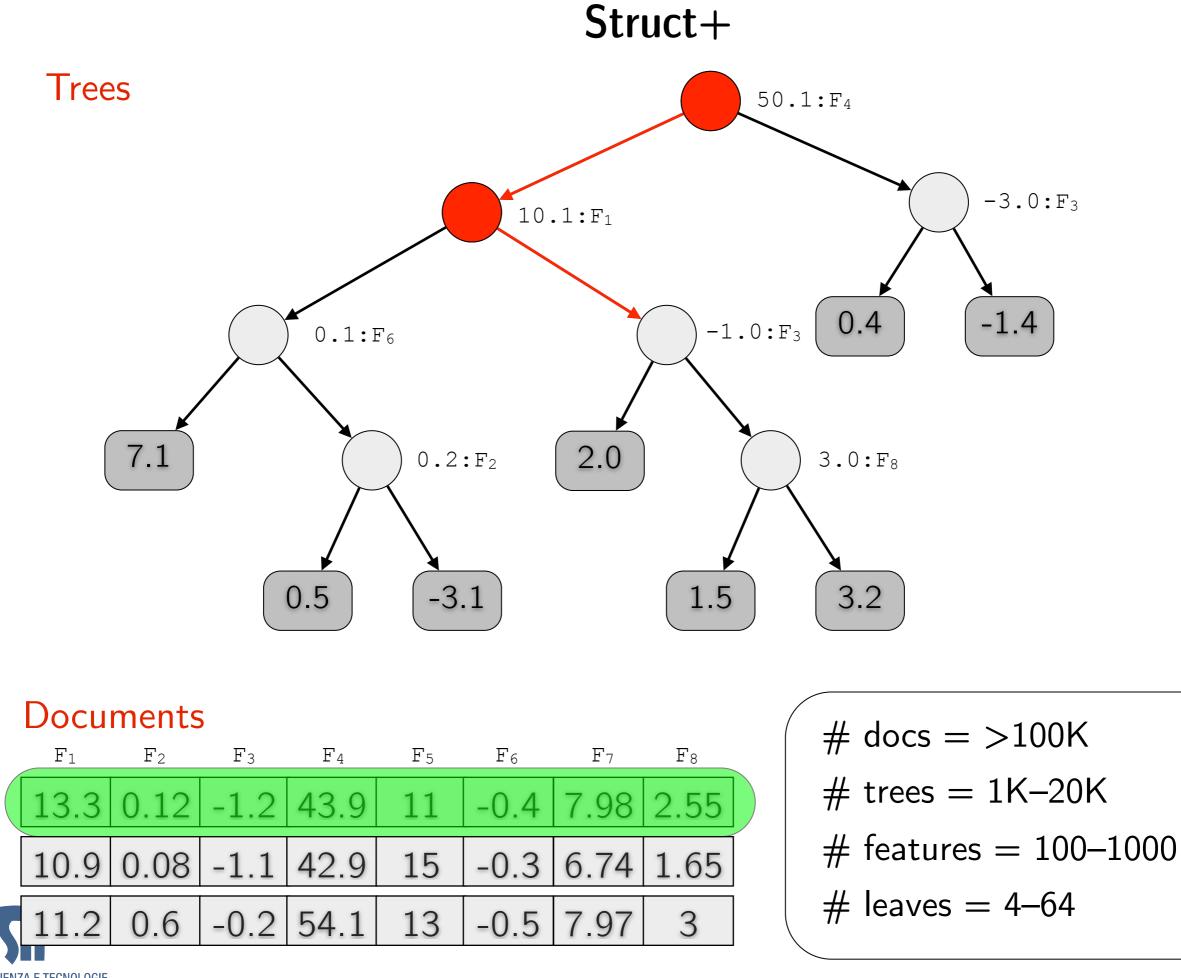




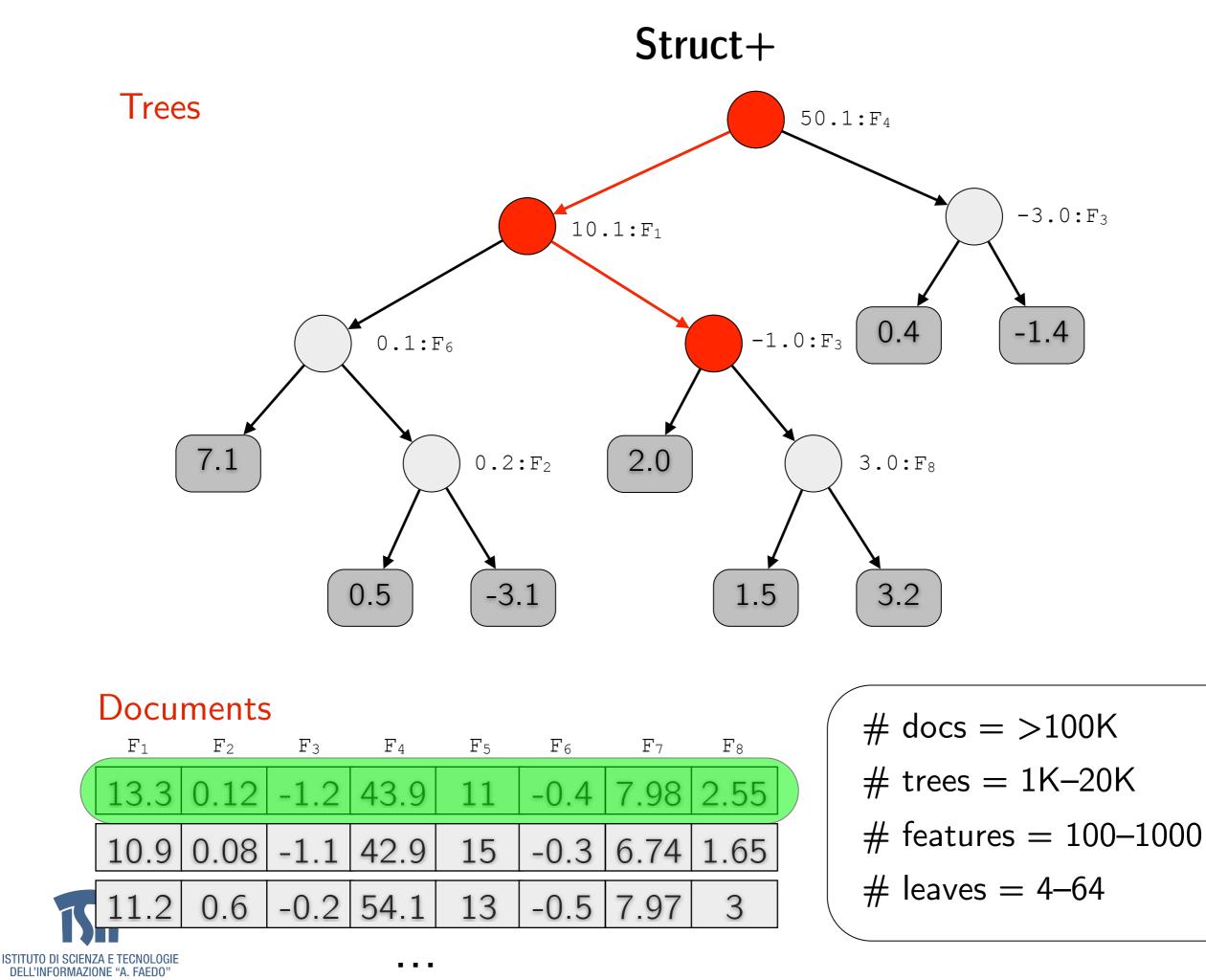


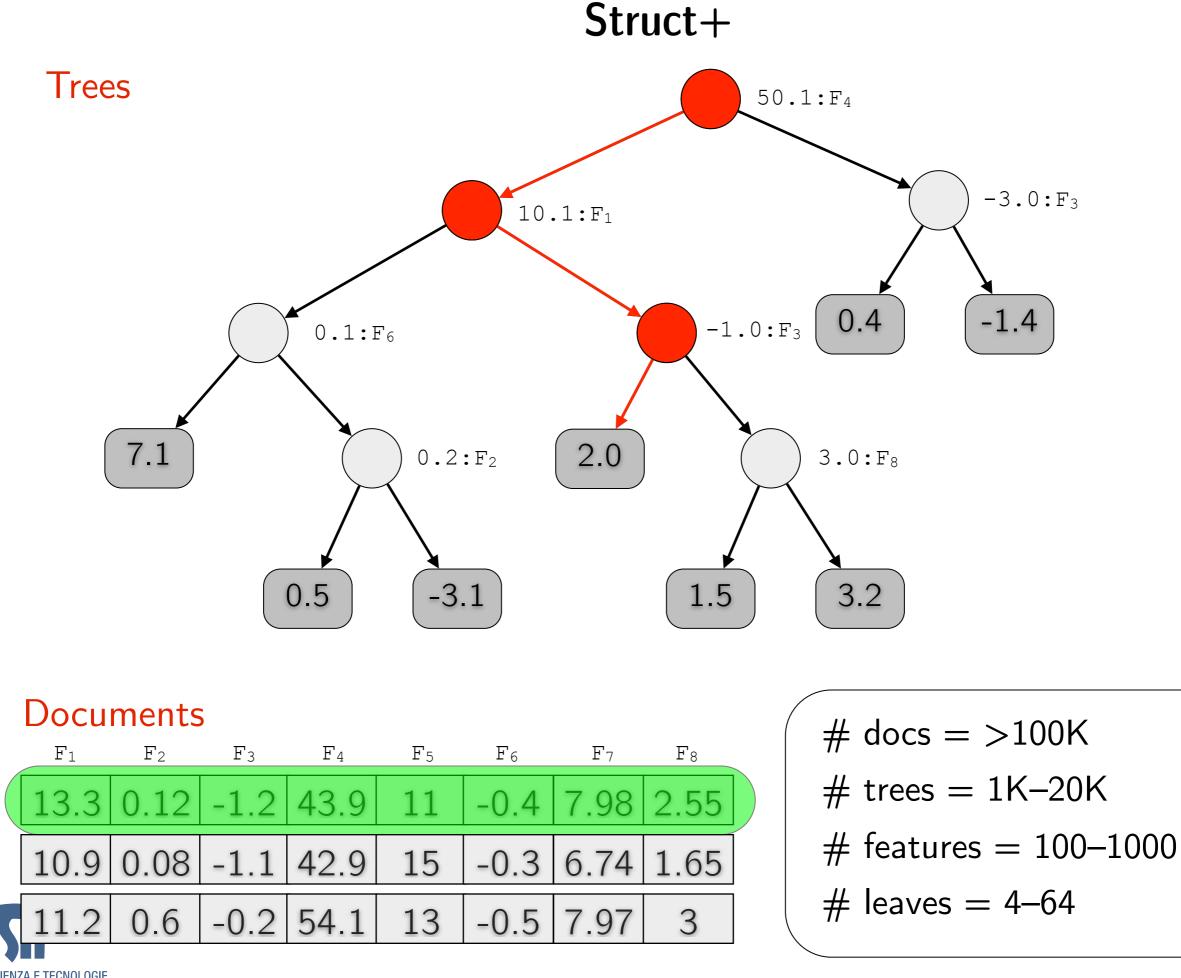




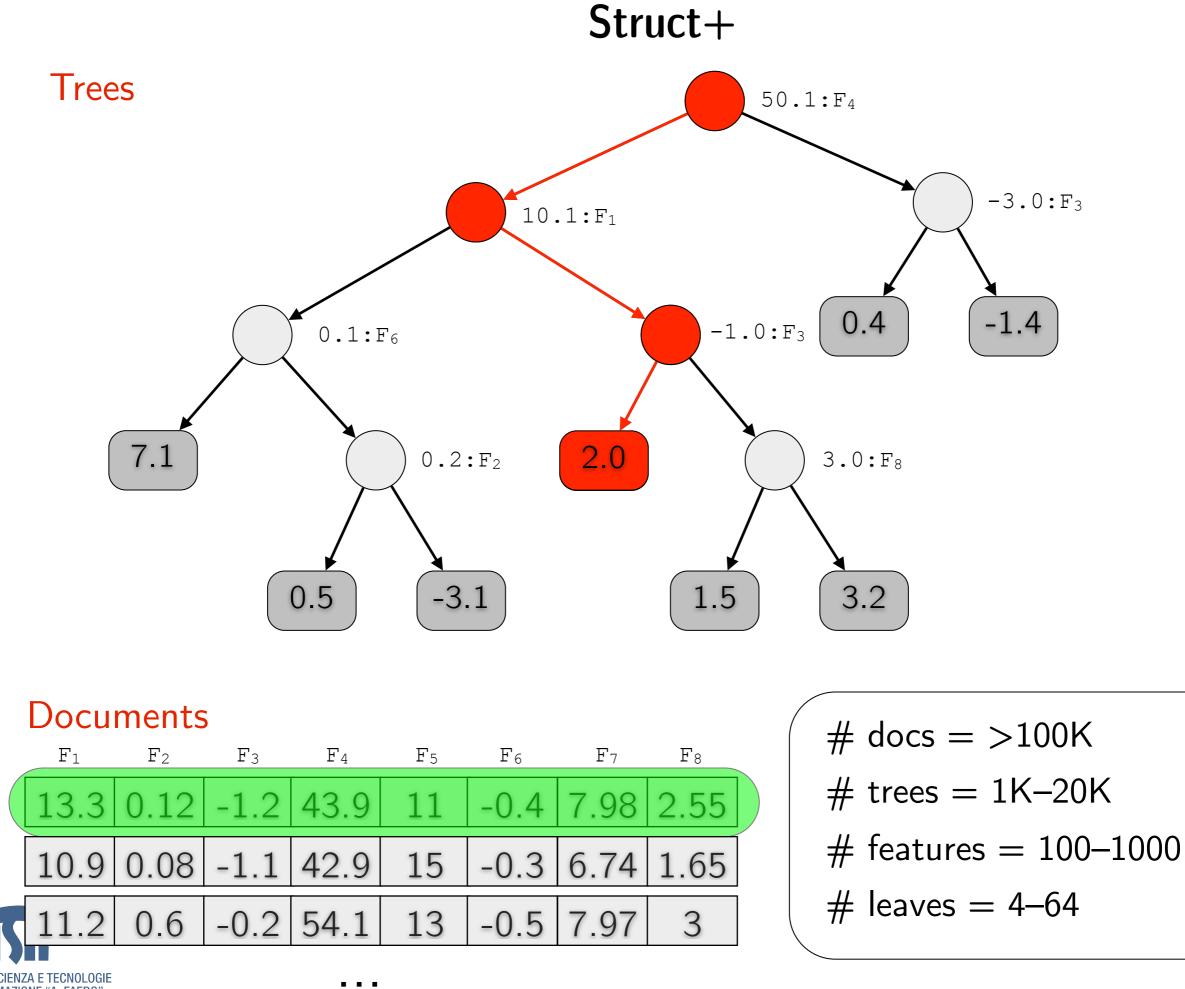


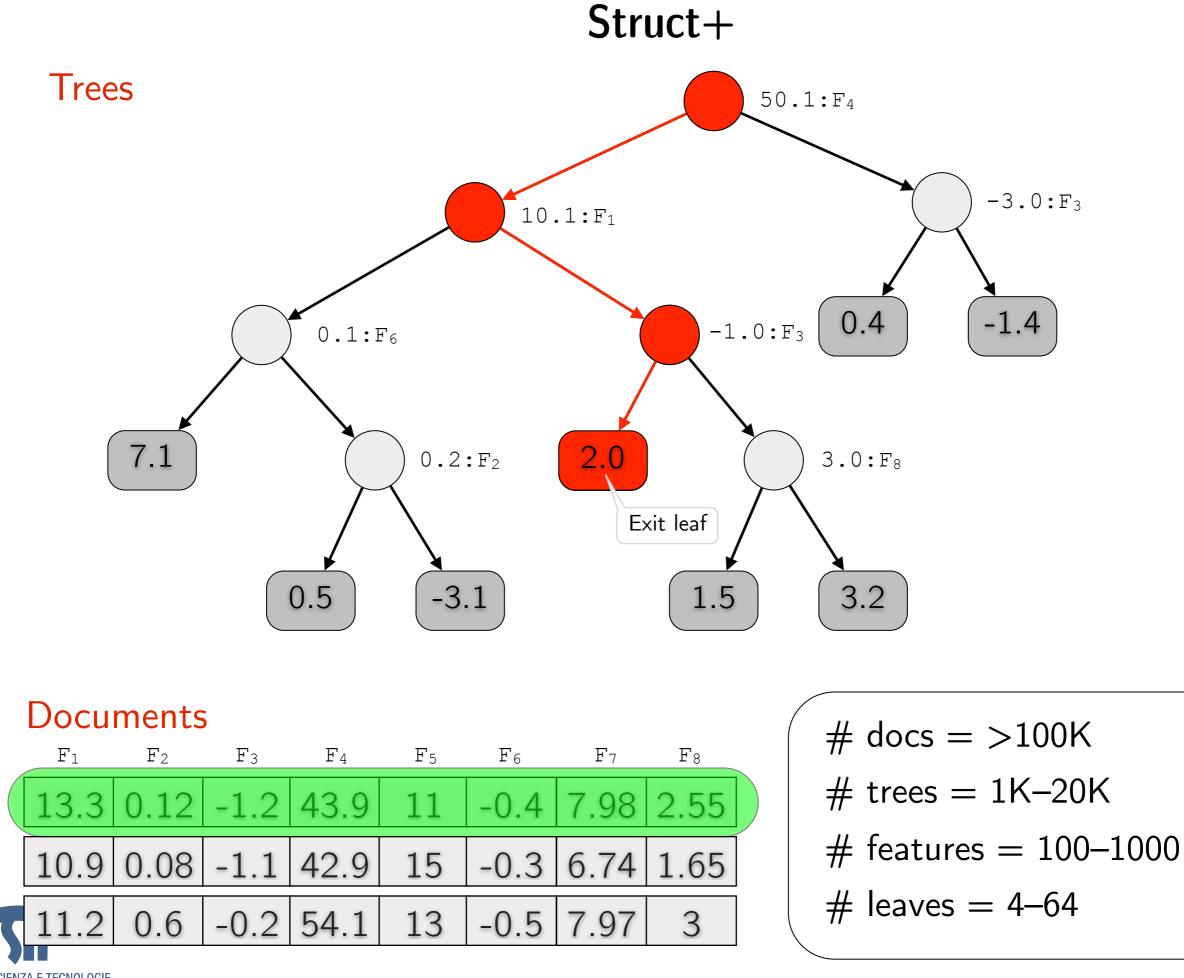
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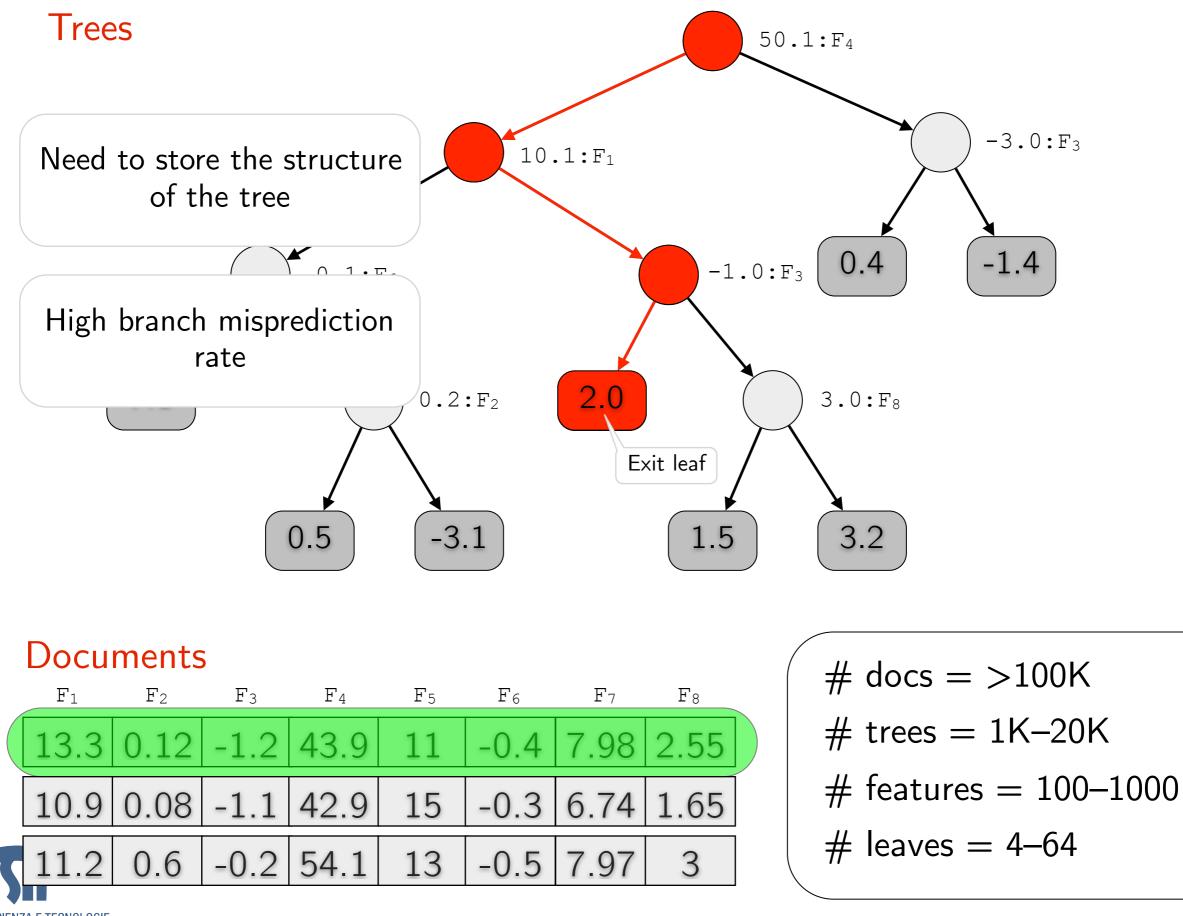




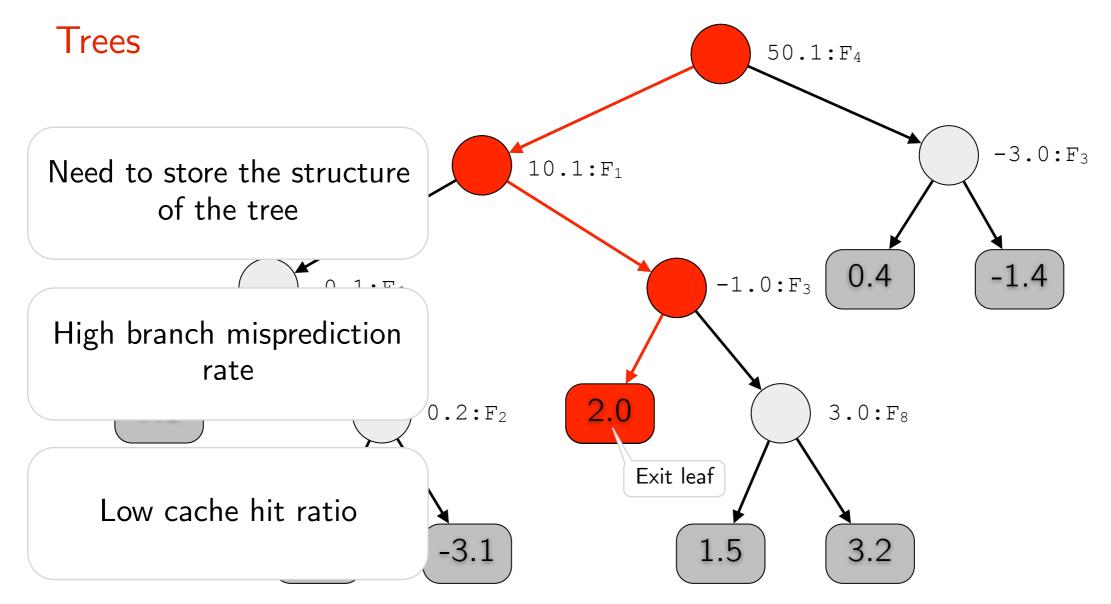
Struct+ Trees 50.1:F₄ -3.0:F₃ 10.1:F₁ Need to store the structure of the tree 0.4 -1.4 -1.0:F₃ 0.1:F₆ 7.12.0 $0.2:F_{2}$ 3.0:F₈ Exit leaf -3.1 0.5 3.2 1.5

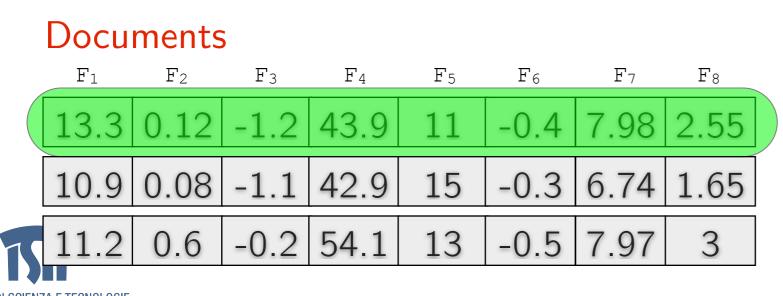
Documents \mathbb{F}_2 ${ m F}_3$ \mathbb{F}_4 F_5 ${ m F}_6$ F7 \mathbb{F}_8 F_1 13.3 0.12 -1.2 43.9 11 -0.4 7.98 2.55 -1.1 10.9 0.08 42.9 15 -0.3 1.65 6.74 0.6 54.1 13 3 1.2 -0.2 7.97 -0.5 . . .

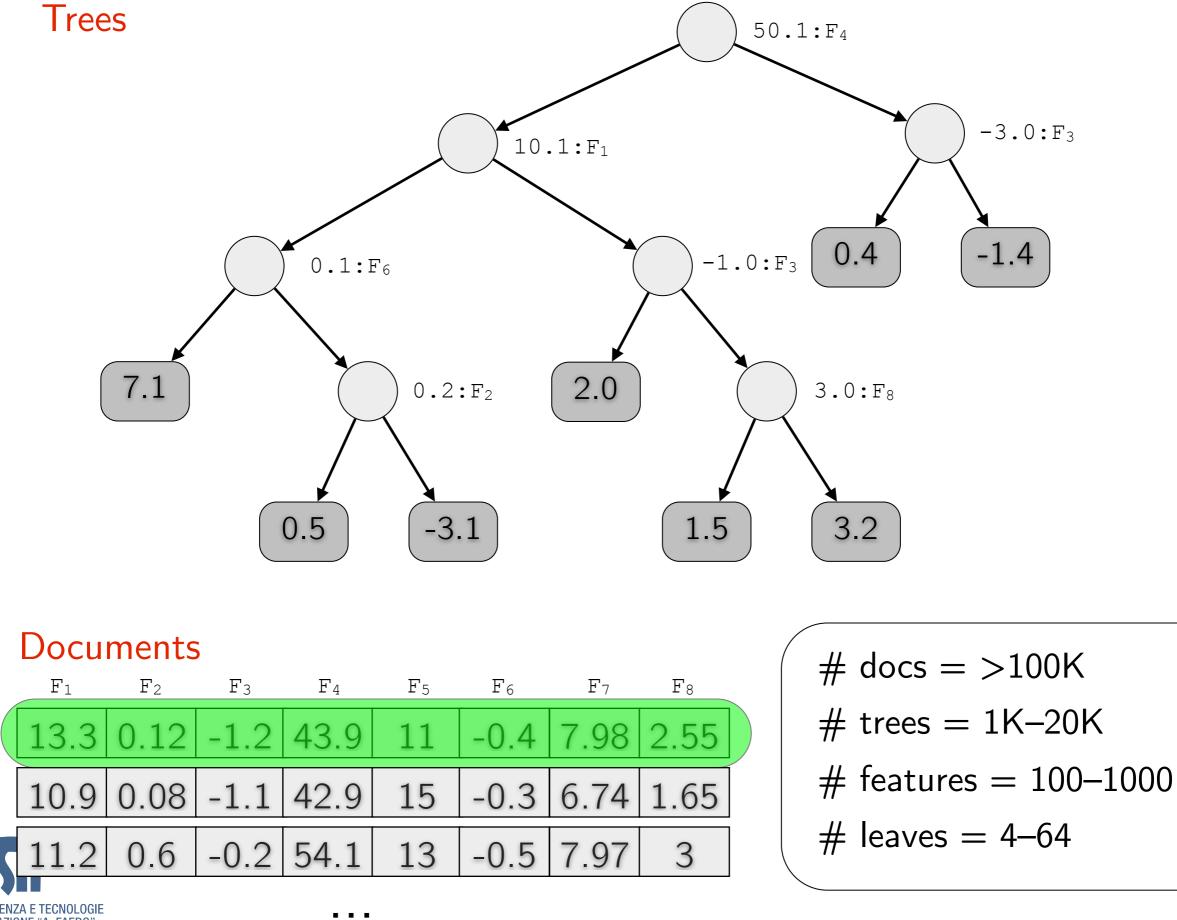
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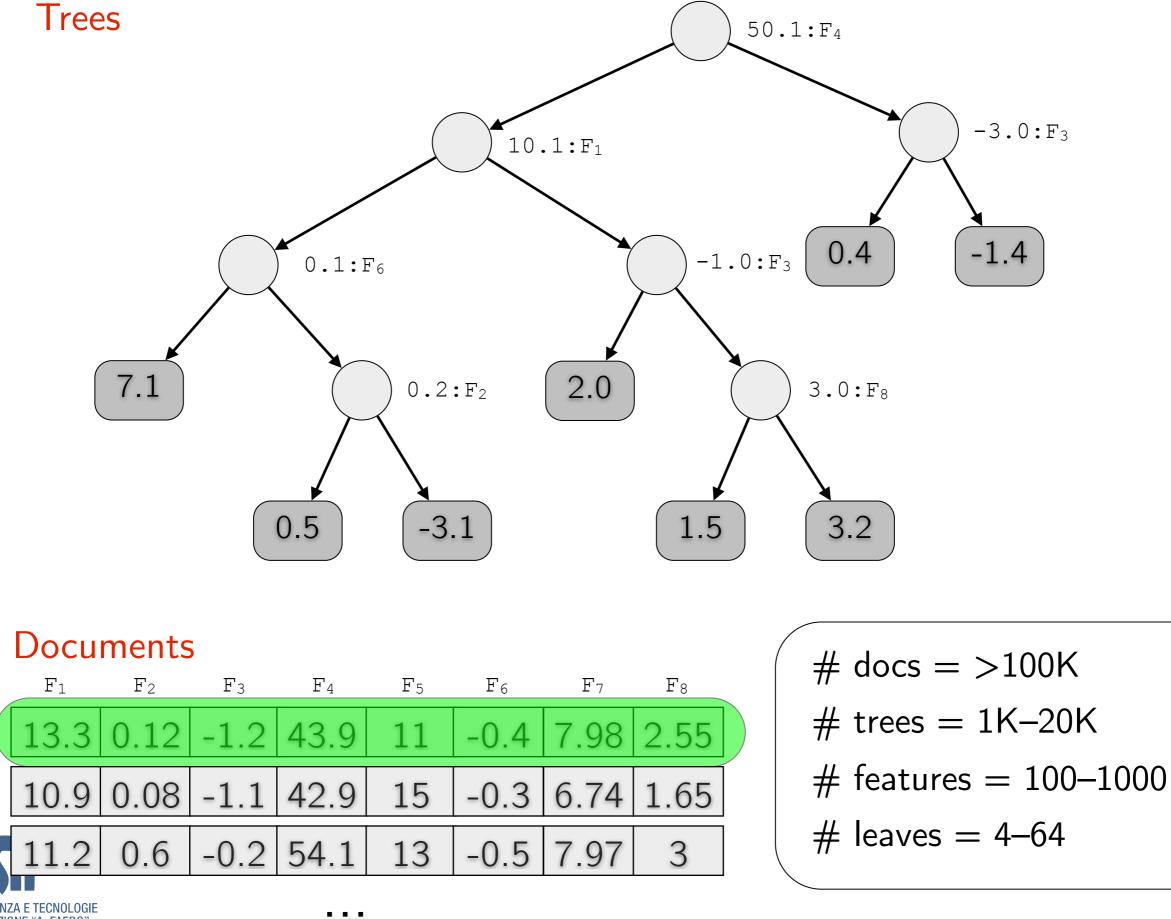
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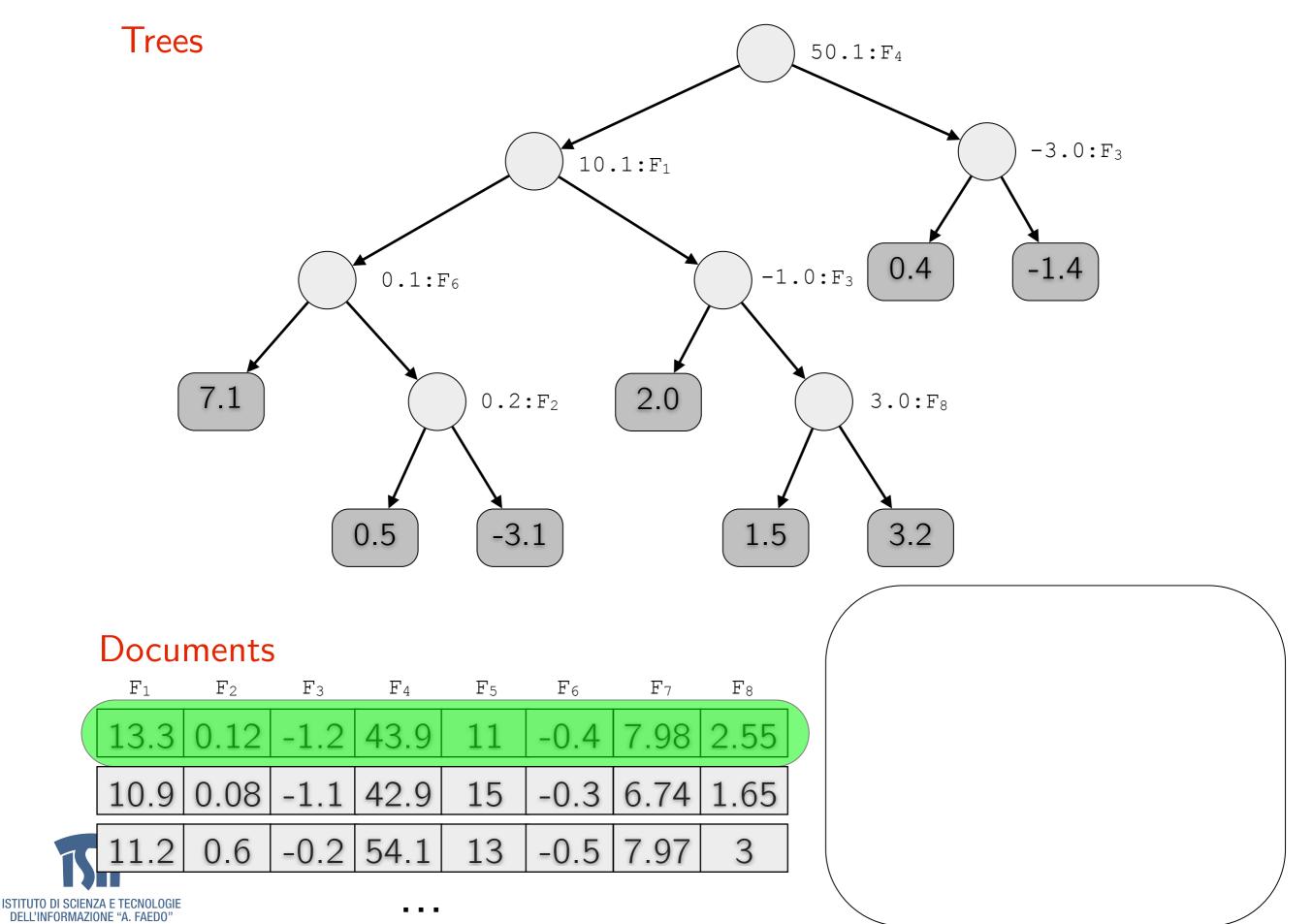


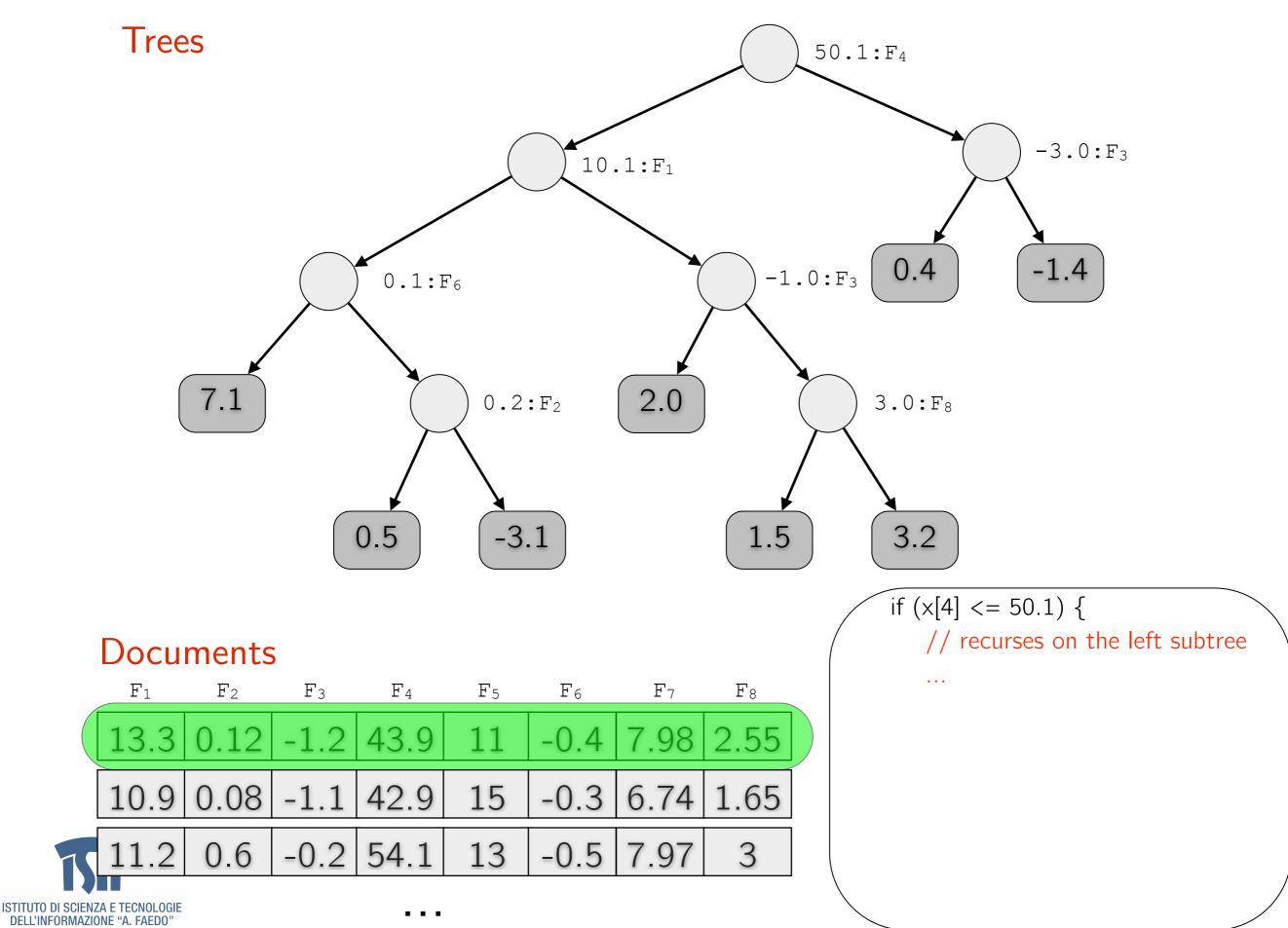


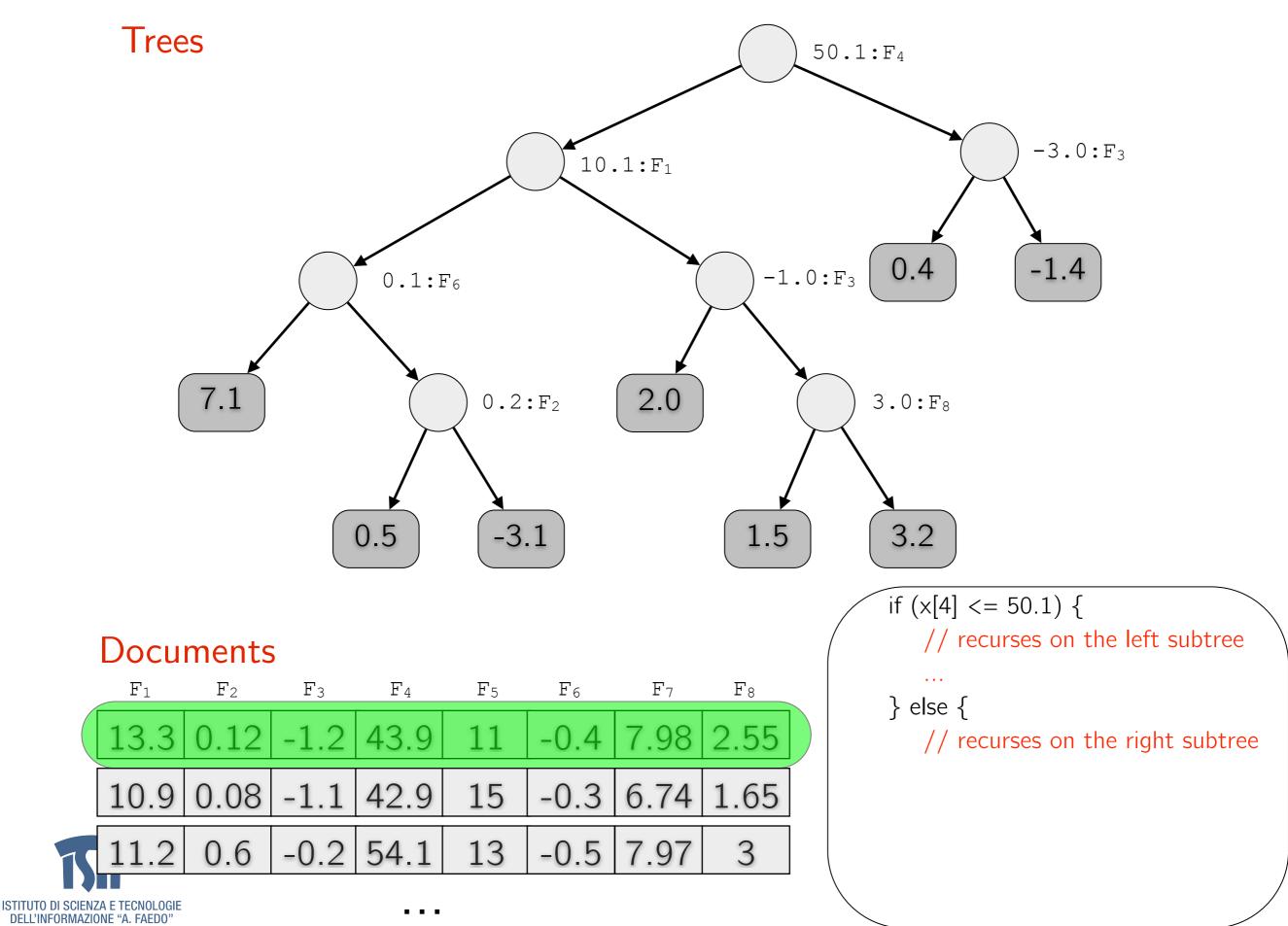


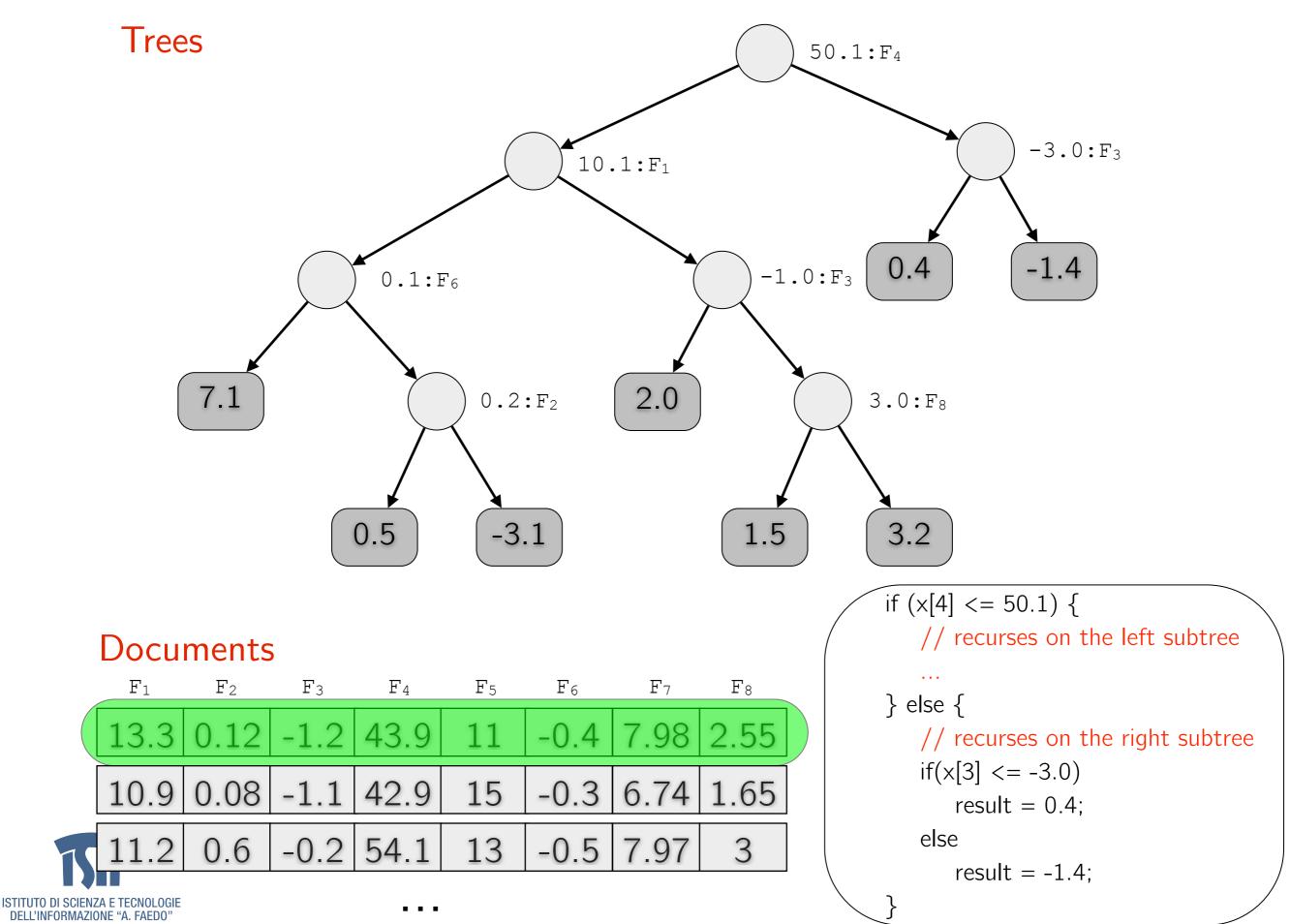
If-then-else

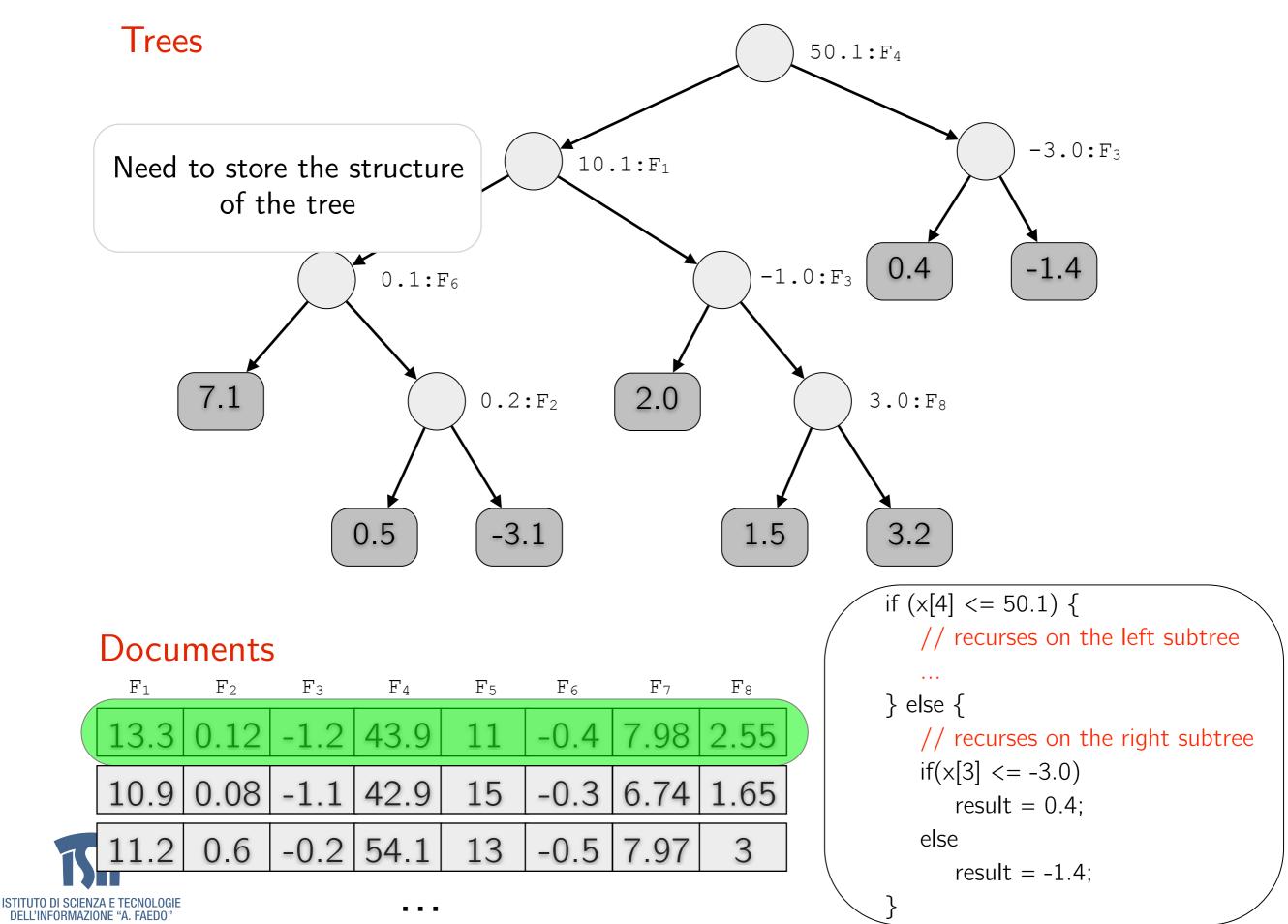


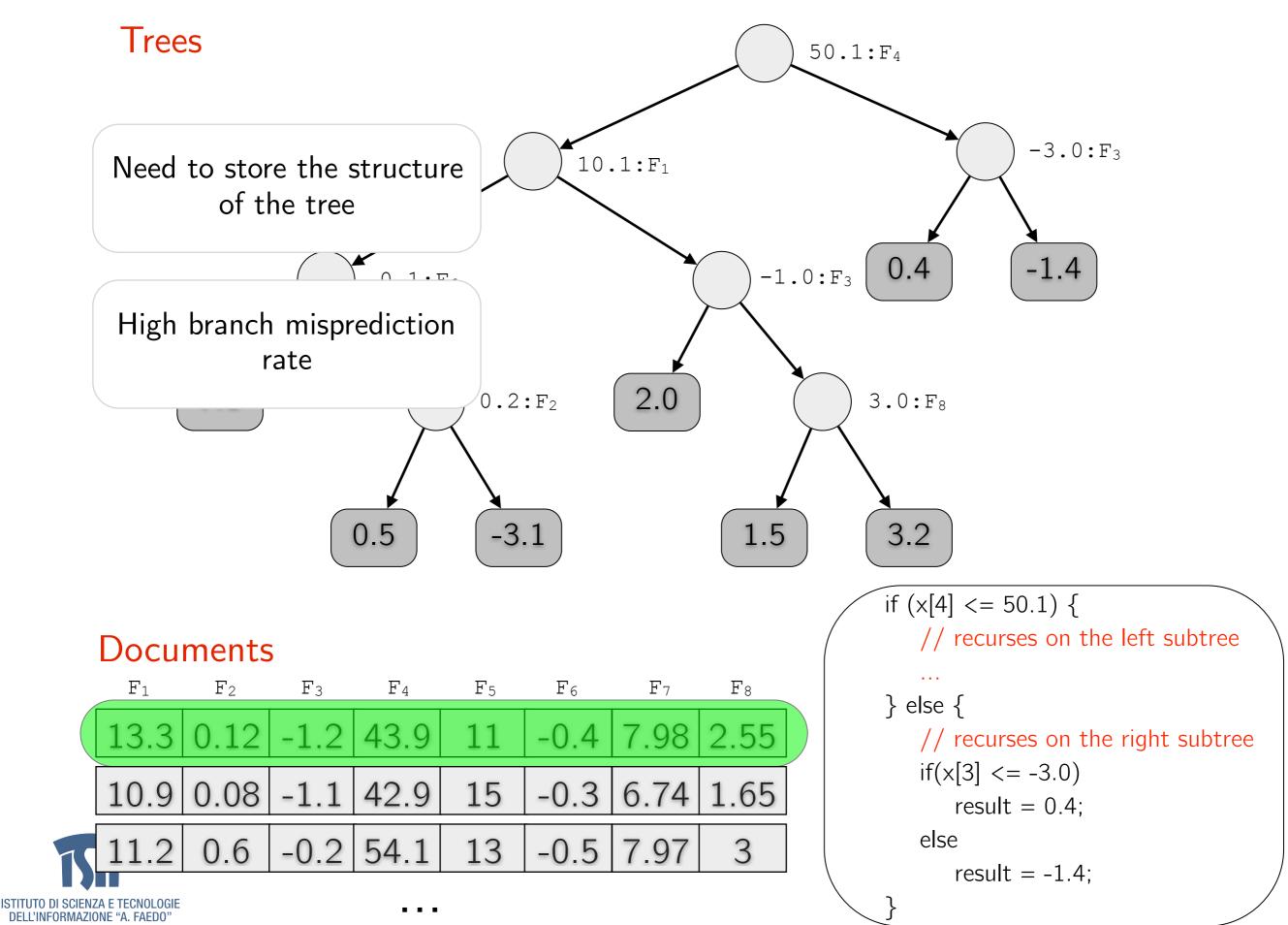


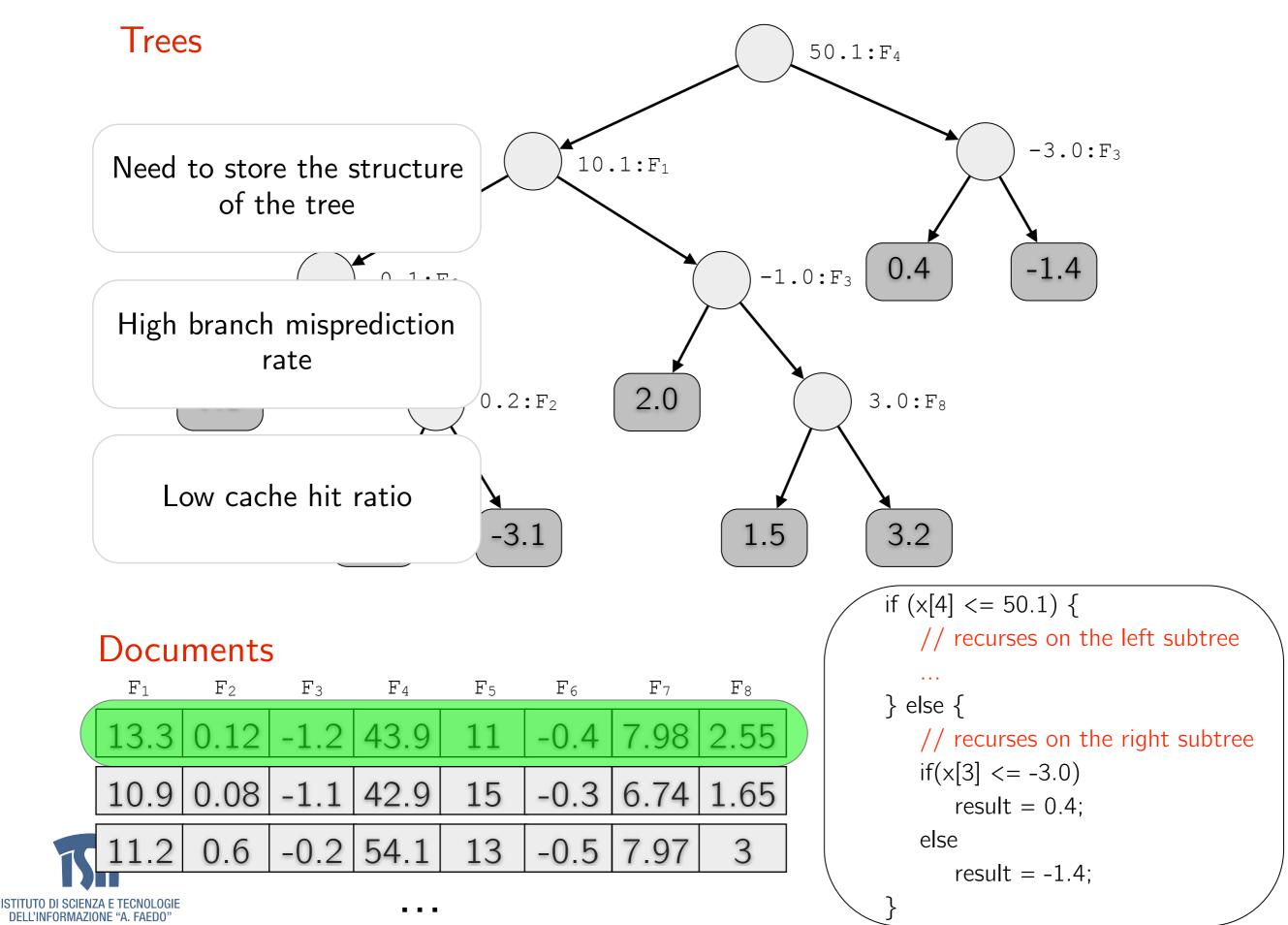


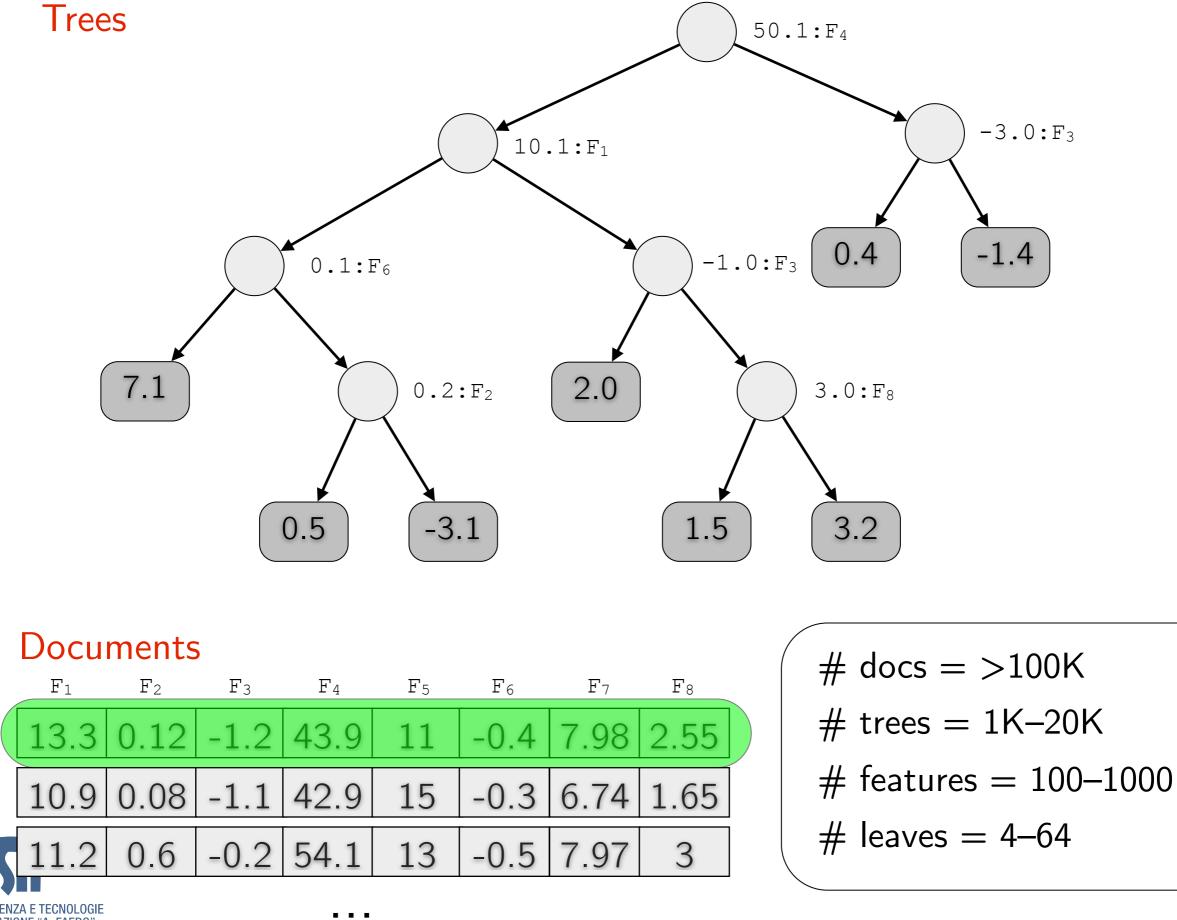


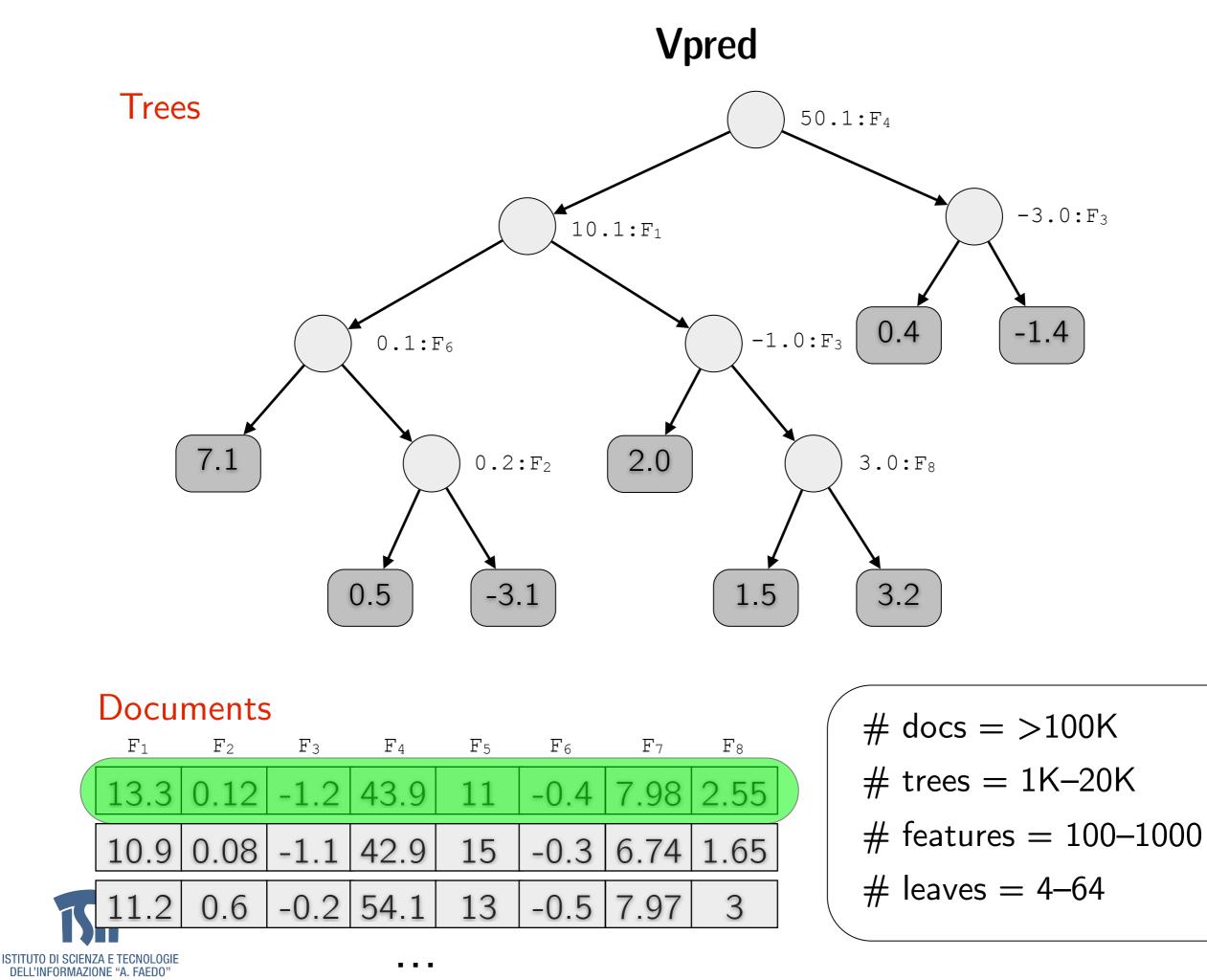


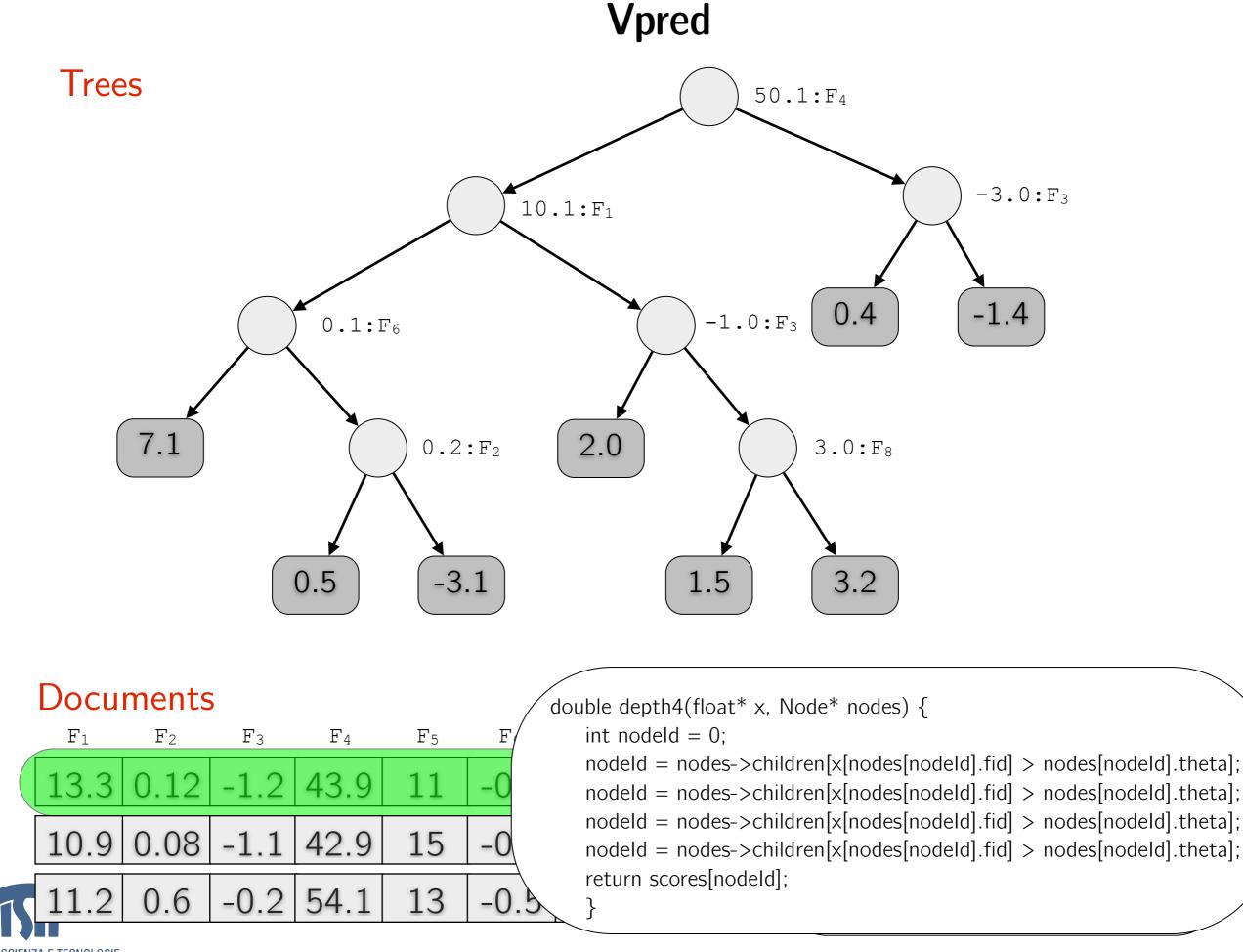


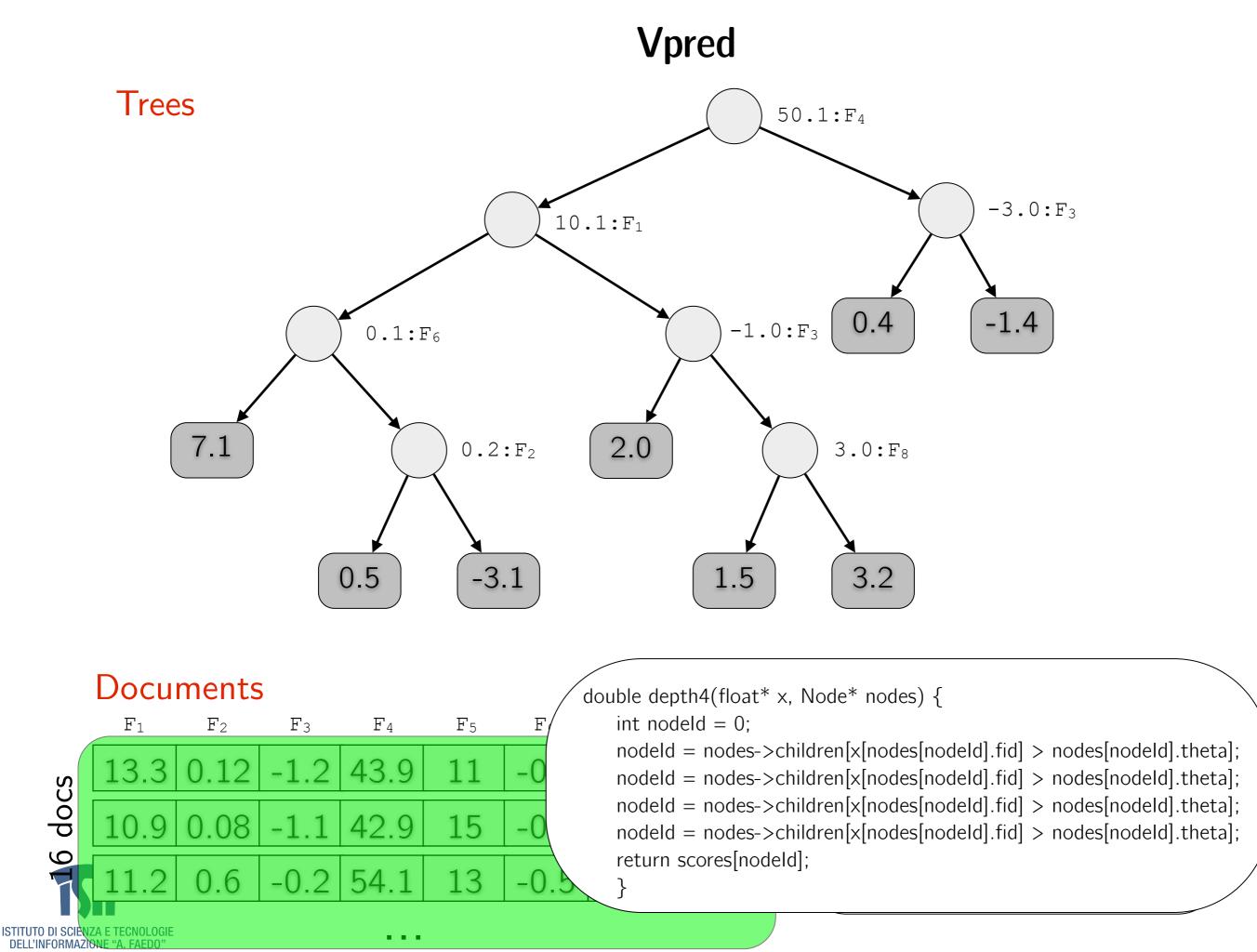


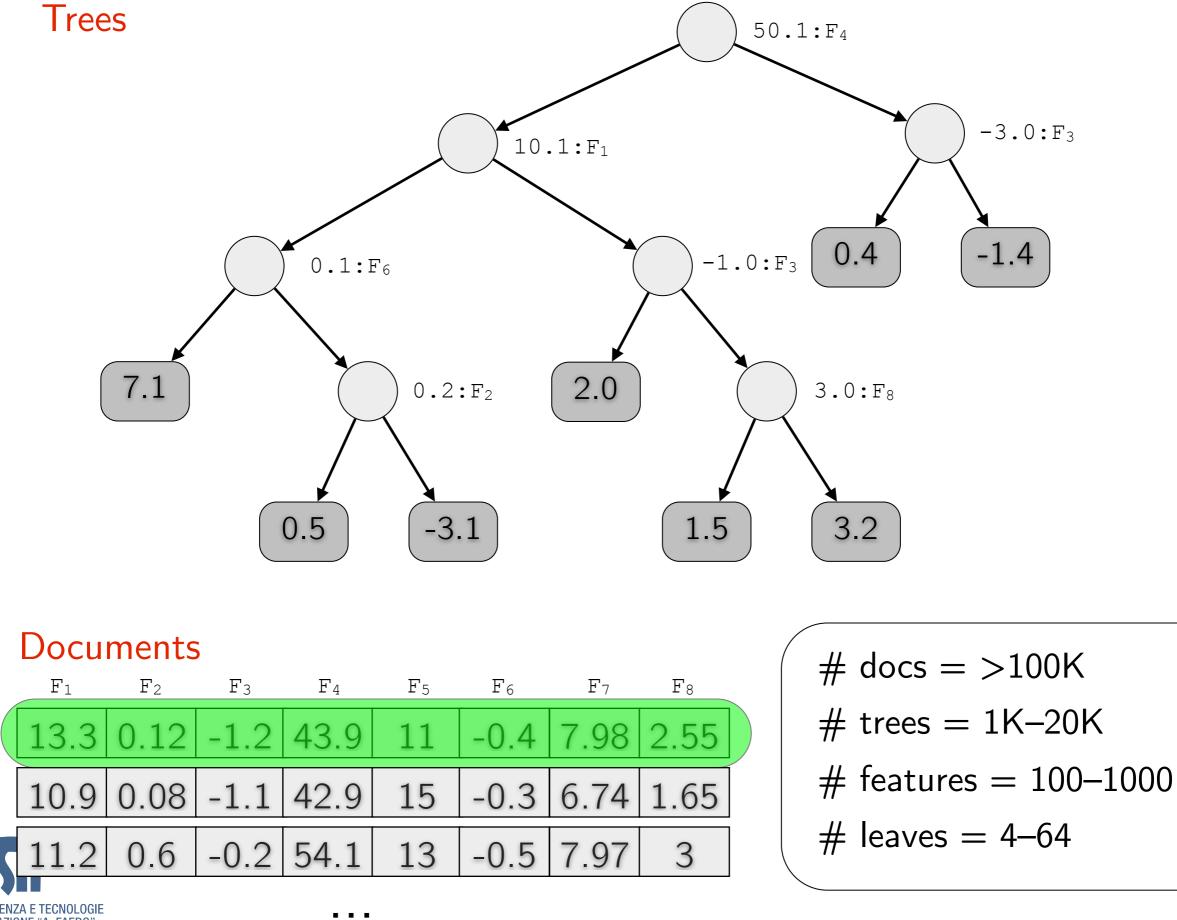


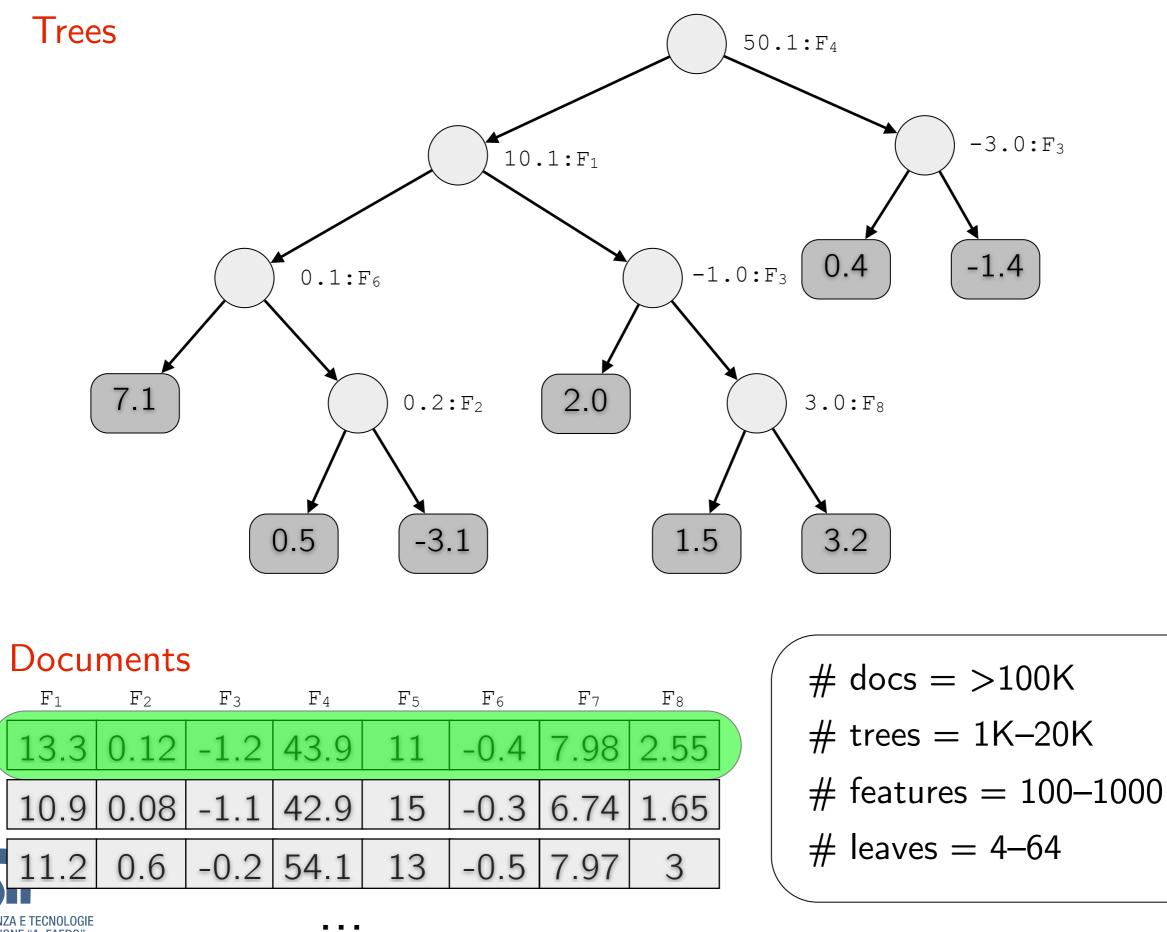


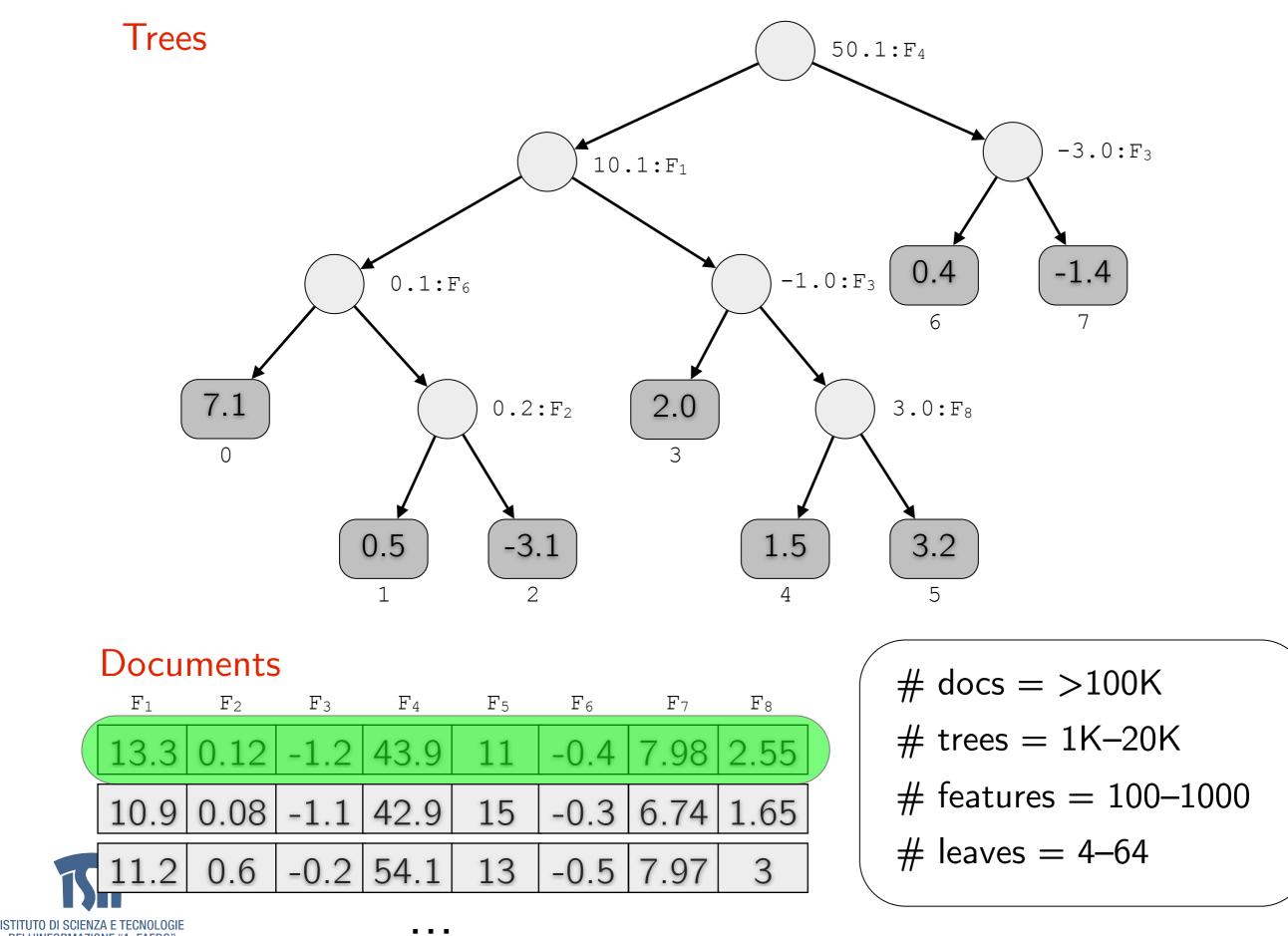


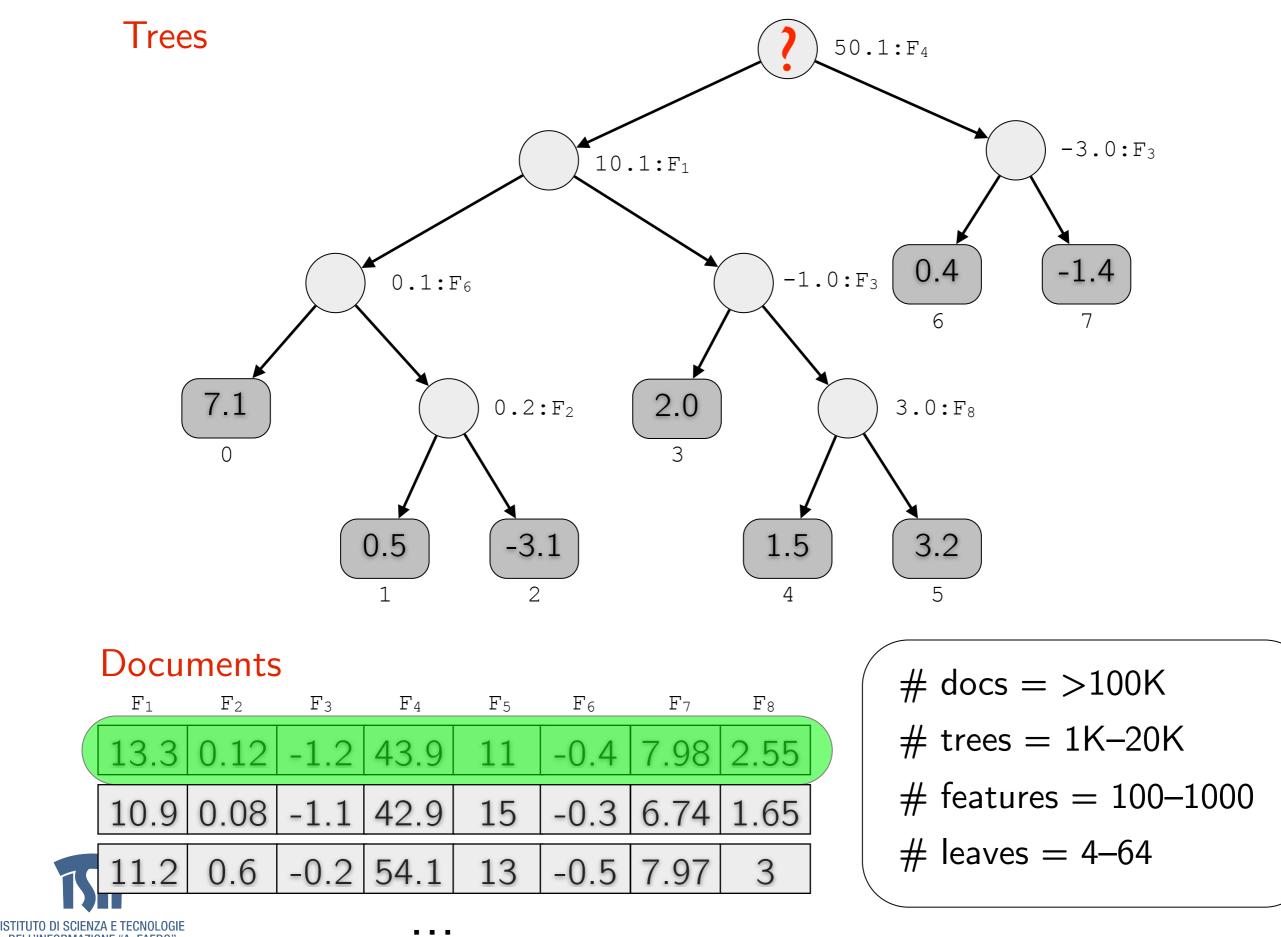


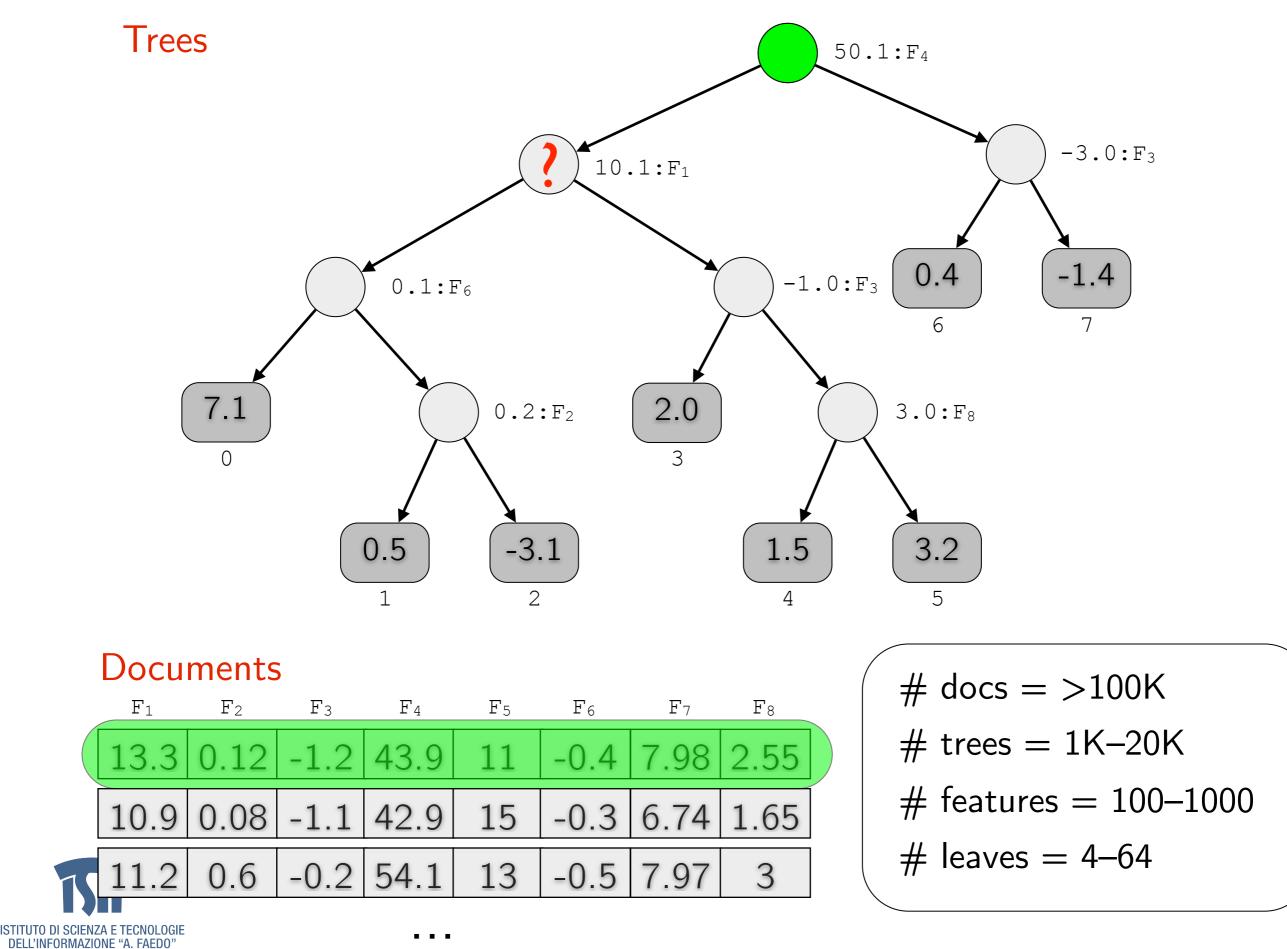


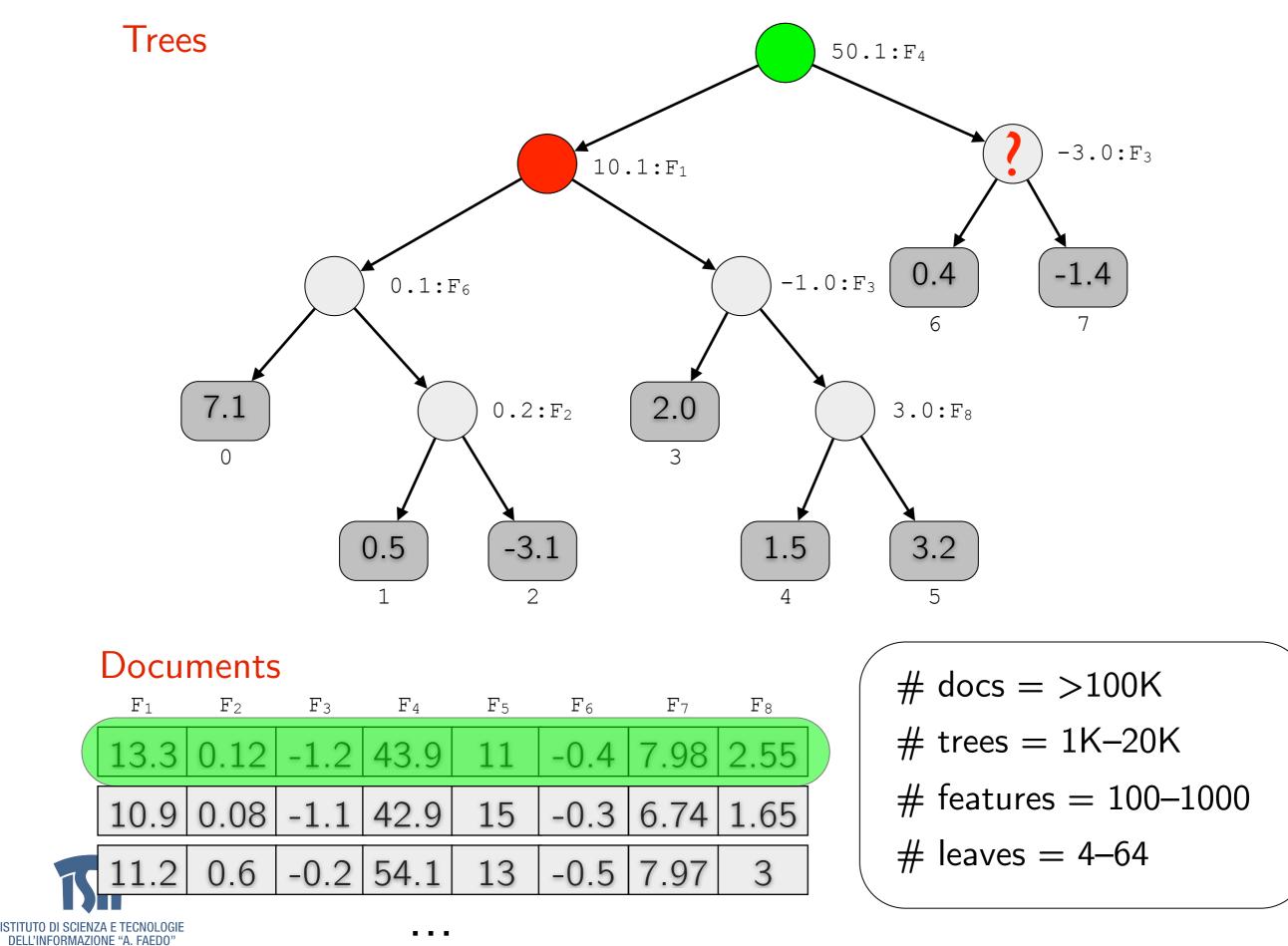


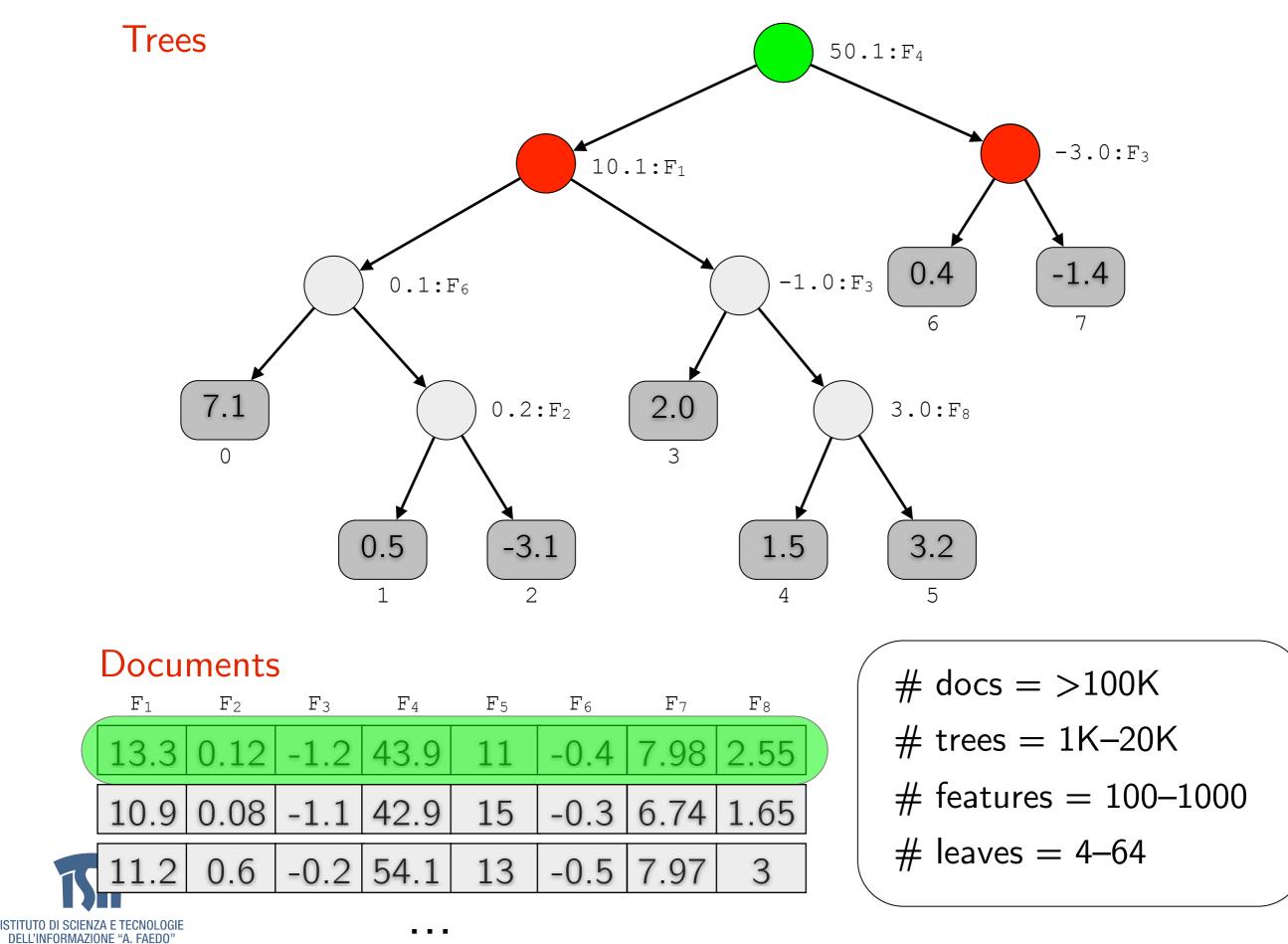


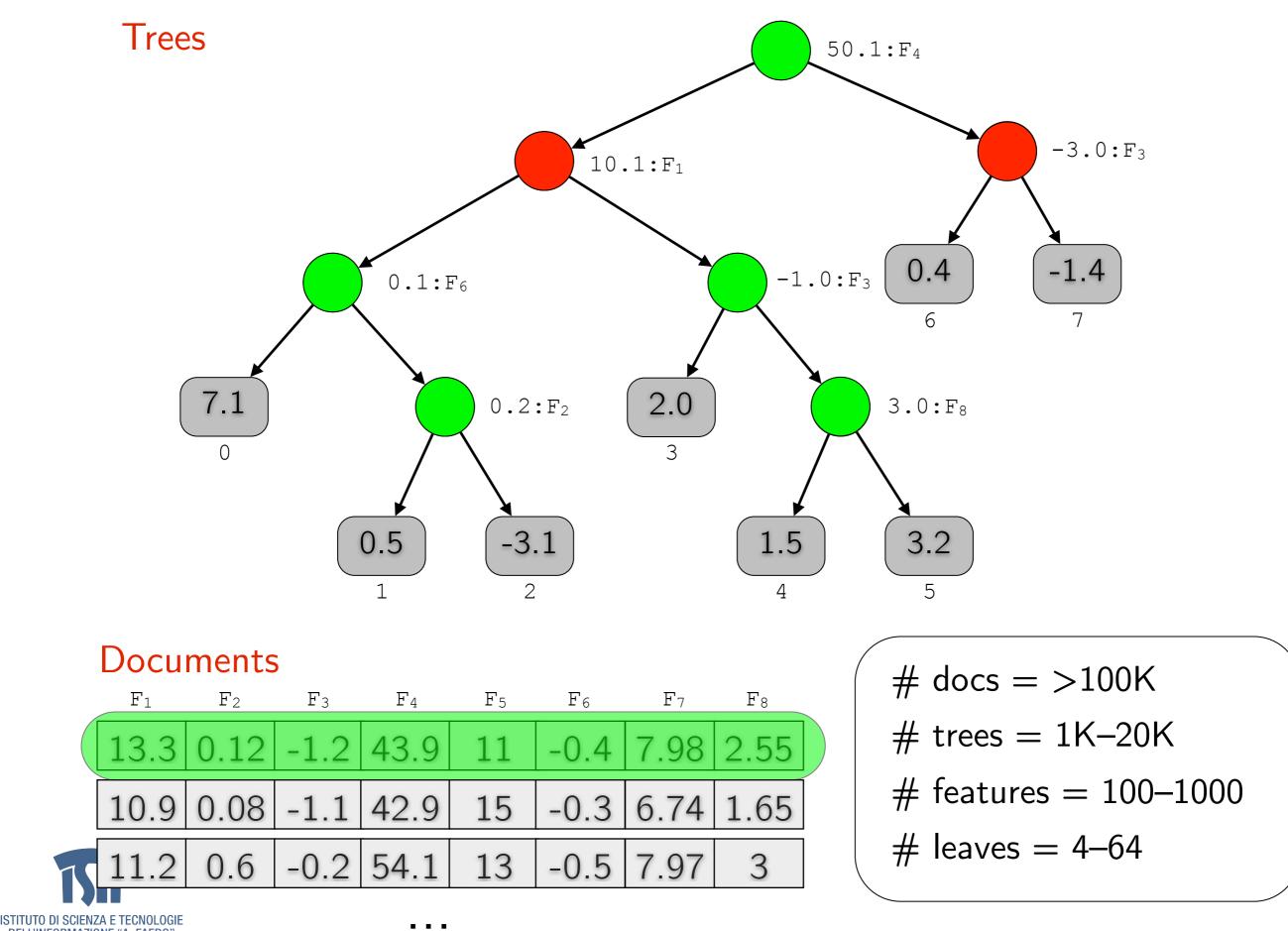


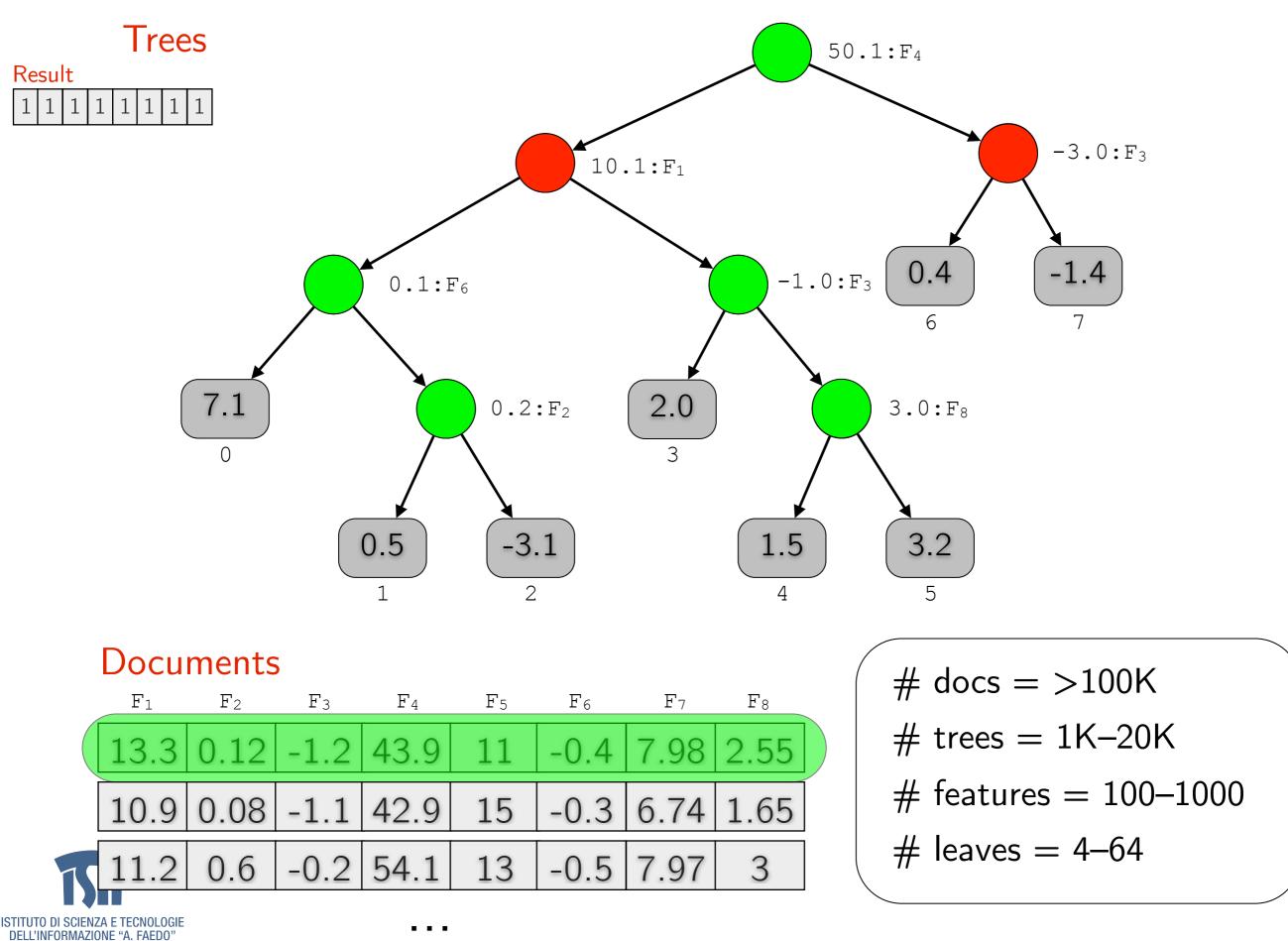


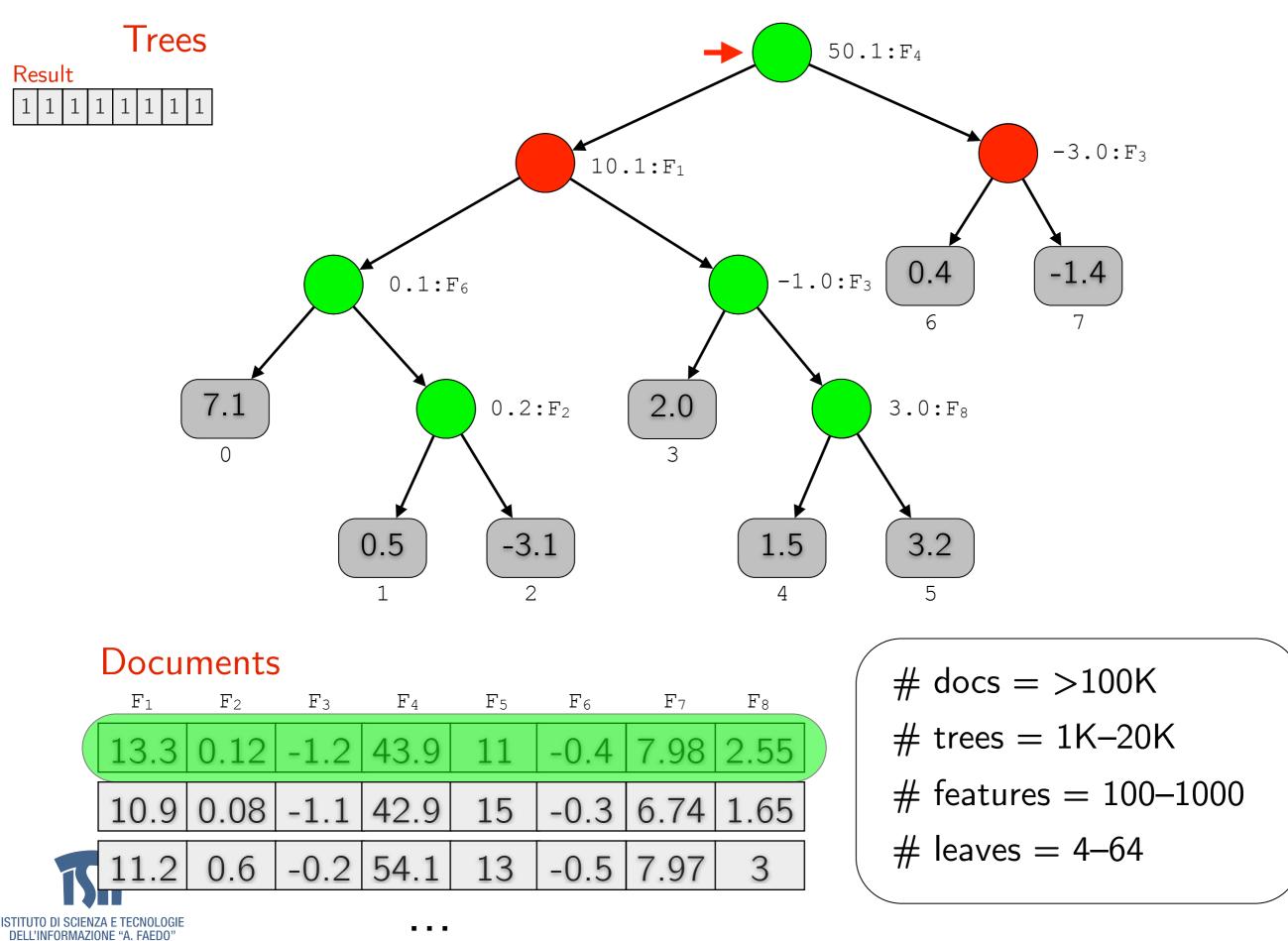


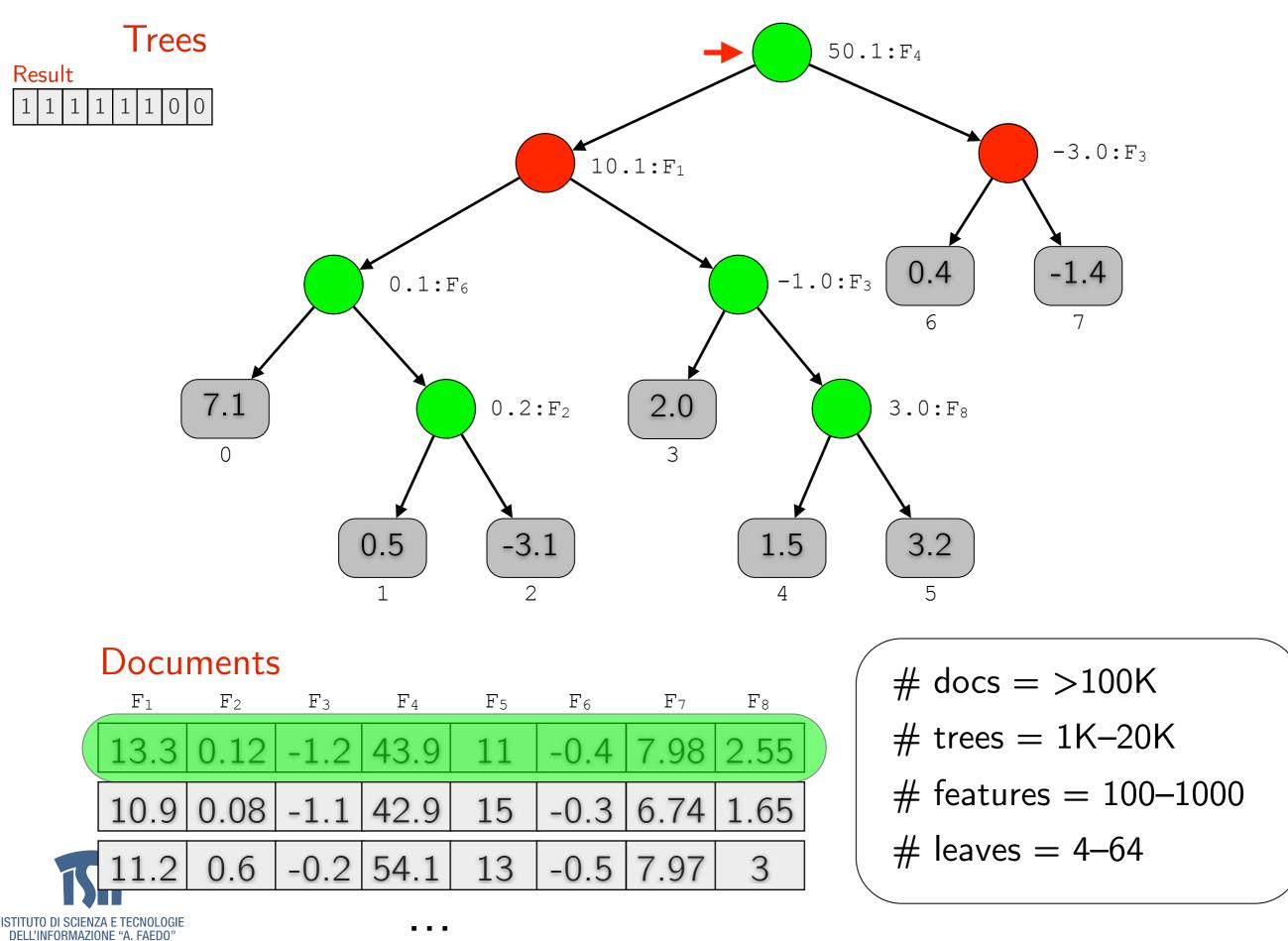


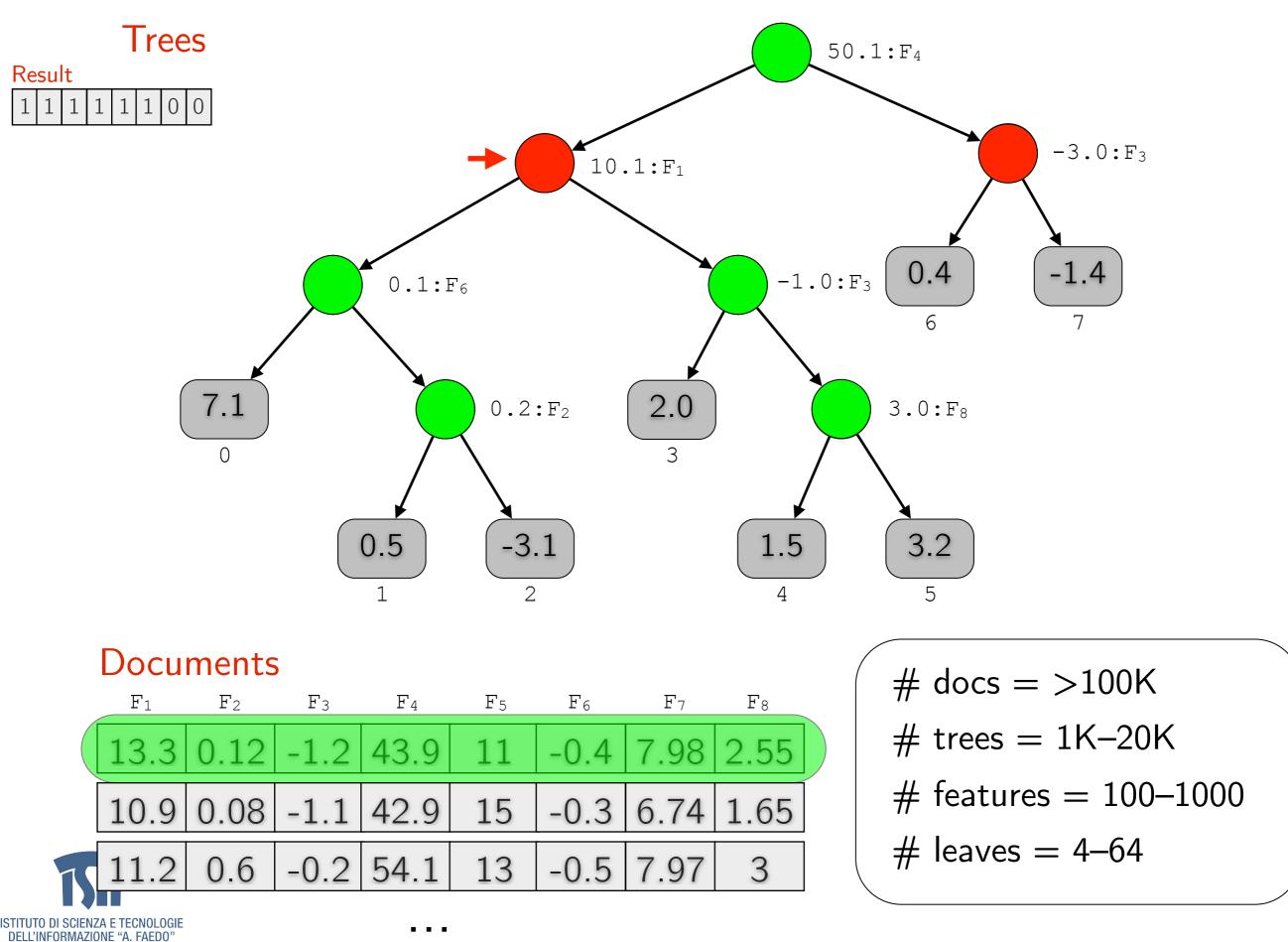


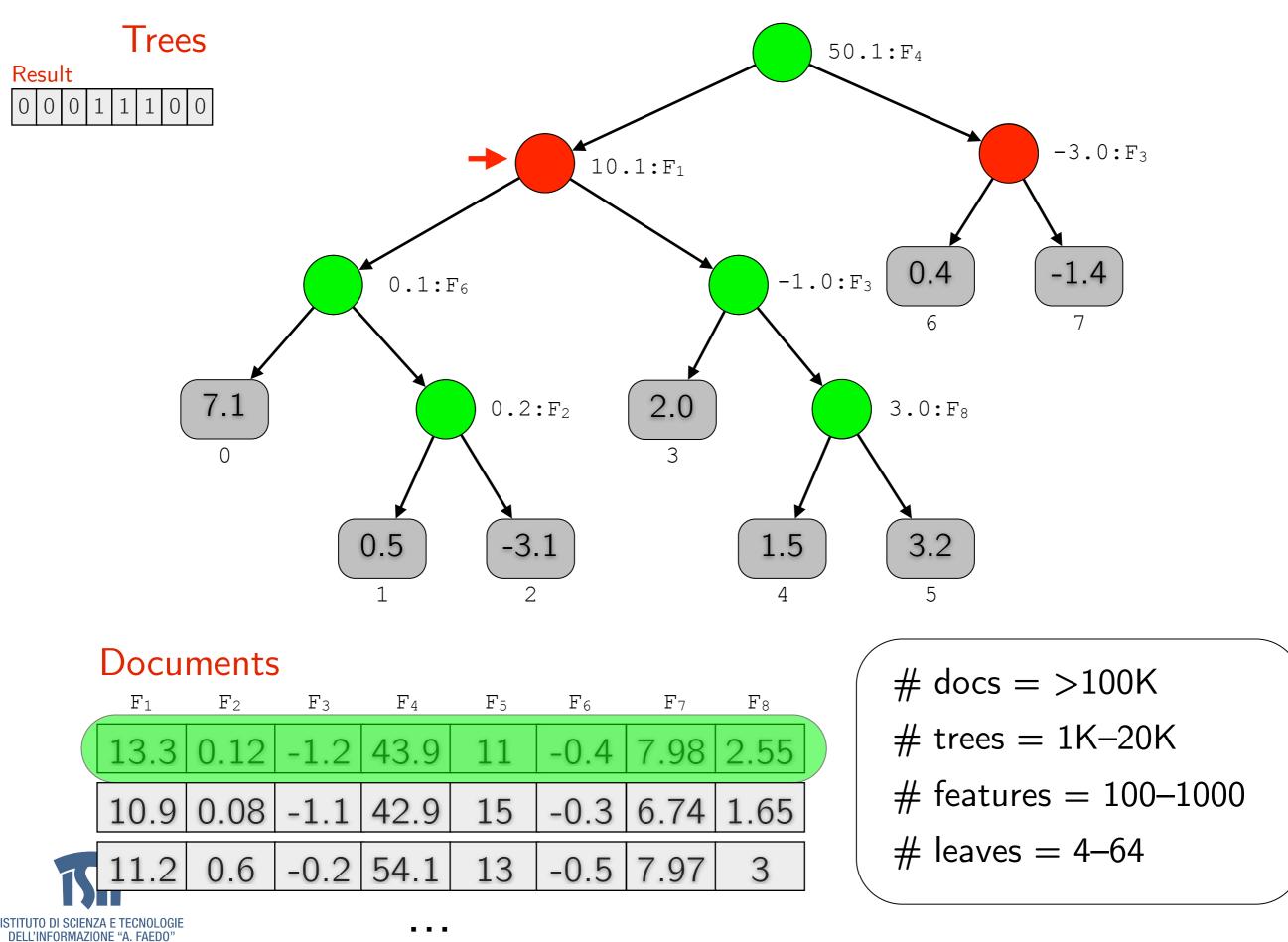


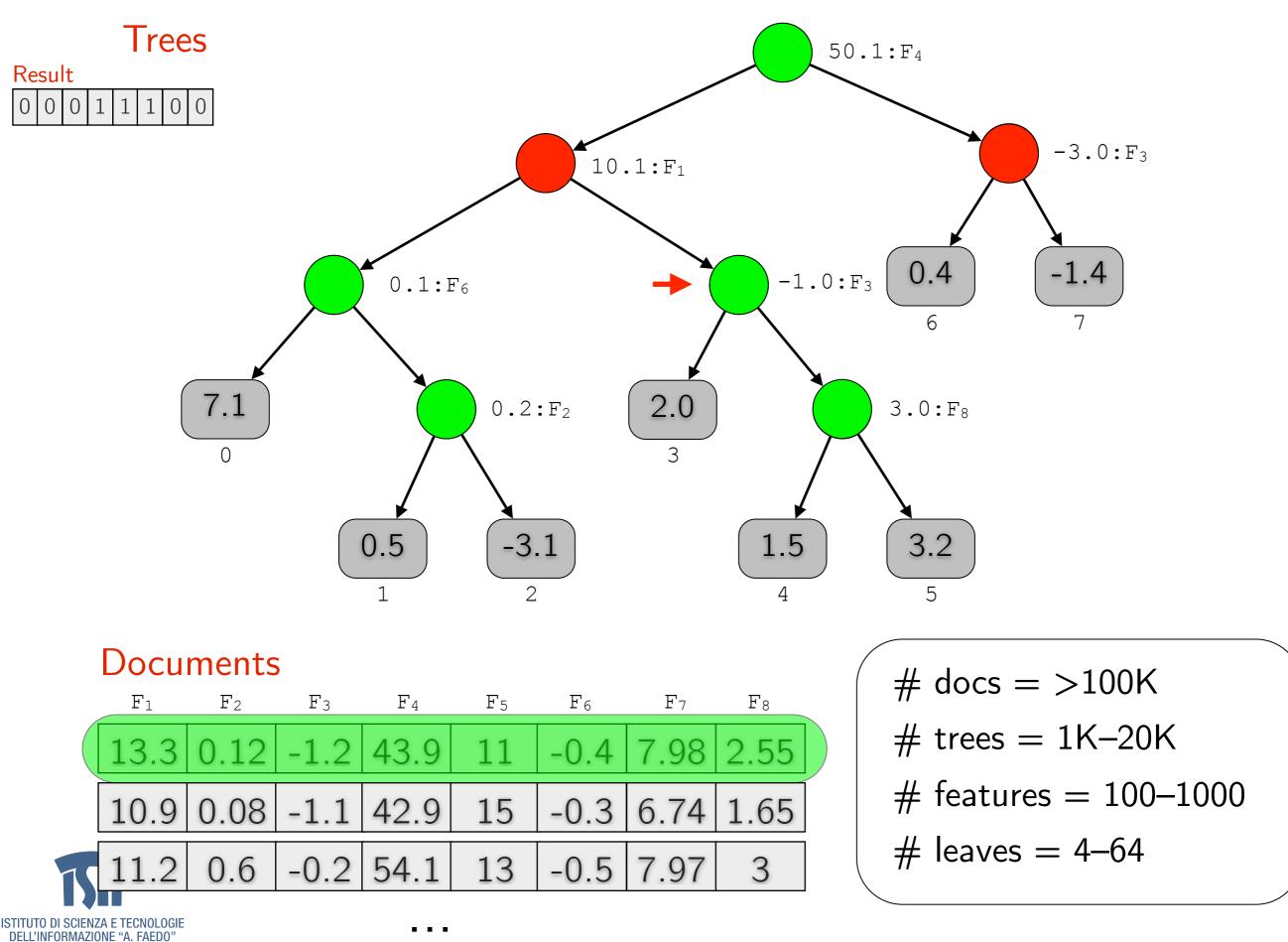


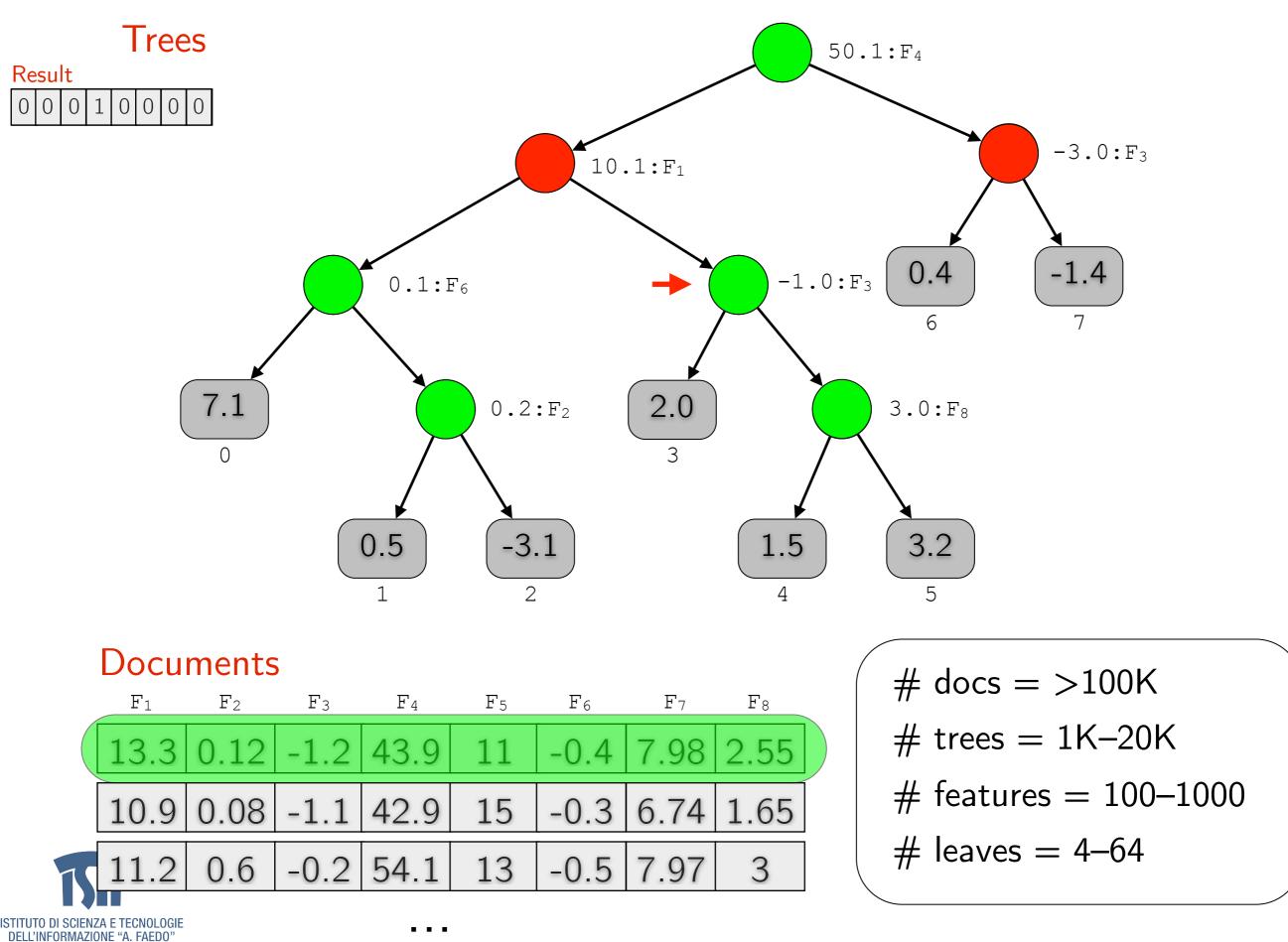


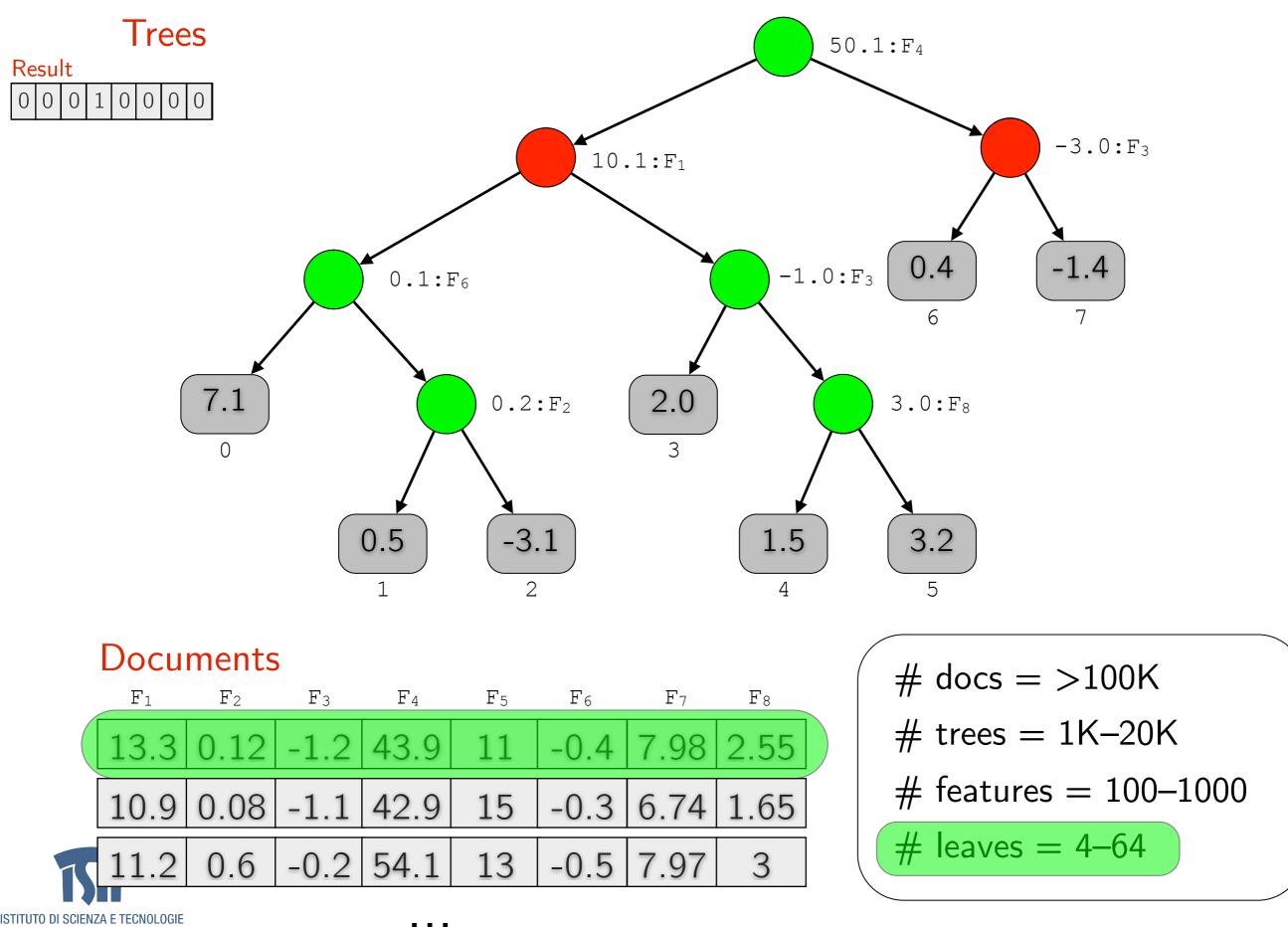


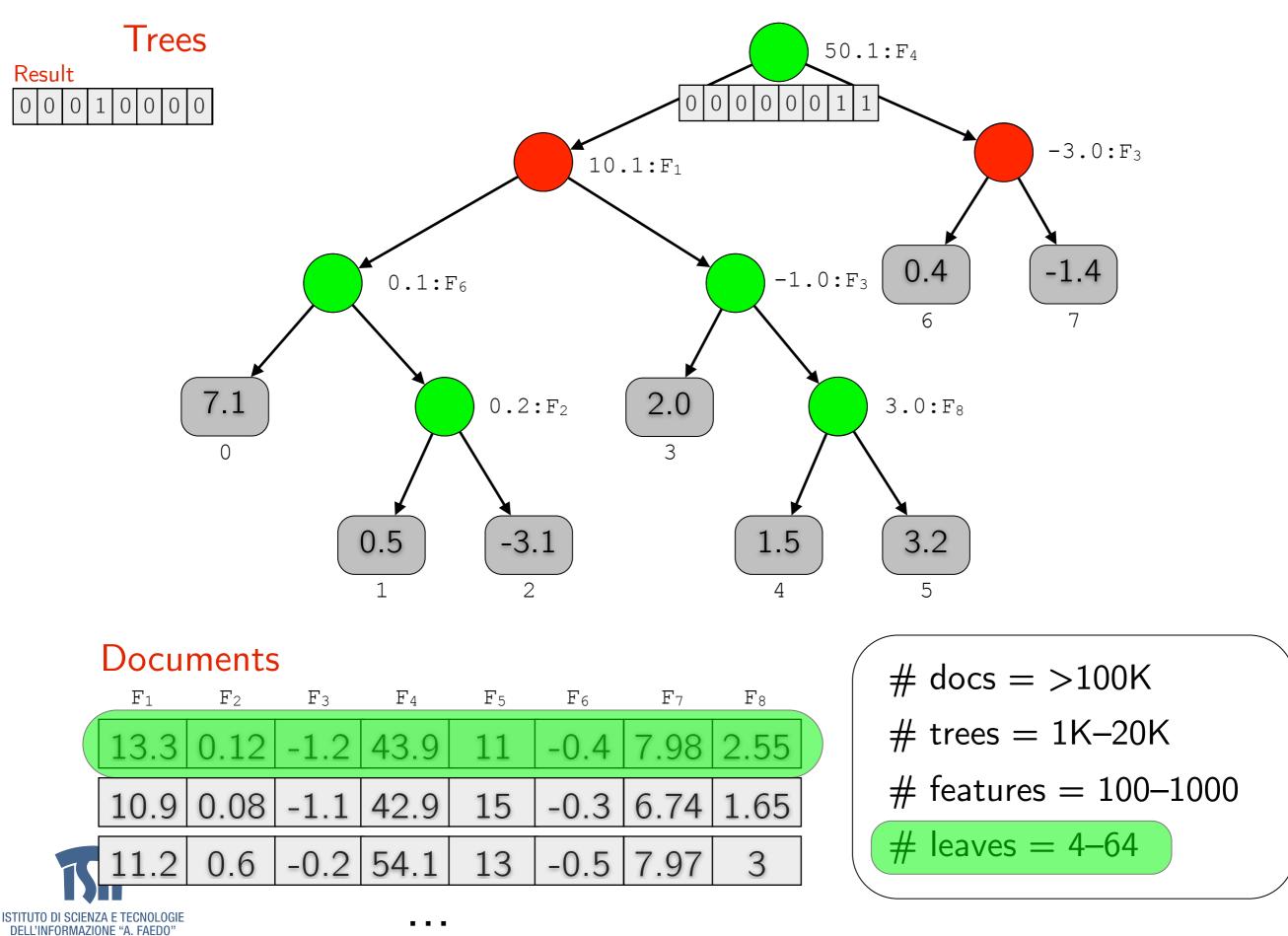


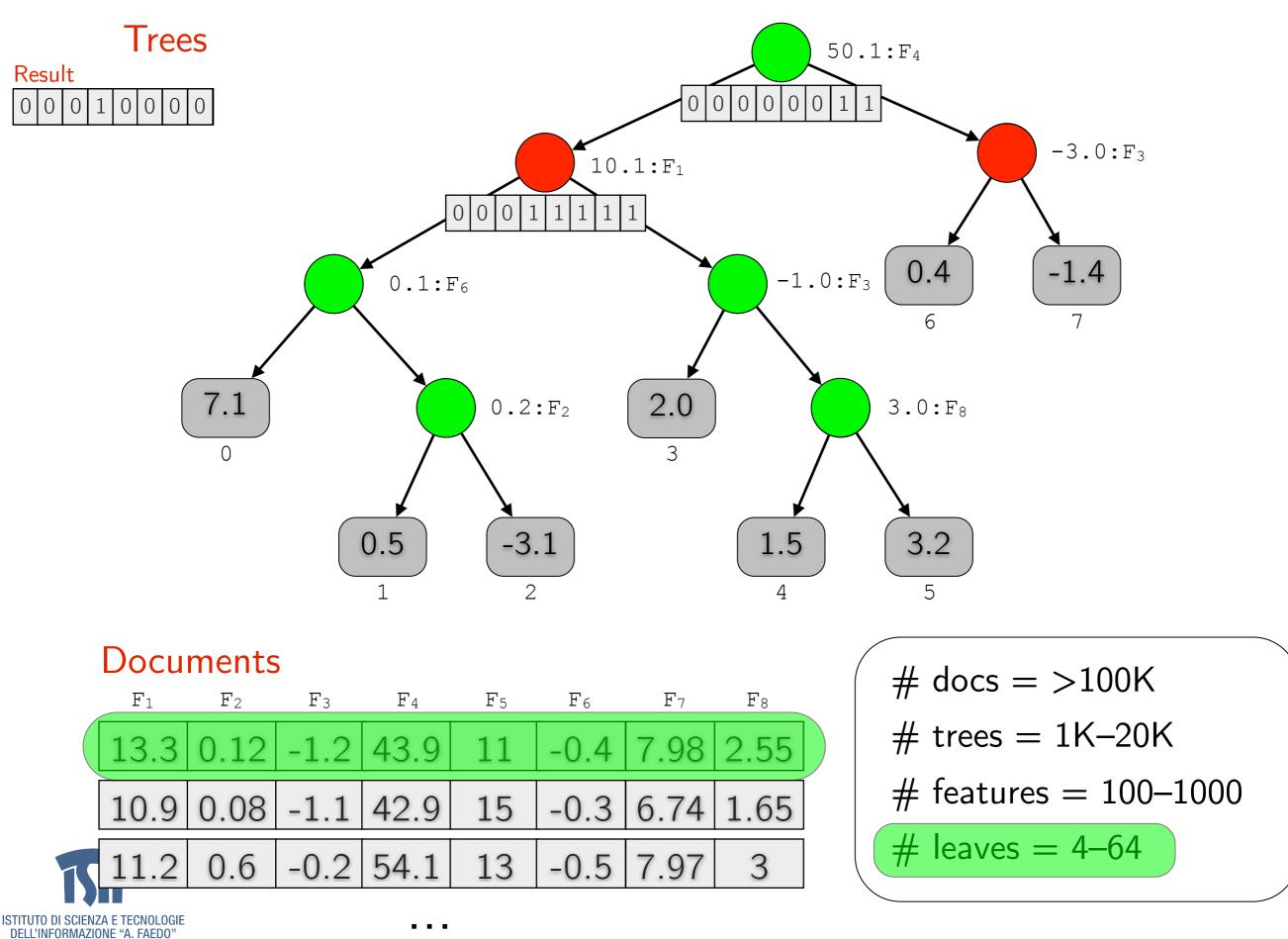


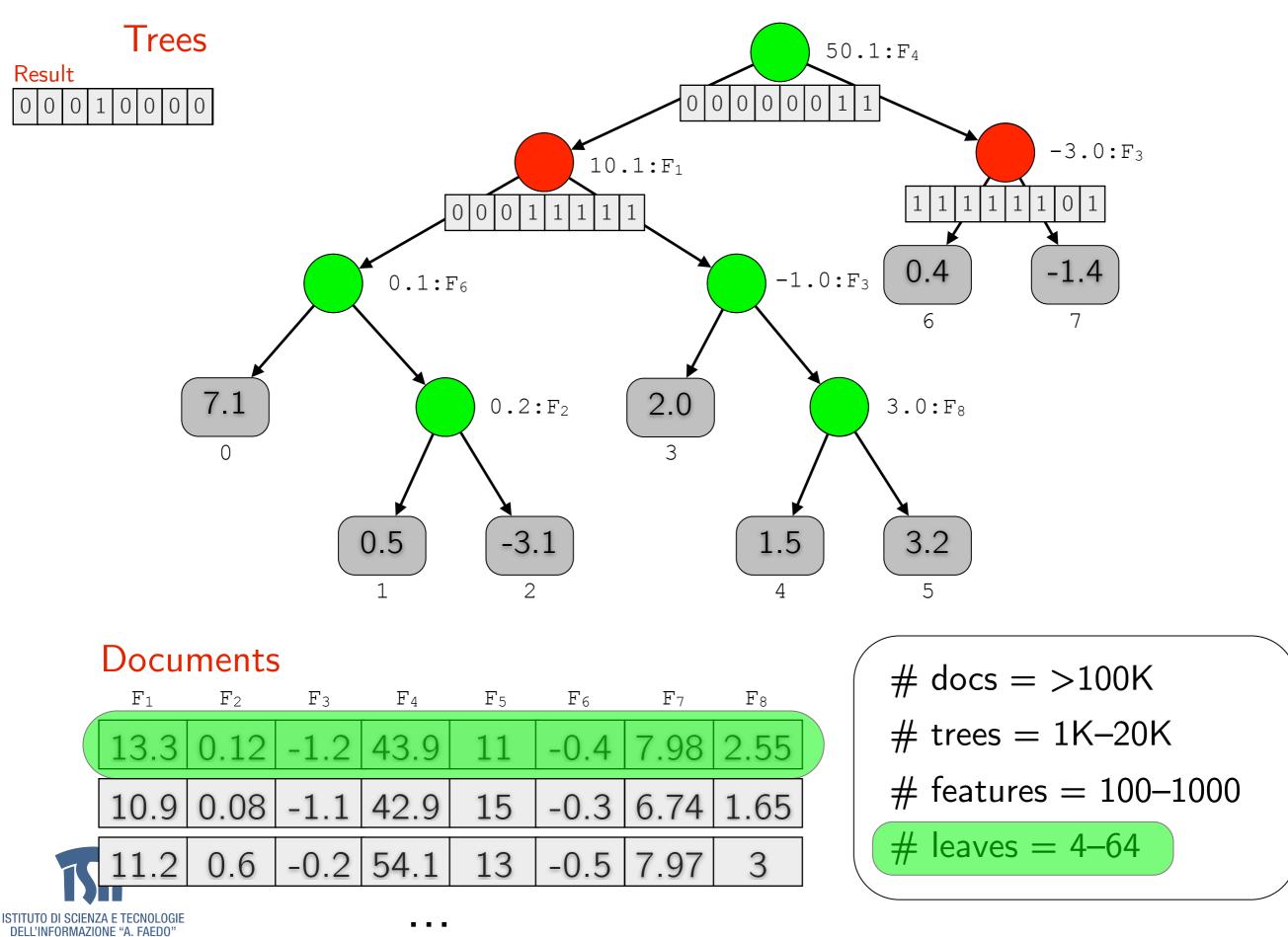


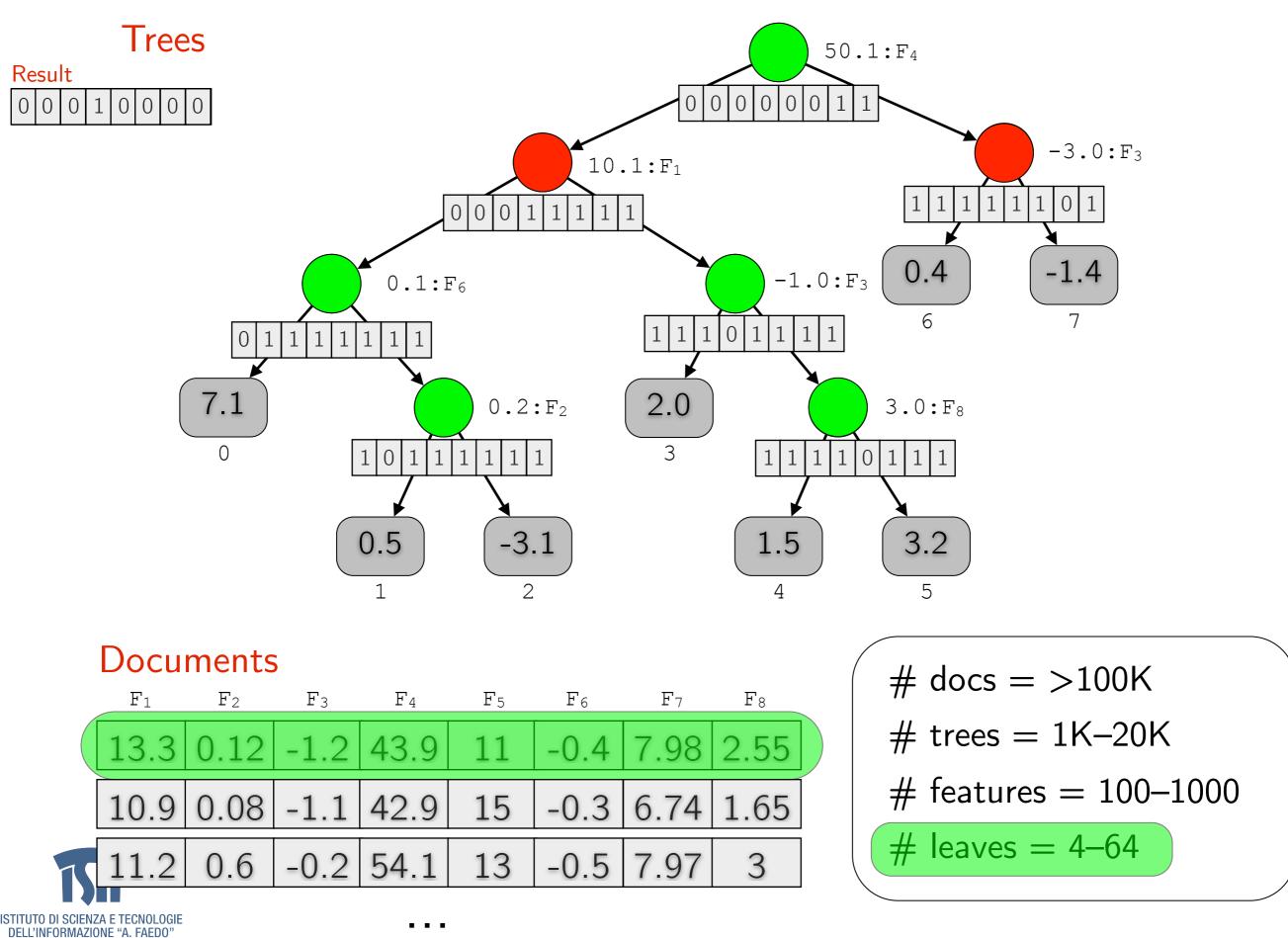


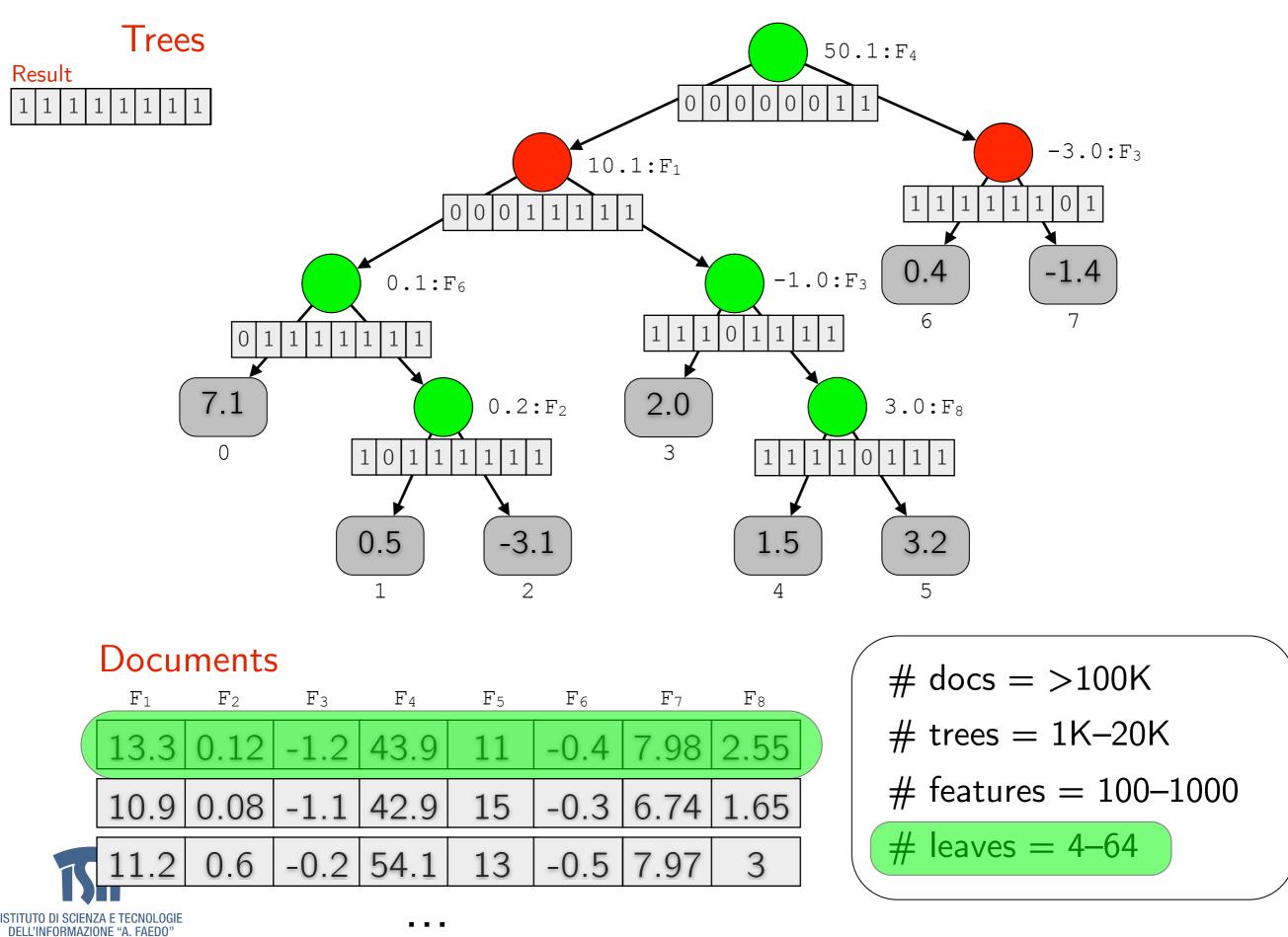


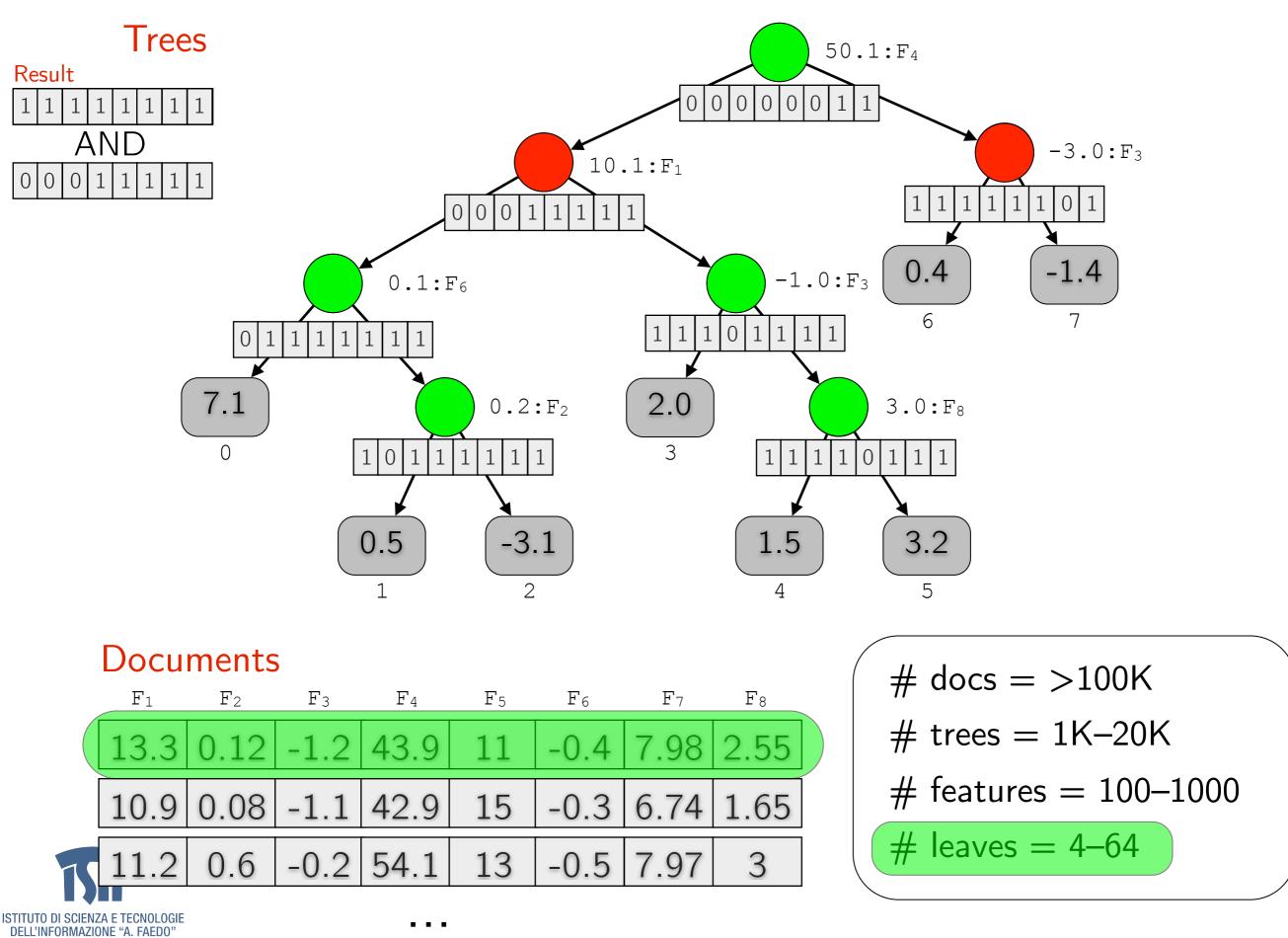


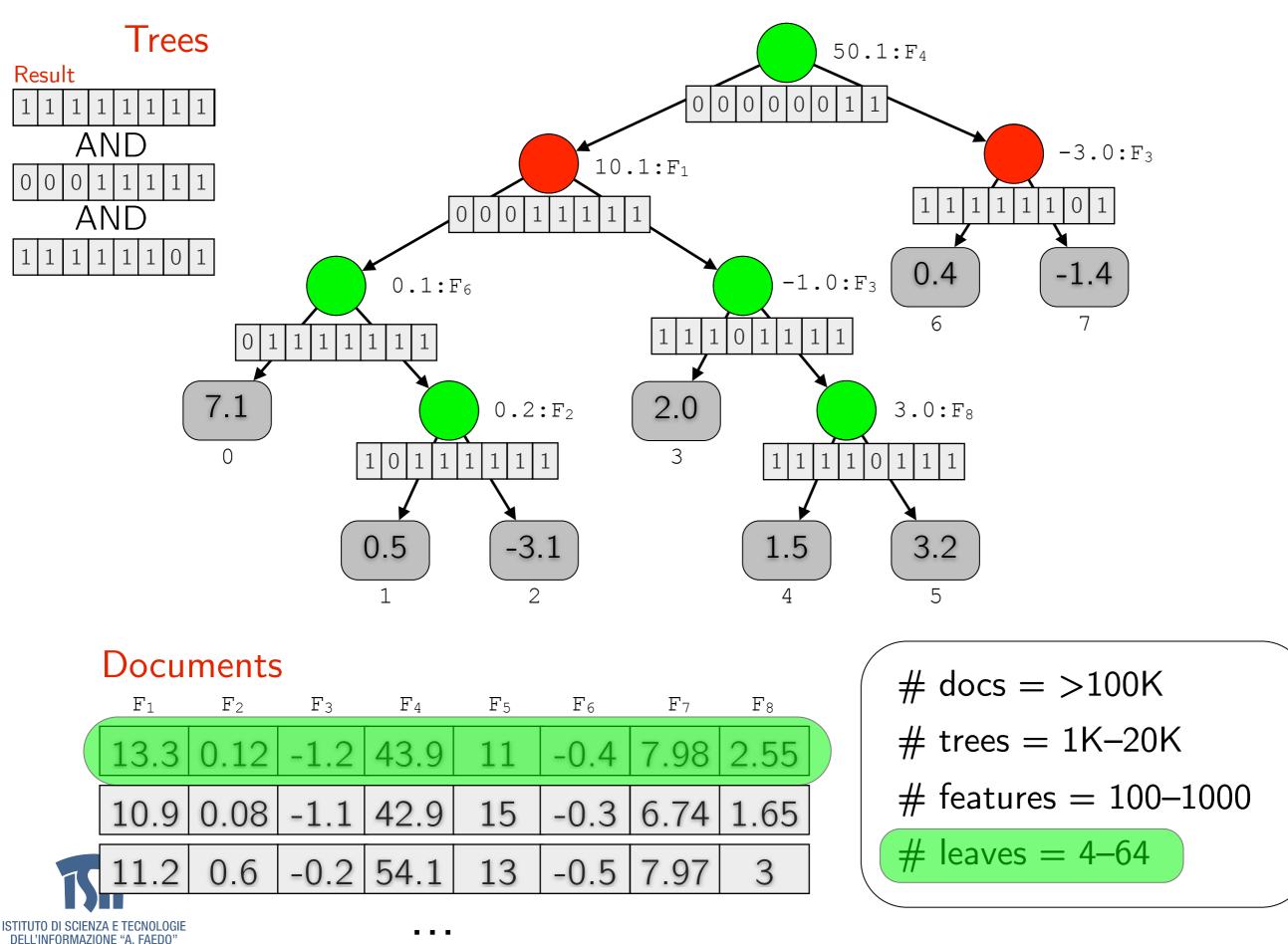


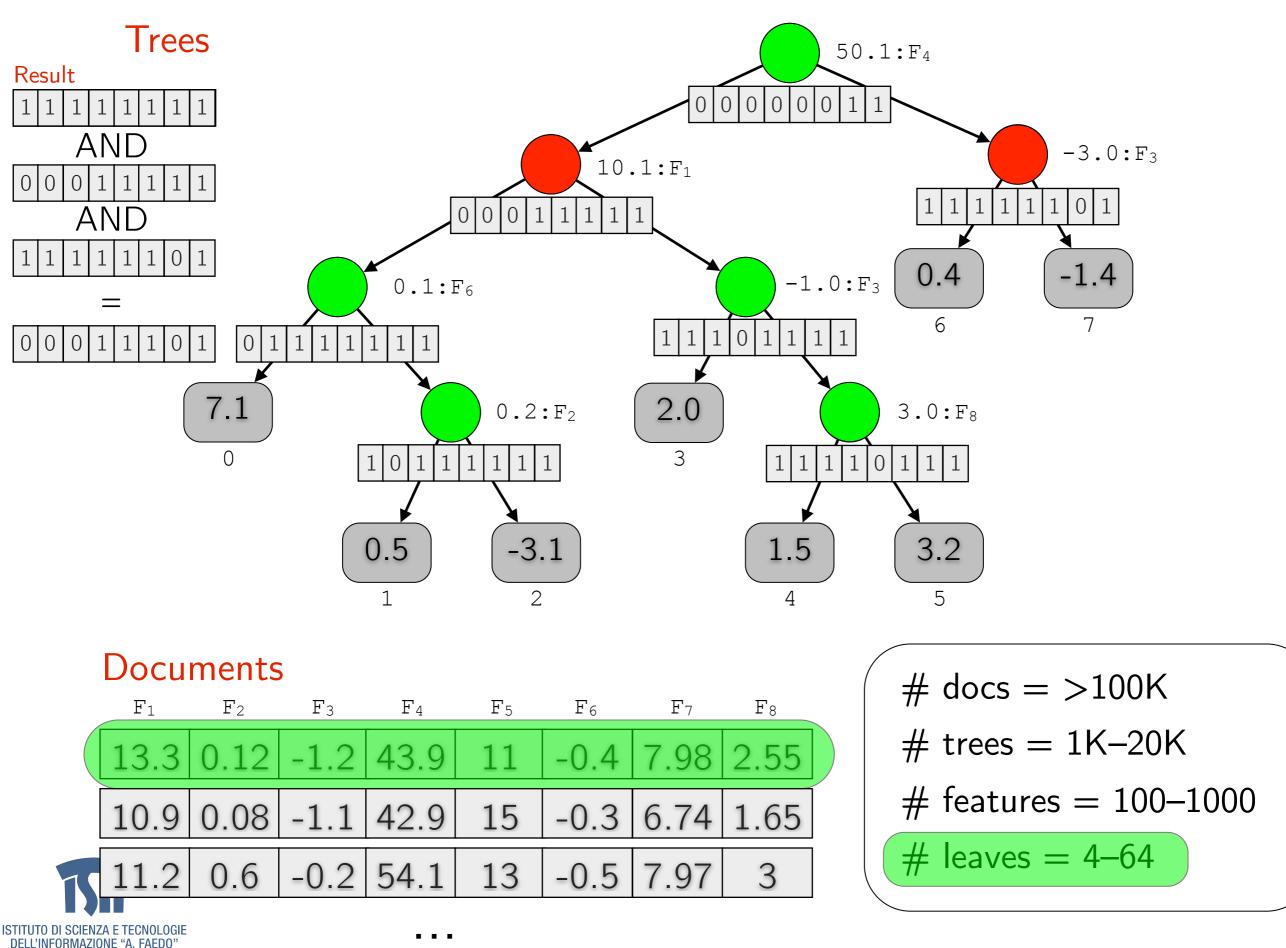


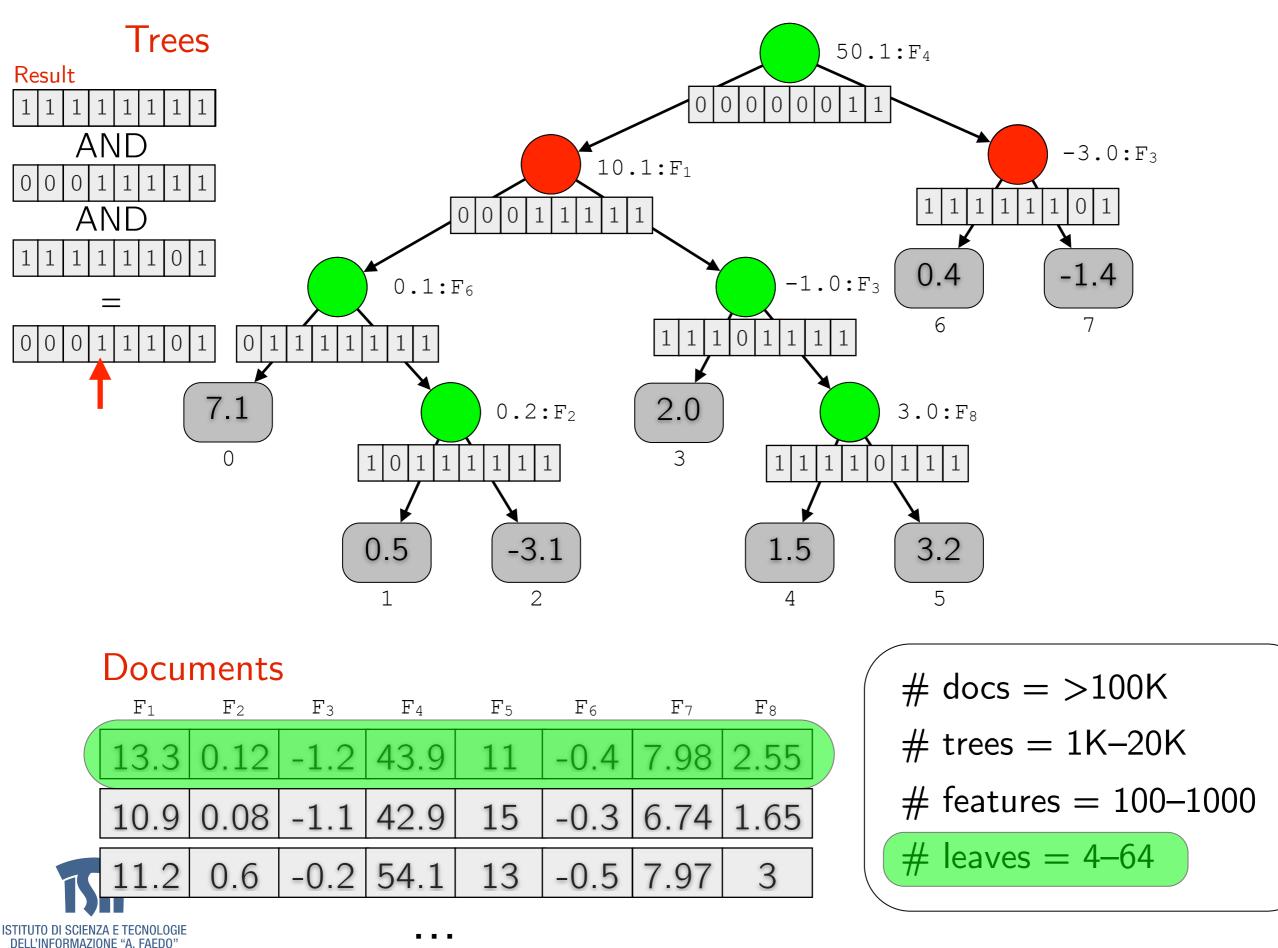




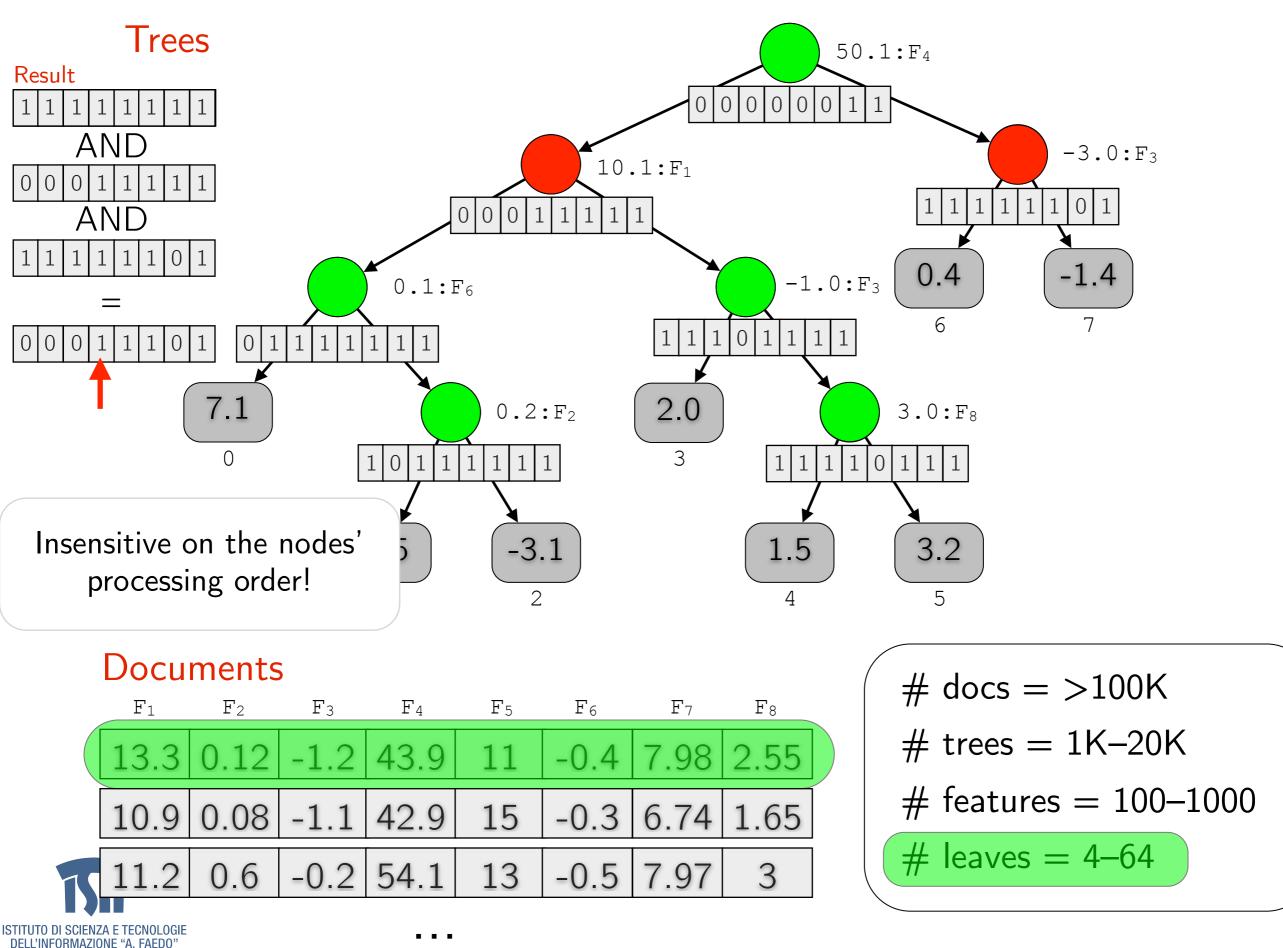




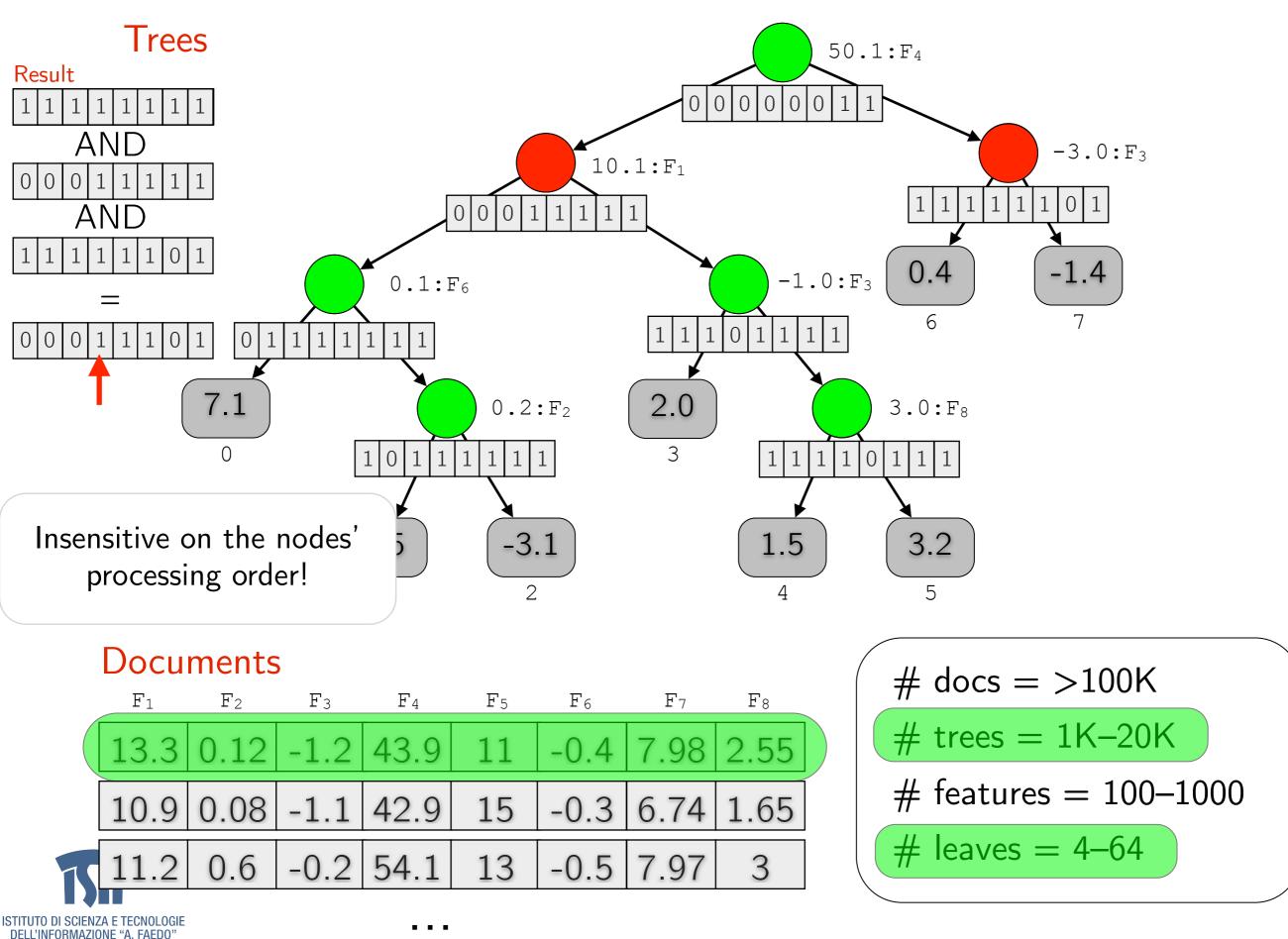


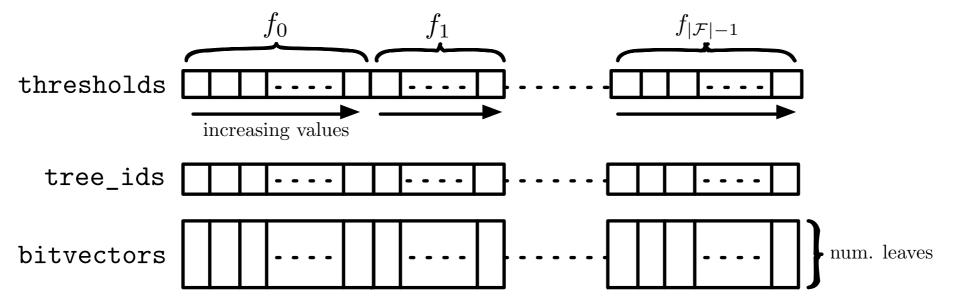


An alternative traversing algorithm

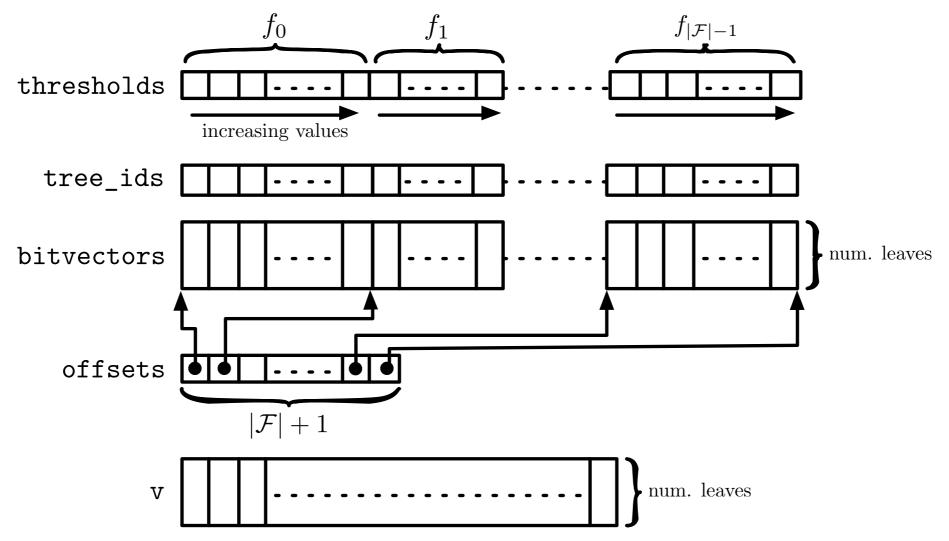


An alternative traversing algorithm

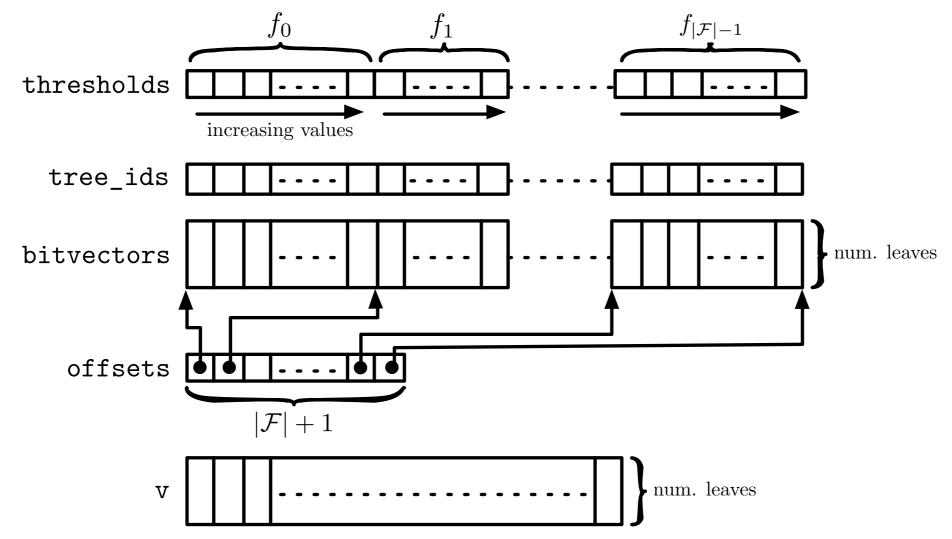


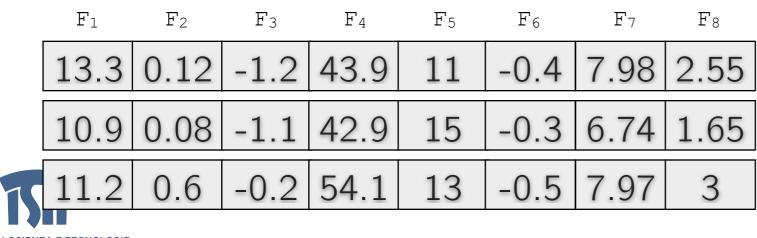


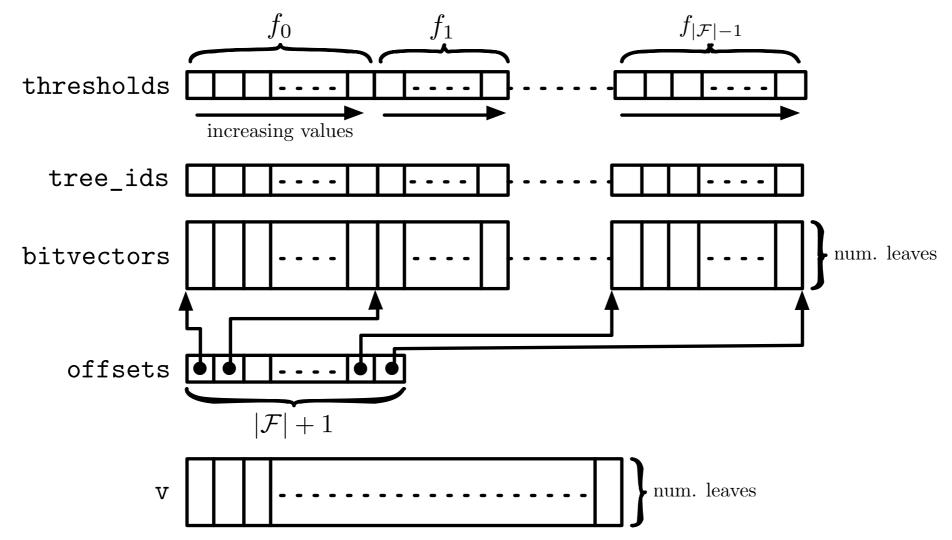




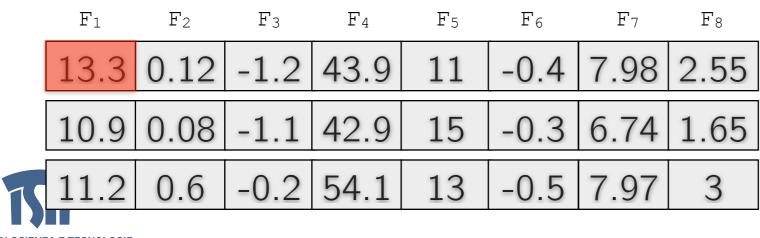




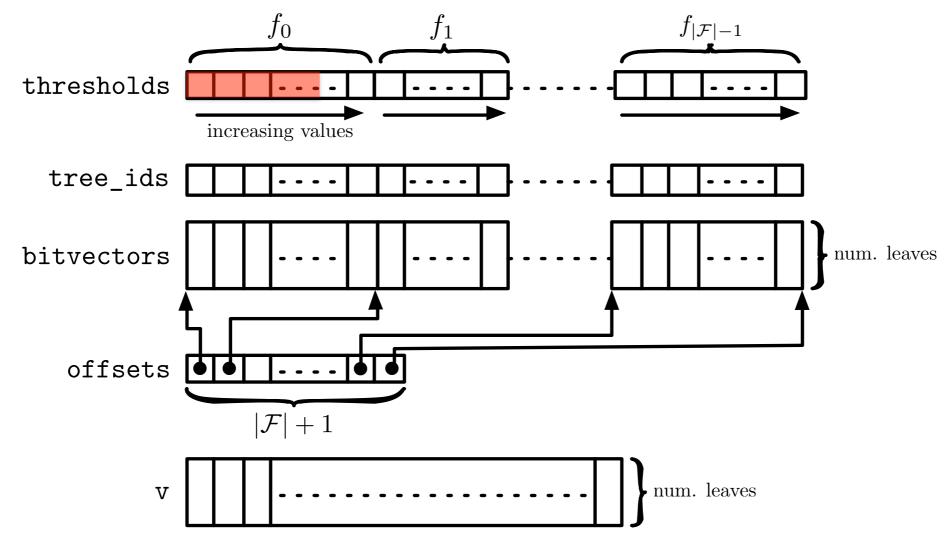


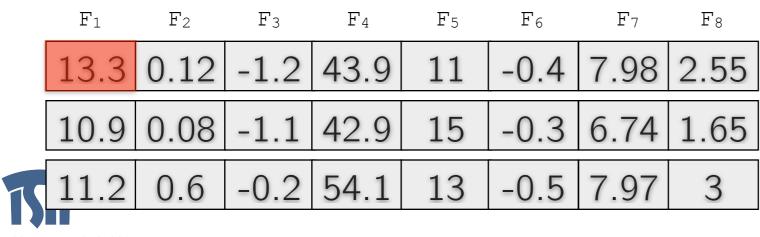


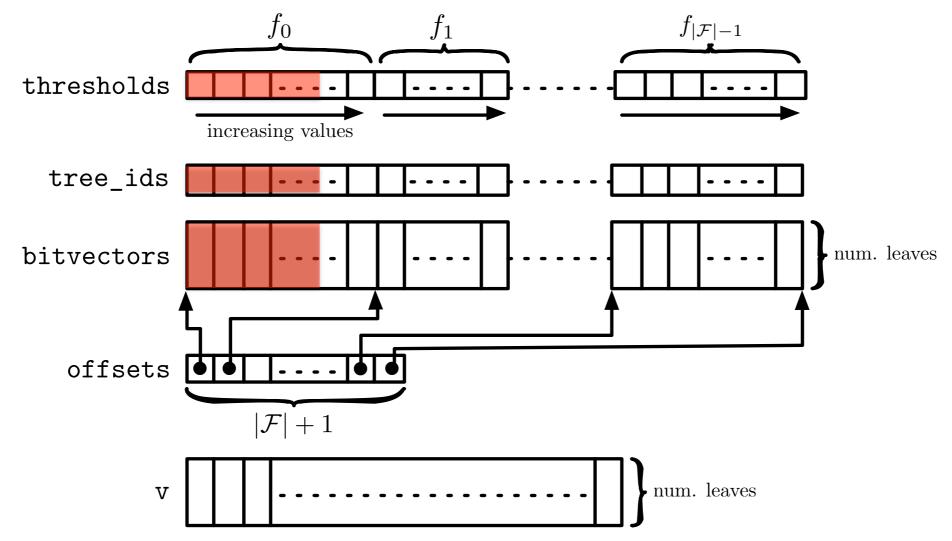
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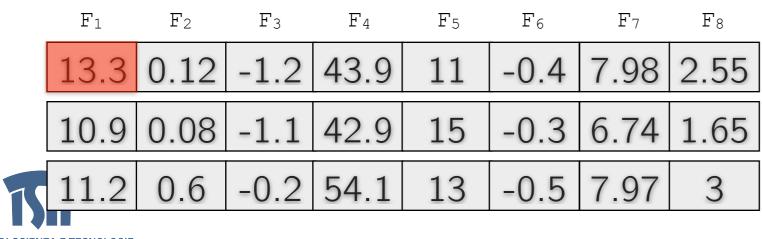


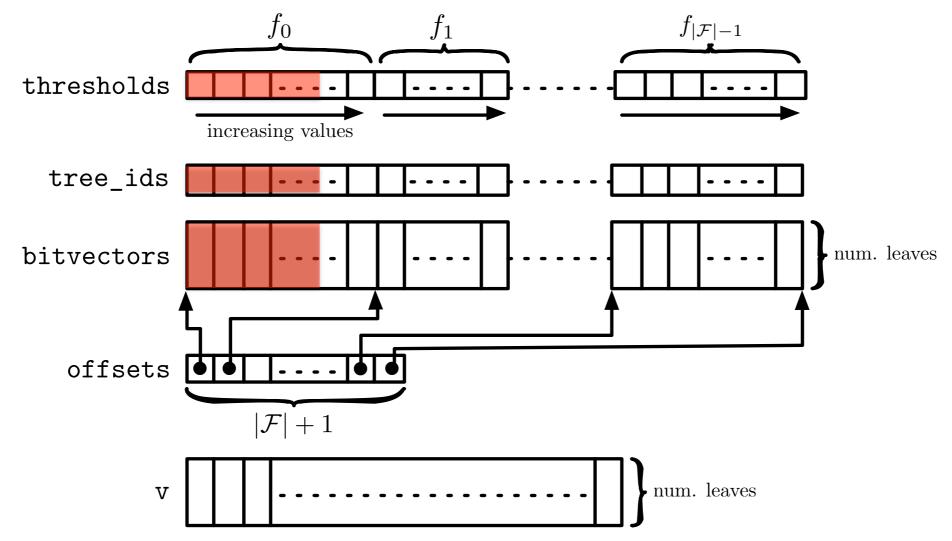
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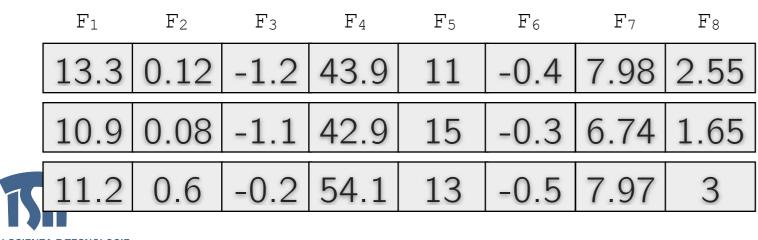


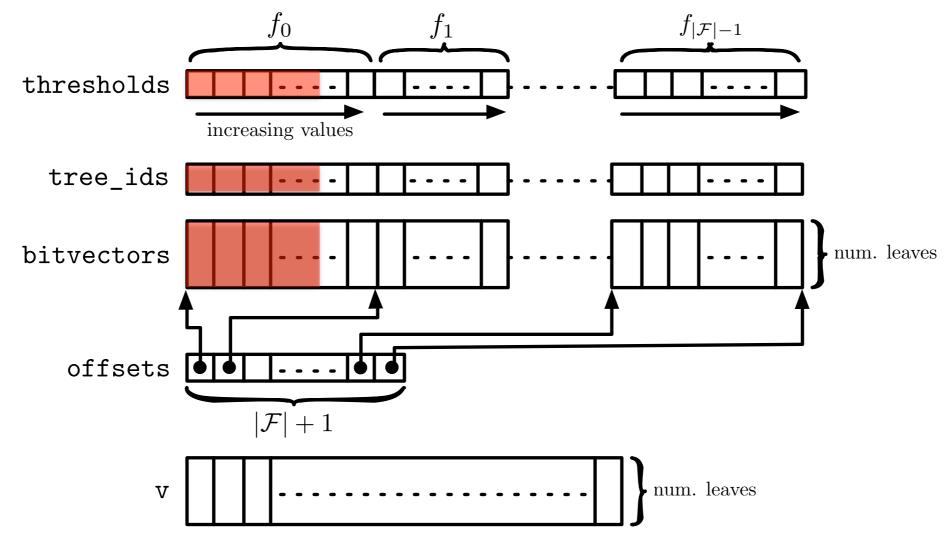




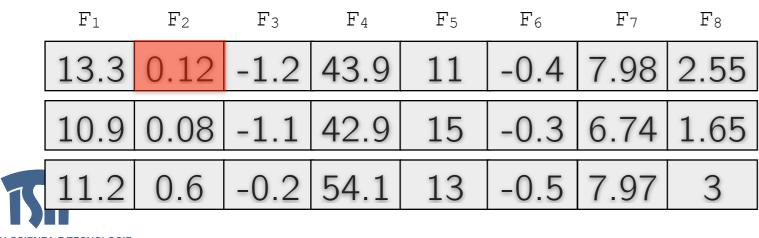




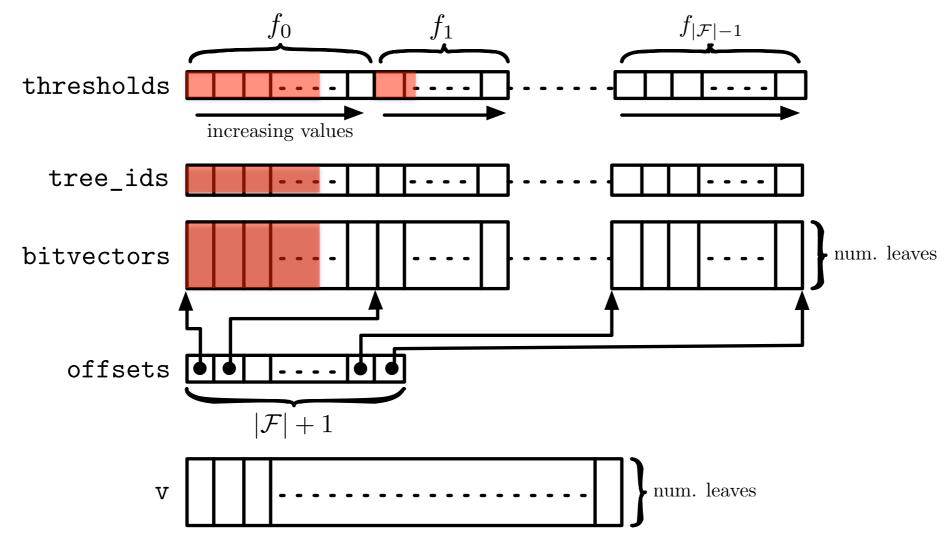


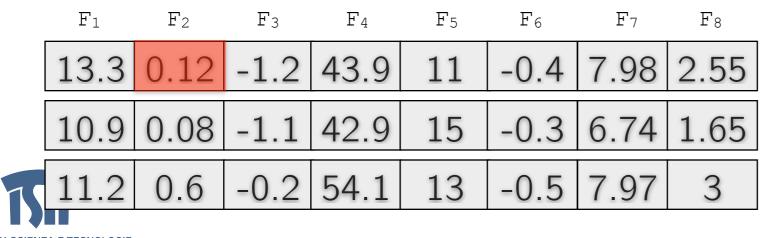


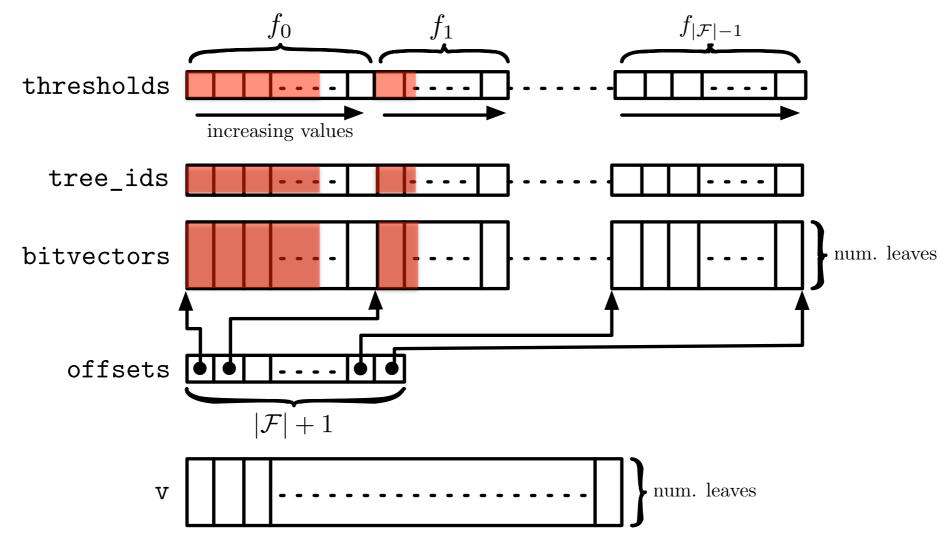
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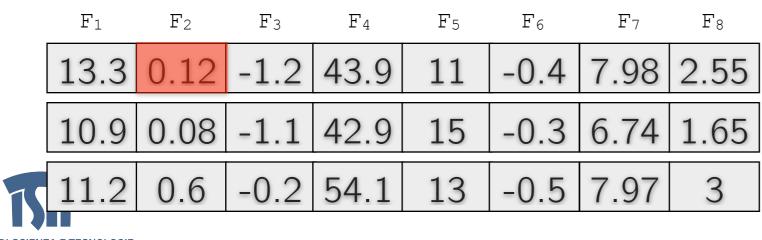


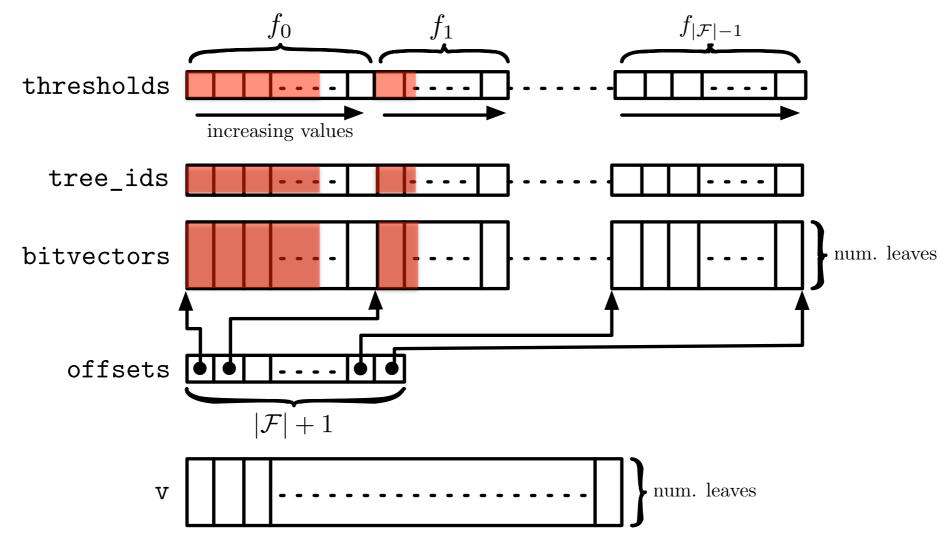
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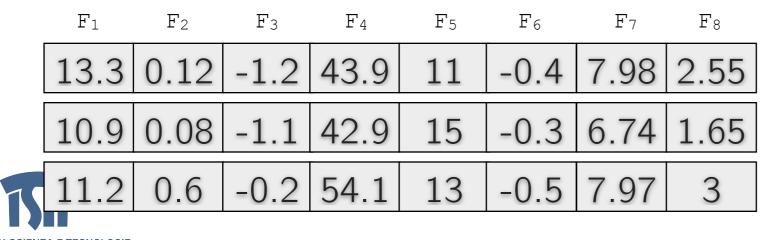


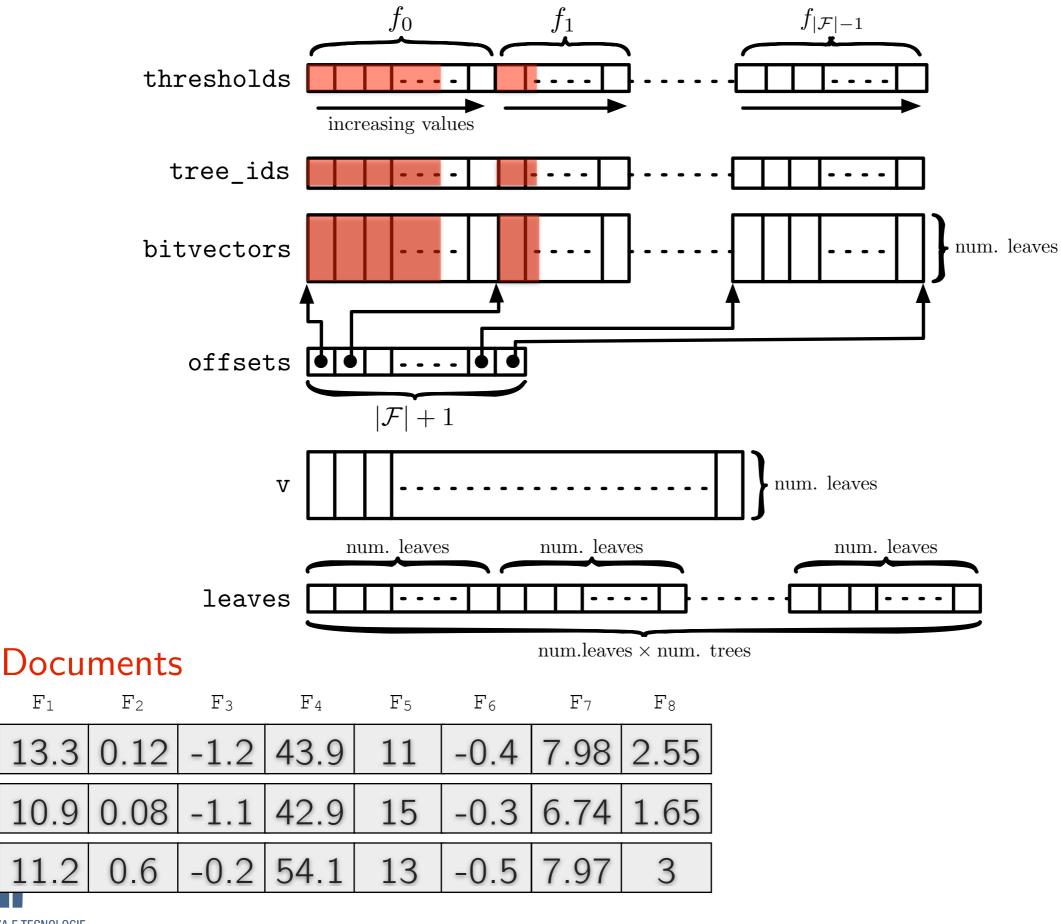


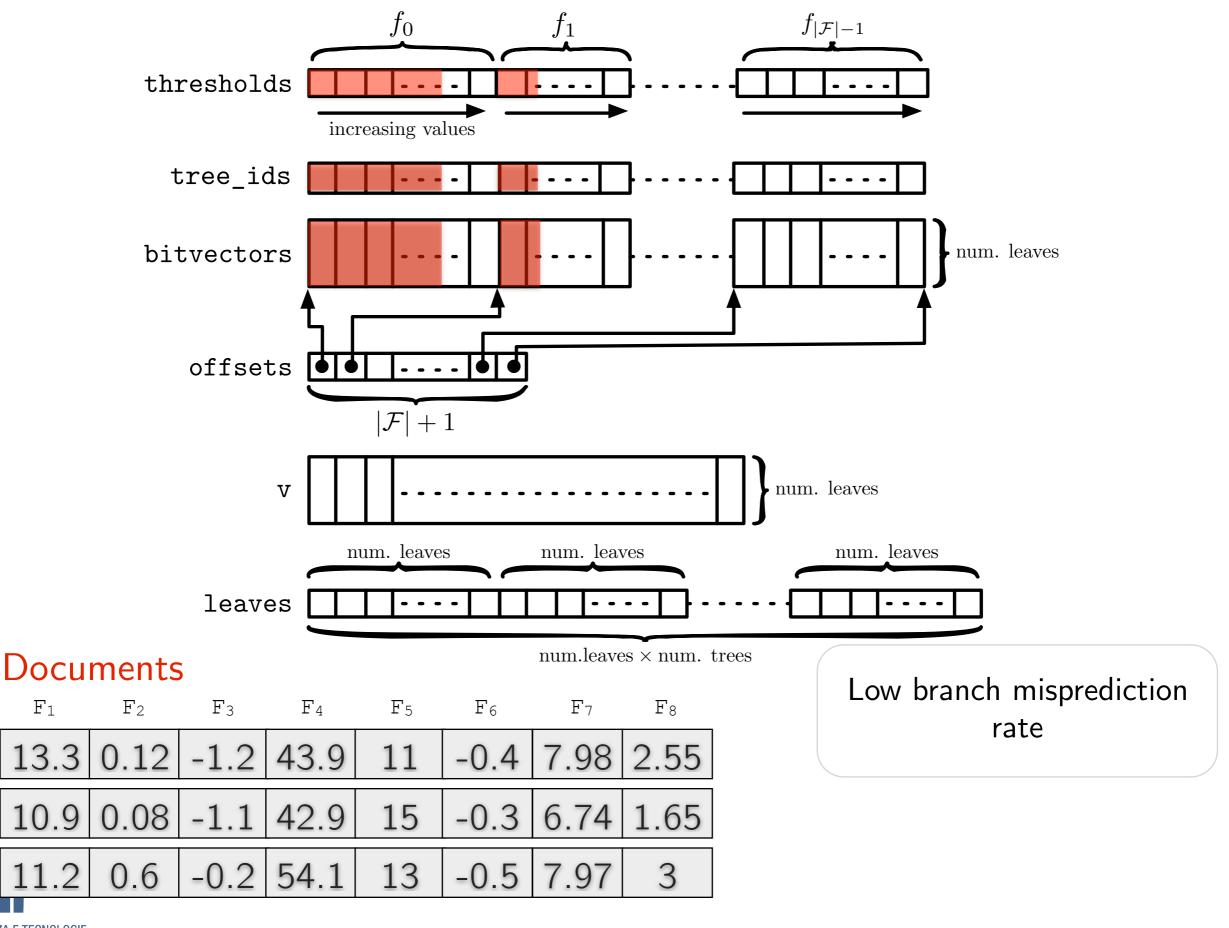


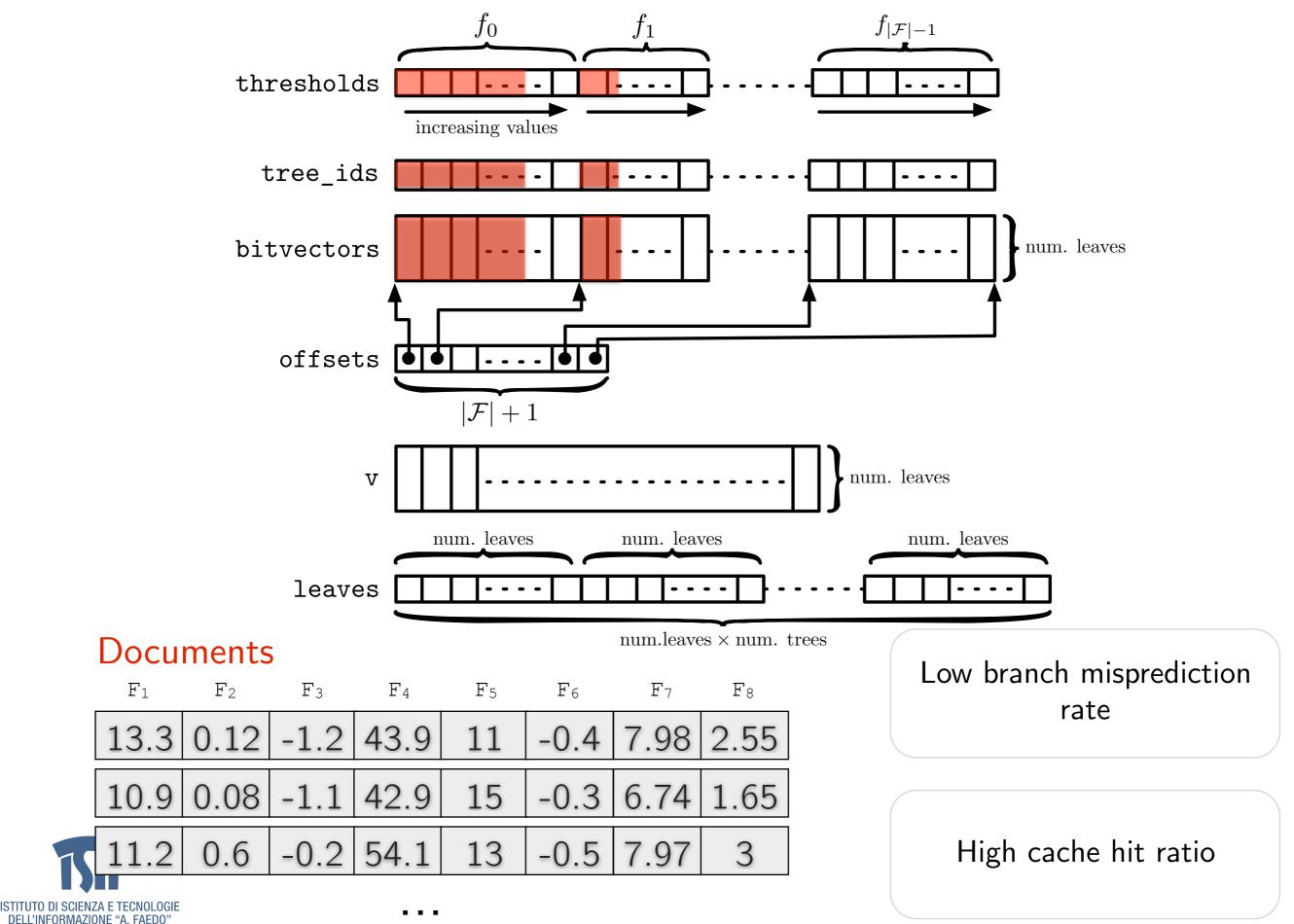




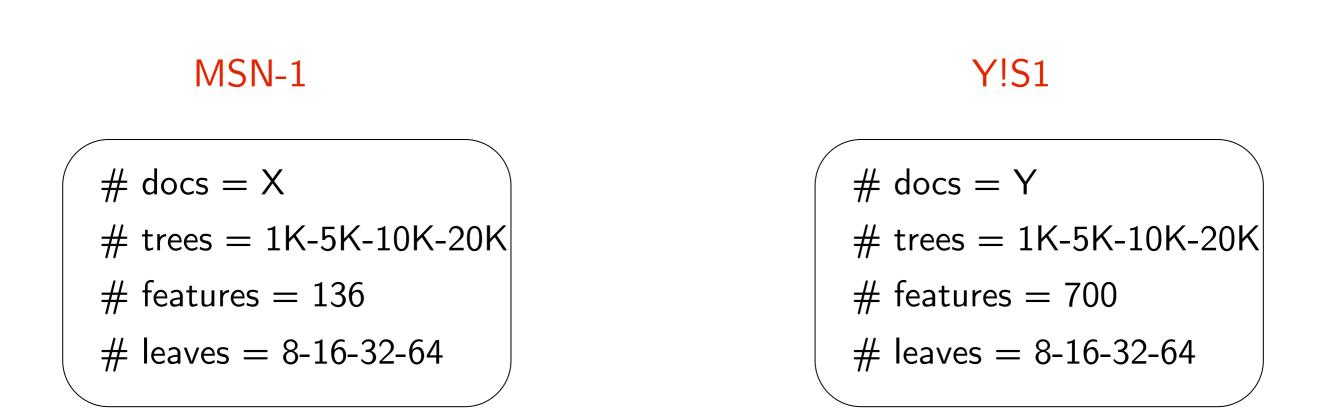








Results



$\lambda\text{-}MART$ for performing the training phase optimizing NDCG@10



Method	Λ	Number of trees/dataset								
		1,000		5,000		10,	10,000		20,000	
		MSN-1	Y!S1	MSN-1	Y!S1	MSN-1	Y!S1	MSN-1	Y!S1	
QS		2.2 (-)	4.3 (-)	10.5 (-)	14.3 (-)	20.0 (-)	25.4 (-)	40.5 (-)	48.1 (-)	
VPred	8	7.9 (3.6x)	8.5 (2.0x)	$40.2 (3.8 \mathrm{x})$	41.6 (2.9x)	80.5 (4.0x)	82.7 (3.3)	161.4 (4.0x)	164.8 (3.4x)	
IF-THEN-ELSE	0	8.2 (3.7x)	10.3 (2.4x)	81.0(7.7x)	85.8~(6.0x)	185.1 (9.3x)	185.8 (7.3x)	709.0 (17.5x)	772.2 (16.0x)	
STRUCT+		21.2 (9.6x)	23.1 (5.4x)	107.7 (10.3x)	112.6 (7.9x)	373.7 (18.7x)	390.8 (15.4x)	1150.4 (28.4x)	1141.6 (23.7x)	
QS		2.9 (-)	6.1 (-)	16.2 (-)	22.2 (-)	32.4 (-)	41.2 (-)	67.8 (-)	81.0 (-)	
VPred	16	16.0 (5.5x)	16.5 (2.7x)	82.4 (5.0x)	82.8 (3.7x)	165.5 (5.1x)	165.2 (4.0x)	336.4 (4.9x)	336.1 (4.1x)	
IF-THEN-ELSE		18.0 (6.2x)	21.8 (3.6x)	126.9 (7.8x)	130.0 (5.8x)	617.8 (19.0x)	406.6 (9.9x)	1767.3 (26.0x)	1711.4 (21.1x)	
STRUCT+		42.6 (14.7x)	41.0 (6.7x)	424.3 (26.2x)	403.9 (18.2x)	1218.6 (37.6x)	1191.3 (28.9x)	2590.8 (38.2x)	2621.2 (32.4x)	
QS		5.2 (-)	9.7 (-)	27.1 (-)	34.3 (-)	59.6 (-)	70.3 (-)	155.8 $(-)$	160.1 (-)	
VPred	32	31.9(6.1x)	31.6 (3.2x)	$165.2 (6.0 \mathrm{x})$	162.2 (4.7x)	343.4 (5.7x)	336.6 (4.8x)	711.9 (4.5x)	694.8 (4.3x)	
IF-THEN-ELSE	02	34.5~(6.6x)	36.2 (3.7x)	300.9 (11.1x)	277.7 (8.0x)	1396.8 (23.4x)	1389.8 (19.8x)	3179.4 (20.4x)	3105.2 (19.4x)	
STRUCT+		69.1 (13.3x)	67.4 (6.9x)	928.6 (34.2x)	834.6 (24.3x)	1806.7 (30.3x)	1774.3 (25.2x)	4610.8 (29.6x)	4332.3 (27.0x)	
QS	64	9.5 (-)	15.1 $(-)$	56.3 (-)	66.9 (-)	157.5 (-)	159.4 (-)	425.1 (-)	343.7 (-)	
VPred		62.2 (6.5x)	57.6 (3.8x)	355.2 (6.3x)	334.9(5.0x)	734.4 (4.7x)	706.8 (4.4x)	1309.7 (3.0x)	1420.7 (4.1x)	
IF-THEN-ELSE		55.9(5.9x)	55.1 (3.6x)	933.1 (16.6x)	935.3 $(14.0x)$	2496.5 (15.9x)	2428.6 (15.2x)	4662.0 (11.0x)	4809.6 (14.0x)	
STRUCT+		109.8 (11.6x)	116.8 (7.7x)	1661.7 (29.5x)	1554.6 (23.2x)	3040.7 (19.3x)	2937.3 (18.4x)	5437.0 (12.8x)	5456.4 (15.9x)	



Method	Λ	Number of trees/dataset								
		1,000		5,000		10,000		20,000		
		MSN-1	Y!S1	MSN-1	Y!S1	MSN-1	Y!S1	MSN-1	Y!S1	
QS		2.2 (-)	4.3 (-)	10.5 (-)	14.3 (-)	20.0 (-)	25.4 (-)	40.5 (-)	48.1 (-)	
VPred	8	7.9~(3.6x)	8.5 (2.0x)	$40.2 (3.8 \mathrm{x})$	41.6~(2.9x)	80.5 (4.0x)	82.7(3.3)	161.4 (4.0x)	164.8 (3.4x)	
IF-THEN-ELSE	0	8.2(3.7x)	10.3 (2.4x)	81.0(7.7x)	85.8~(6.0x)	185.1 (9.3x)	185.8 (7.3x)	709.0 (17.5x)	772.2 (16.0x)	
STRUCT+		21.2 (9.6x)	23.1 (5.4x)	107.7 (10.3x)	112.6 (7.9x)	373.7 (18.7x)	390.8 (15.4x)	1150.4 (28.4x)	1141.6 (23.7x)	
QS		2.9 (-)	6.1 (-)	16.2 (-)	22.2 (-)	32.4 (-)	41.2 (-)	67.8 (-)	81.0 (-)	
VPred	16	16.0 (5.5 x)	16.5 (2.7x)	82.4 (5.0x)	82.8 (3.7x)	165.5 (5.1x)	165.2 (4.0x)	336.4 (4.9x)	336.1 (4.1x)	
IF-THEN-ELSE		18.0 (6.2x)	21.8 (3.6x)	126.9 (7.8x)	130.0 (5.8x)	617.8 (19.0x)	406.6 (9.9x)	1767.3 (26.0x)	1711.4 (21.1x)	
STRUCT+		42.6 (14.7x)	41.0 (6.7x)	424.3 (26.2x)	403.9 (18.2x)	1218.6 (37.6x)	1191.3 (28.9x)	2590.8 (38.2x)	2621.2 (32.4x)	
QS		5.2 $(-)$	9.7 (-)	27.1 (-)	34.3 (-)	59.6 (-)	70.3 (-)	155.8 (-)	160.1 (-)	
VPred	32	31.9~(6.1x)	31.6 (3.2x)	165.2 (6.0x)	162.2 (4.7x)	343.4 (5.7x)	336.6 (4.8x)	711.9 (4.5x)	694.8 (4.3x)	
IF-THEN-ELSE	52	34.5~(6.6x)	36.2 (3.7x)	300.9 (11.1x)	277.7 (8.0x)	1396.8 (23.4x)	1389.8 (19.8x)	3179.4 (20.4x)	3105.2 (19.4x)	
STRUCT+		69.1 (13.3x)	67.4 (6.9x)	928.6 (34.2x)	834.6 (24.3x)	1806.7 (30.3x)	1774.3 (25.2x)	4610.8 (29.6x)	4332.3 (27.0x)	
QS	64	9.5 (-)	15.1 $(-)$	56.3 (-)	66.9 (-)	157.5 (-)	159.4 (-)	425.1 (-)	343.7 (-)	
VPred		62.2~(6.5x)	57.6 (3.8x)	355.2 (6.3x)	334.9(5.0x)	734.4 (4.7x)	706.8 (4.4x)	1309.7 (3.0x)	1420.7 (4.1x)	
IF-THEN-ELSE		$55.9 (5.9 \mathrm{x})$	55.1 (3.6x)	933.1 (16.6x)	935.3 (14.0x)	2496.5 (15.9x)	2428.6 (15.2x)	4662.0 (11.0x)	4809.6 (14.0x)	
STRUCT+		109.8 (11.6x)	116.8 (7.7x)	1661.7 (29.5x)	1554.6 (23.2x)	3040.7 (19.3x)	2937.3 (18.4x)	5437.0 (12.8x)	5456.4 (15.9x)	



Method	Λ	Number of trees/dataset								
		1,000		5,0	5,000 1		000	20,000		
		MSN-1	Y!S1	MSN-1	Y!S1	MSN-1	Y!S1	MSN-1	Y!S1	
QS		2.2 (-)	4.3 (-)	10.5 (-)	14.3 (-)	20.0 (-)	25.4 (-)	40.5 (-)	48.1 (-)	
VPred	8	7.9(3.6x)	8.5 (2.0x)	$40.2 (3.8 \mathrm{x})$	41.6 (2.9x)	80.5 (4.0x)	82.7 (3.3)	161.4 (4.0x)	164.8 (3.4x)	
IF-THEN-ELSE	0	8.2 (3.7x)	10.3 (2.4x)	81.0(7.7x)	85.8~(6.0x)	185.1 (9.3x)	185.8 (7.3x)	709.0 (17.5x)	772.2 (16.0x)	
STRUCT+		21.2 (9.6x)	23.1 (5.4x)	107.7 (10.3x)	112.6 (7.9x)	373.7 (18.7x)	390.8 (15.4x)	1150.4 (28.4x)	1141.6 (23.7x)	
QS		2.9 (-)	6.1 (-)	16.2 (-)	22.2 (-)	32.4 (-)	41.2 (-)	67.8 (-)	81.0 (-)	
VPred	16	16.0 (5.5x)	16.5 (2.7x)	82.4 (5.0x)	82.8 (3.7x)	165.5 (5.1x)	165.2 (4.0x)	336.4 (4.9x)	336.1 (4.1x)	
IF-THEN-ELSE		18.0 (6.2x)	21.8 (3.6x)	126.9 (7.8x)	130.0 (5.8x)	617.8 (19.0x)	406.6 (9.9x)	1767.3 (26.0x)	1711.4 (21.1x)	
STRUCT+		42.6 (14.7x)	41.0 (6.7x)	424.3 (26.2x)	403.9 (18.2x)	1218.6 (37.6x)	1191.3 (28.9x)	2590.8 (38.2x)	2621.2 (32.4x)	
QS		5.2 $(-)$	9.7 (-)	27.1 (-)	34.3 (-)	59.6 (-)	70.3 (-)	155.8 $(-)$	160.1 (-)	
VPred	32	31.9~(6.1x)	31.6 (3.2x)	$165.2 (6.0 \mathrm{x})$	162.2 (4.7x)	343.4 (5.7x)	336.6 (4.8x)	711.9 (4.5x)	694.8 (4.3x)	
IF-THEN-ELSE	02	34.5~(6.6x)	36.2 (3.7x)	300.9 (11.1x)	277.7 (8.0x)	1396.8 (23.4x)	1389.8 (19.8x)	3179.4 (20.4x)	3105.2 (19.4x)	
STRUCT+		69.1 (13.3x)	67.4 (6.9x)	928.6 (34.2x)	834.6 (24.3x)	1806.7 (30.3x)	1774.3 (25.2x)	4610.8 (29.6x)	4332.3 (27.0x)	
QS		9.5 (-)	15.1 $(-)$	56.3 (-)	66.9 (-)	157.5 (-)	159.4 (-)	425.1 (-)	343.7 (-)	
VPred	64	62.2 (6.5x)	57.6 (3.8x)	355.2 (6.3x)	334.9(5.0x)	734.4 (4.7x)	706.8 (4.4x)	1309.7 (3.0x)	1420.7 (4.1x)	
IF-THEN-ELSE		55.9(5.9x)	55.1 (3.6x)	933.1 (16.6x)	935.3 $(14.0x)$	2496.5 (15.9x)	2428.6 (15.2x)	4662.0 (11.0x)	4809.6 (14.0x)	
STRUCT+		109.8 (11.6x)	116.8 (7.7x)	1661.7 (29.5x)	1554.6 (23.2x)	3040.7 (19.3x)	2937.3 (18.4x)	5437.0 (12.8x)	5456.4 (15.9x)	



Method	Λ	Number of trees/dataset								
		1,000		5,0	5,000 1		000	20,000		
		MSN-1	Y!S1	MSN-1	Y!S1	MSN-1	Y!S1	MSN-1	Y!S1	
QS		2.2 (-)	4.3 (-)	10.5 (-)	14.3 (-)	20.0 (-)	25.4 (-)	40.5 (-)	48.1 (-)	
VPred	8	7.9(3.6x)	8.5 (2.0x)	$40.2 (3.8 \mathrm{x})$	41.6 (2.9x)	80.5 (4.0x)	82.7(3.3)	161.4 (4.0x)	164.8 (3.4x)	
IF-THEN-ELSE	0	8.2 (3.7x)	10.3 (2.4x)	81.0(7.7x)	85.8 (6.0x)	185.1 (9.3x)	185.8 (7.3x)	709.0 (17.5x)	772.2 (16.0x)	
STRUCT+		21.2 (9.6x)	23.1 (5.4x)	107.7 (10.3x)	112.6 (7.9x)	373.7 (18.7x)	390.8 (15.4x)	1150.4 (28.4x)	1141.6 (23.7x)	
QS		2.9 (-)	6.1 (-)	16.2 (-)	22.2 (-)	32.4 (-)	41.2 (-)	67.8 (-)	81.0 (-)	
VPred	16	16.0 (5.5x)	16.5 (2.7x)	82.4 (5.0x)	82.8 (3.7x)	165.5 (5.1x)	165.2 (4.0x)	336.4 (4.9x)	336.1 (4.1x)	
IF-THEN-ELSE		18.0 (6.2x)	21.8 (3.6x)	126.9(7.8x)	130.0 (5.8x)	617.8 (19.0x)	406.6 (9.9x)	1767.3 (26.0x)	1711.4 (21.1x)	
STRUCT+		42.6 (14.7x)	41.0 (6.7x)	424.3 (26.2x)	403.9 (18.2x)	1218.6 (37.6x)	1191.3 (28.9x)	2590.8 (38.2x)	2621.2 (32.4x)	
QS		5.2 (-)	9.7 (-)	27.1 (-)	34.3 (-)	59.6 (-)	70.3 (-)	155.8 (-)	160.1 (-)	
VPred	32	31.9~(6.1x)	31.6 (3.2x)	165.2 (6.0x)	162.2 (4.7x)	343.4 (5.7x)	336.6 (4.8x)	711.9 (4.5x)	694.8 (4.3x)	
IF-THEN-ELSE	52	34.5~(6.6x)	36.2 (3.7x)	300.9 (11.1x)	277.7 (8.0x)	1396.8 (23.4x)	1389.8 (19.8x)	3179.4 (20.4x)	3105.2 (19.4x)	
STRUCT+		69.1 (13.3x)	67.4 (6.9x)	928.6 (34.2x)	834.6 (24.3x)	1806.7 (30.3x)	1774.3 (25.2x)	4610.8 (29.6x)	4332.3 (27.0x)	
QS	64	9.5 (-)	15.1 (-)	56.3 (-)	66.9 (-)	157.5 $(-)$	159.4 (-)	425.1 (-)	343.7 (-)	
VPred		62.2 (6.5x)	57.6 (3.8x)	355.2 (6.3x)	334.9(5.0x)	734.4 (4.7x)	706.8 (4.4x)	1309.7 (3.0x)	1420.7 (4.1x)	
IF-THEN-ELSE	04	55.9(5.9x)	55.1 (3.6x)	933.1 (16.6x)	935.3 (14.0x)	2496.5 (15.9x)	2428.6 (15.2x)	4662.0 (11.0x)	4809.6 (14.0x)	
STRUCT+		109.8 (11.6x)	116.8 (7.7x)	1661.7 (29.5x)	1554.6 (23.2x)	3040.7 (19.3x)	2937.3 (18.4x)	5437.0 (12.8x)	5456.4 (15.9x)	



Method	Λ	Number of trees/dataset								
		1,000		5,000		10,	10,000		20,000	
		MSN-1	Y!S1	MSN-1	Y!S1	MSN-1	Y!S1	MSN-1	Y!S1	
QS		2.2 (-)	4.3 (-)	10.5 (-)	14.3 (-)	20.0 (-)	25.4 (-)	40.5 (-)	48.1 (-)	
VPred	8	7.9 (3.6x)	8.5 (2.0x)	$40.2 (3.8 \mathrm{x})$	41.6 (2.9x)	80.5 (4.0x)	82.7 (3.3)	161.4 (4.0x)	164.8 (3.4x)	
IF-THEN-ELSE	0	8.2 (3.7x)	10.3 (2.4x)	81.0(7.7x)	85.8~(6.0x)	185.1 (9.3x)	185.8 (7.3x)	709.0 (17.5x)	772.2 (16.0x)	
STRUCT+		21.2 (9.6x)	23.1 (5.4x)	107.7 (10.3x)	112.6 (7.9x)	373.7 (18.7x)	390.8 (15.4x)	1150.4 (28.4x)	1141.6 (23.7x)	
QS		2.9 (-)	6.1 (-)	16.2 (-)	22.2 (-)	32.4 (-)	41.2 (-)	67.8 (-)	81.0 (-)	
VPred	16	16.0 (5.5x)	16.5 (2.7x)	82.4 (5.0x)	82.8 (3.7x)	165.5 (5.1x)	165.2 (4.0x)	336.4 (4.9x)	336.1 (4.1x)	
IF-THEN-ELSE		18.0 (6.2x)	21.8 (3.6x)	126.9 (7.8x)	130.0 (5.8x)	617.8 (19.0x)	406.6 (9.9x)	1767.3 (26.0x)	1711.4 (21.1x)	
STRUCT+		42.6 (14.7x)	41.0 (6.7x)	424.3 (26.2x)	403.9 (18.2x)	1218.6 (37.6x)	1191.3 (28.9x)	2590.8 (38.2x)	2621.2 (32.4x)	
QS		5.2 (-)	9.7 (-)	27.1 (-)	34.3 (-)	59.6 (-)	70.3 (-)	155.8 $(-)$	160.1 (-)	
VPred	32	31.9(6.1x)	31.6 (3.2x)	$165.2 (6.0 \mathrm{x})$	162.2 (4.7x)	343.4 (5.7x)	336.6 (4.8x)	711.9 (4.5x)	694.8 (4.3x)	
IF-THEN-ELSE	02	34.5~(6.6x)	36.2 (3.7x)	300.9 (11.1x)	277.7 (8.0x)	1396.8 (23.4x)	1389.8 (19.8x)	3179.4 (20.4x)	3105.2 (19.4x)	
STRUCT+		69.1 (13.3x)	67.4 (6.9x)	928.6 (34.2x)	834.6 (24.3x)	1806.7 (30.3x)	1774.3 (25.2x)	4610.8 (29.6x)	4332.3 (27.0x)	
QS	64	9.5 (-)	15.1 $(-)$	56.3 (-)	66.9 (-)	157.5 (-)	159.4 (-)	425.1 (-)	343.7 (-)	
VPred		62.2 (6.5x)	57.6 (3.8x)	355.2 (6.3x)	334.9(5.0x)	734.4 (4.7x)	706.8 (4.4x)	1309.7 (3.0x)	1420.7 (4.1x)	
IF-THEN-ELSE		55.9(5.9x)	55.1 (3.6x)	933.1 (16.6x)	935.3 $(14.0x)$	2496.5 (15.9x)	2428.6 (15.2x)	4662.0 (11.0x)	4809.6 (14.0x)	
STRUCT+		109.8 (11.6x)	116.8 (7.7x)	1661.7 (29.5x)	1554.6 (23.2x)	3040.7 (19.3x)	2937.3 (18.4x)	5437.0 (12.8x)	5456.4 (15.9x)	



Questions & Comments





Università La Sapienza – 18 October 2016